

# Universidad de El Salvador

Facultad de Ciencias Naturales y Matemática

Escuela de Química



***“Parámetros cinéticos de la degradación térmica del Betacaroteno en  
aceite de palma crudo”***

**Trabajo de graduación presentado por:**

Katia Marixa Guerrero de Arévalo

**Asesores: Lic. Hugo Alexander Estrada Pérez**

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Ciudad Universitaria, Febrero 2021

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# Universidad de El Salvador

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## ***Dedicatoria***

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Por su invaluable sacrificio y su fuerza.

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# 1 Resumen

Este trabajo presenta un estudio de los parámetros cinéticos que describen la degradación del aporte nutritivo que provee el  $\beta$ -caroteno en el aceite de palma crudo, cuando este es sometido a un proceso fisicoquímico para su refinación y posterior consumo.

Haciendo una evaluación de dos técnicas de análisis: HPLC y Espectrofotometría UV/VIS, las cuales presentaban un alcance prometedor en la generación de resultados se concluyó que para este estudio y las condiciones involucradas favorece más el uso del Espectrofotómetro UV/VIS ya que se reduce ampliamente el consumo de solventes y el tiempo entre cada análisis.

Se determinó la concentración del carotenoide empleando una curva de calibración elaborada con un estándar de  $\beta$ -caroteno (90% pureza, HPLC) donado por la empresa SUMMA Industrial, S.A de C.V, en donde además se tomaron las muestras de aceite de palma necesarias para el desarrollo de la investigación. La concentración de  $\beta$ -caroteno fue de 3150 ppm, un dato que se justifica con la procedencia e historial del fruto.

El estudio de la variación del  $\beta$ -caroteno en función del tiempo se realizó monitoreando las absorbancias en diferentes rangos de tiempo empleando una longitud de onda de 450 nm.

Al finalizar se obtuvo que la cinética de degradación sigue un orden 1 y obedece la Ley de Arrhenius al igual que en la mayoría de bibliografía consultada. Además, se calcularon satisfactoriamente los parámetros cinéticos con los que se genera un antecedente en nuestro país para cualquier estudio relacionado con procesos térmicos al aceite de palma crudo.

La energía de activación para el aceite de palma cruda fue de 75972.8 J/mol, comparado con el aceite de oleína de palma que posee un valor más elevado implica que su degradación térmica es mucho más rápida lo cual se atribuye al efecto matriz evidenciado a lo largo de este estudio.

## 2 Objetivos

### 2.1 Objetivo general

Caracterizar la cinética química proximal de la degradación térmica del Betacaroteno en el aceite de palma.

### 2.2 Objetivos específicos

- i. Comparar las técnicas HPLC y espectroscopía UV-Vis en el seguimiento de la concentración de Betacaroteno en aceite de palma crudo durante la degradación térmica.
- ii. Escoger la técnica de seguimiento de la concentración del Betacaroteno para el método cinético a establecer.
- iii. Establecer la curva de calibración empleando un estándar de Betacaroteno.
- iv. Someter las muestras de aceite de palma crudo a diferentes temperaturas y darle seguimiento a la concentración, en función del tiempo, del Betacaroteno.
- v. Determinar los parámetros cinéticos de orden de reacción, constante cinética y energía de activación, tiempo de vida media y tiempo de reducción decimal para el Betacaroteno en la matriz de aceite de palma crudo.

### 3 Marco Teórico

#### 3.1 Generalidades de la Palma africana (*Elaeis guineensis* Jacq.)

La palma aceitera es la especie oleaginosa vegetal que produce mayor cantidad de aceite por unidad de hectárea. Debido a la abundancia en su producción los costos son bajos mientras que sus usos y aplicaciones son variados. La producción del aceite de palma se convirtió en la materia prima de la producción de aceites vegetales a nivel mundial por arriba de la soya. [1] [2] [3] [4]

La palma de aceite es una planta tropical propia de climas cálidos que crece en tierras por debajo de los 500 metros sobre el nivel del mar. Su origen se ubica en el golfo de Guinea, África Occidental. De ahí su nombre científico: *Elaeis guineensis* Jacq. Siendo su denominación popular: palma africana de aceite. [5] [6]



Figura 1 Imagen botánica de *Elaeis guineensis* Jacq. [7]

### 3.1.1 Fruto de Palma africana

El fruto de palma está constituido por 4 secciones:

- a. Exocarpio: Es la capa epidérmica delgada y cerosa (cáscara).
- b. Mesocarpio: Es la pulpa de donde se obtiene el aceite.
- c. Endocarpio: Es la que junto con la almendra forma la semilla.
- d. Endospermo: Conocida mayormente como almendra o palmiste.



Figura 2 Partes del fruto de *Elaeis guineensis* Jacq. [8]

El aceite de palma se extrae del mesocarpio del fruto de la semilla de la palma africana a través de diversos procedimientos, siendo el más común el prensado en frío. [6] [9] [10]

### 3.1.2 Composición del Aceite de Palma

Está constituido por una mezcla de ésteres de glicerol (triglicéridos) y es fuente natural de carotenos (provitamina A) y vitamina E en forma de tocotrienoles. [6] [11] [12] [13] [14]

#### 3.1.2.1 Componentes mayoritarios

El perfil de ácidos grasos de un aceite define sus fortalezas y limitaciones para diferentes aplicaciones alimentarias. La tecnología ha realizado avances en los que modifican sus características, para ampliar sus usos alimentarios y potencializar sus beneficios nutricionales. [4] [15]

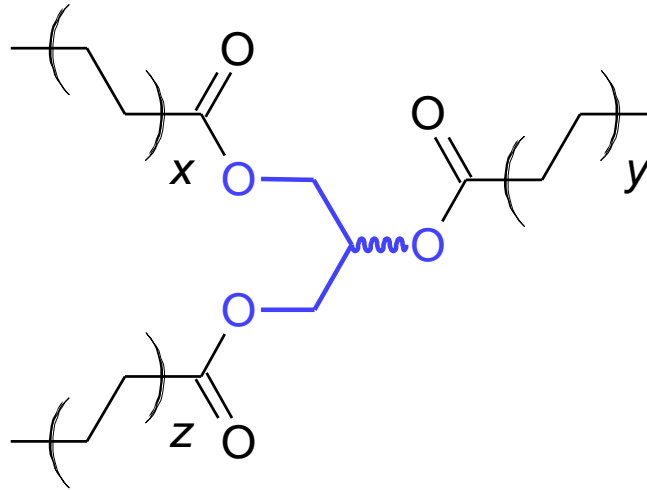


Figura 3 Estructura básica de un triglicérido, en azul la unidad del glicerol. Las longitudes de los ácidos grasos variarán atendiendo el tipo de ácido unido al glicerol.

La composición del aceite de palma consiste principalmente en ácidos grasos esterificados con el glicerol (glicéridos), y un contenido estimado entre 2.3-6.7% de ácidos grasos libres; estos ácidos grasos poseen una relación aproximada de 1:1 entre saturados e insaturados. La importancia de este producto en la industria se relaciona con su estabilidad y resistencia a la rancidez oxidativa; dada la especial resistencia que presenta este aceite, es una alternativa empleada para sustituir aceites insaturados en formulaciones de alimentos, además es empleado en preparaciones que requieren elevadas temperaturas, como las frituras prolongadas y los productos horneados; gracias a su versatilidad, dada por su composición de ácidos grasos saturados e insaturados y su aporte nutricional, el aceite de palma y las fracciones líquida (oleína) y sólida (estearina) son empleadas en la elaboración de margarinas, mezclas de aceites, grasas de repostería y confitería, etc. [6] [11] [15] [16] [17] [18] [19] [20]

Tabla 1 Composición de ácidos grasos en aceite de palma crudo y refinado, blanqueado y desodorizado. [11]

| Ácido graso        | Composición de ácidos grasos (%p/p) |   |
|--------------------|-------------------------------------|---|
|                    | Aceite de palma crudo               | Aceite de palma refinado, blanqueado y desodorizado |
| <b>Saturados</b>   |                                     |   |
| Palmítico          | 45.48                               | 46.30   |
| Esteárico          | 3.49                                | 3.52  |
| Mirístico          | 0.93                                | 0.92  |
| Total              | 49.91                               | 50.74   |
| <b>Insaturados</b> |                                     |   |
| Oleico             | 40.17                               | 39.58   |
| Linoleico          | 9.92                                | 9.68  |
| Total              | 50.09                               | 49.26   |



Tabla 2 Composición de glicéridos para ácidos Palmítico (P), Estéarico (E), Mirístico (M), Oleico (O), Linoleico (L) en aceite de palma crudo y refinado, blanqueado y desodorizado. [11]

| Ácido graso          | Composición de glicéridos (%p/p) |   |
|----------------------|----------------------------------|---|
|                      | Aceite de palma crudo            | Aceite de palma refinado, blanqueado y desodorizado |
| Triglicéridos        | 93.60                            | 94.80   |
| Diglicéridos         | 6.32                             | 5.20  |
| <b>Trisaturados</b>  |                                  |   |
| PPP                  | 4.81                             | 5.51  |
| MMP                  | 2.38                             | 1.70  |
| MMM                  | 0.76                             | 0.42  |
| Total                | 7.95                             | 8.69  |
| <b>Disaturados</b>   |                                  |   |
| PPO                  | 27.39                            | 29.62   |
| PPL                  | 9.37                             | 9.23  |
| POE                  | 5.29                             | 4.90  |
| MPL                  | 3.03                             | 2.20  |
| EOE                  | 1.36                             | -   |
| Total                | 46.63                            | 45.95   |
| <b>Monosaturados</b> |                                  |   |
| POO                  | 21.39                            | 23.26   |
| PLO                  | 10.02                            | 9.68  |
| OOE                  | 2.78                             | 2.24  |
| Total                | 34.1                             | 35.18   |
| <b>Triinsaturado</b> |                                  |   |
| OOO                  | 3.90                             | 4.40  |
| OOL                  | 1.22                             | 0.58  |
| Total                | 5.12                             | 4.98  |

### 3.1.2.2 Componentes minoritarios del aceite de palma crudo

El aceite de palma crudo contiene cerca del 1% de componentes minoritarios, incluyendo carotenoides, tocoferoles, esteroides, alcoholes triterpénicos, fosfolípidos, glicolípidos e hidrocarburos terpénicos y parafínicos. La importancia nutricional de tales componentes como los carotenoides y tocoferoles también mejora la estabilidad del aceite. Aunque son productos del alto valor, los carotenoides desafortunadamente son destruidos en el proceso de refinado, aunque existen diversos métodos prometedores de extracción. Los tocoferoles, al ser antioxidantes naturales, deben ser preservados cuidadosamente durante el procesado del aceite de palma, El papel de los fosfolípidos frecuentemente es mal entendido, debido a su

capacidad dual de acción, cómo un sinergista antioxidante o un agente tensoactivo que dispersa las impurezas en el aceite. En el aceite de palma crudo el contenido de fosfolípidos es pequeño debido principalmente a la mayor pérdida de éste durante el molido; el contenido de fósforo proviene principalmente de fósforo inorgánico. Entre los esteroides, el colesterol constituye un porcentaje demasiado bajo para ser considerado. [21] [22] [23] [24]

### 3.1.2.2.1 Carotenoides

El contenido de carotenoides en el aceite de palma crudo varía dependiendo de la zona de cultivo, las condiciones ambientales, la calidad de la cosecha, especie, tipo de procesado realizado, etc. En estudios realizados el valor de los carotenoides suele oscilar entre 500-700 ppm, sin embargo, especies como *E. guineensis* fo. *dura* reportan concentraciones hasta de 800-1600 ppm. [21] [25]

Un análisis típico de composición de carotenoides muestra al  $\beta$ - y  $\alpha$ - caroteno como los mayoritarios (54 y 36% respectivamente), siendo el resto  $\gamma$ -caroteno, licopeno y xantofilas (cómo la cataxantina). [25] [26]

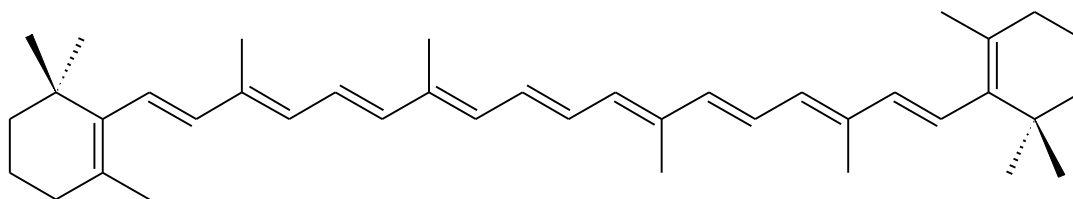


Figura 4  $\beta$ -caroteno

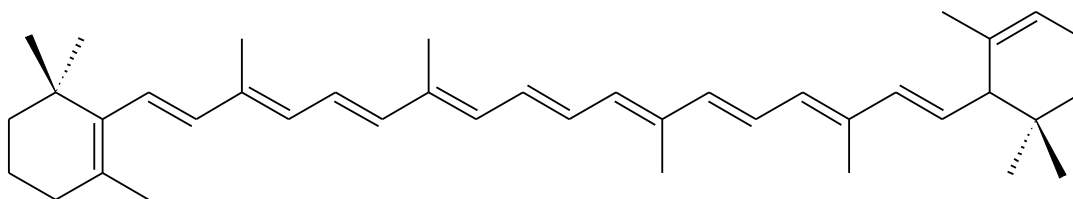


Figura 5  $\alpha$ -caroteno

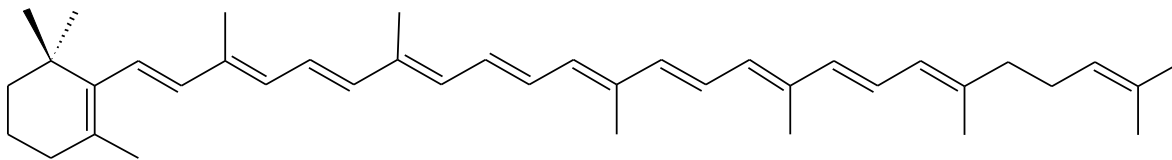


Figura 6  $\gamma$ -caroteno

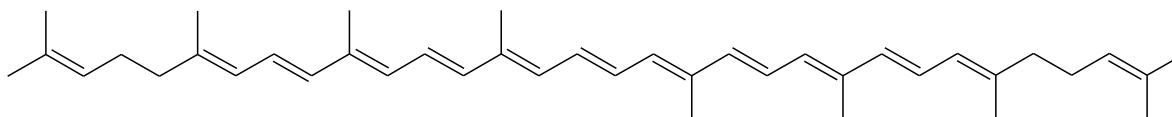


Figura 7 Licopeno

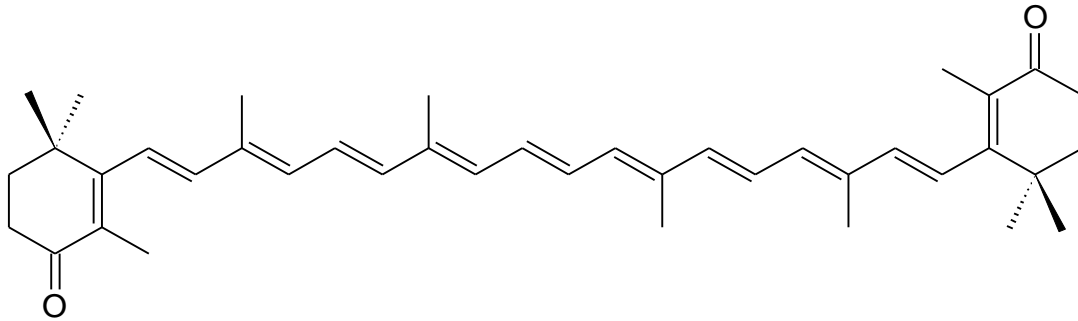


Figura 8 cataxantina

Los carotenoides son precursores de vitamina A (Retinol), con el  $\beta$ -caroteno con la mayor actividad de provitamina A, pudiendo *transformarse in vivo*. La producción mundial del aceite de palma crudo ronda los 6 millones de toneladas, la cantidad respectiva de carotenoides estaría entre 3000-4200 toneladas. El aceite de palma crudo ha sido usado durante mucho tiempo por los africanos como fuente de vitamina A, sin embargo, en el resto del mundo no se considera una fuente aceptable por su contenido de ácidos grasos libres (sin esterificar con el glicerol). Contrariamente, la mayor parte de los carotenoides son destruidos por el proceso de refinado que consiste en el blanqueo, desodorizado y desacidificado del aceite; lo anterior ha motivado la búsqueda de técnicas y métodos viables de extracción, inclusive, los concentrados de  $\beta$ -caroteno pueden tener un alto valor comercial. [21] [24] [25] [26] [27]

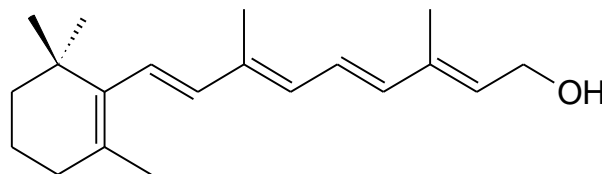


Figura 9 Retinol (Vitamina A)

### 3.1.2.2.2 Tocoferoles y Tocotrienoles (Tococromanos)

Tocoferoles y Tocotrienoles están presentes en el aceite de palma en un rango variable, siendo un rango general entre 600-1000 ppm. Dichos compuestos son antioxidantes naturales importantes que también funcionan como vitamina E. Es sabido que los tocoferoles, en especial el  $\alpha$ -tocoferol, presentan actividad antioxidante frente a reacciones en cadena radicalarias comparado con análogos sintéticos que no son aceptados globalmente, por tanto, el contenido de tocoferoles constituye un parámetro importante de calidad. Los principales constituyentes del aceite de palma son 44%  $\gamma$ -tocotrienol, 22%  $\alpha$ -tocoferol y 12%  $\delta$ -tocotrienol; el resto  $\alpha$ - y  $\beta$ -tocotrienoles y  $\beta$ -,  $\gamma$ - y  $\delta$ -tocoferoles. El aceite de palma, a pesar de ser relativamente resistente a la degradación oxidativa por sus niveles bajos de polinsaturación, los tocoferoles aún permanecen como antioxidantes útiles y su pérdida durante el procesado debe ser minimizado. [21] [28] [29] [30] [31] [32]

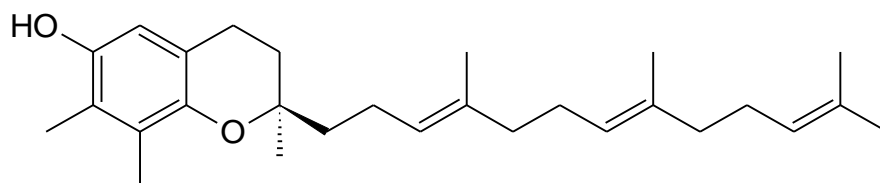


Figura 10  $\gamma$ -tocotrienol

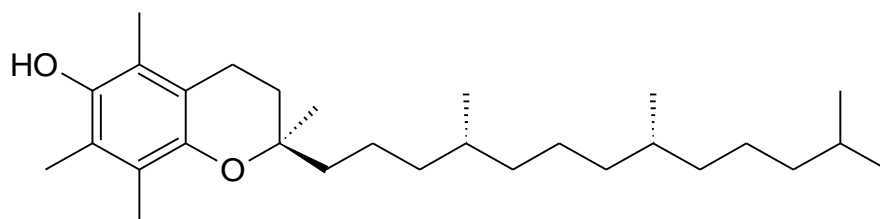


Figura 11  $\alpha$ -tocoferol

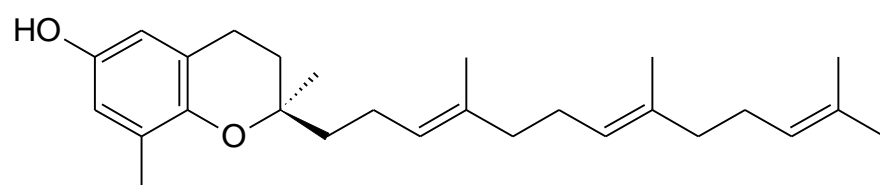


Figura 12  $\delta$ -tocotrienol

### 3.1.2.2.3 Esteroles

Los fitosteroles están presentes en el aceite de palma, siendo los mayoritarios sitosterol, campesterol y estigmasterol mientras que una pequeña fracción de colesterol está presente. El nivel de colesterol en los aceites vegetales es mínimo y junto con otros esteroides es disminuido aún más en el refinado. Los esteroides y sus ésteres, que también han sido detectados, aparentemente no poseen funcionalidad en el aceite, ni tampoco presentan un efecto negativo sobre éste; sin embargo, se ha sugerido que ciertos esteroides pueden proteger el aceite de polimerizaciones oxidativas durante el freído. Su presencia en la composición insaponificable, junto con otros componentes minoritarios, puede emplearse como huella dactilar para el aceite, es decir, para la detección de adulteración o mezclado. Dichos esteroides tienen el potencial, de ser extraídos, de conversión en derivados esteroidales, insecticidas fitosterólicos etc. [21] [23] [24] [33] [34]

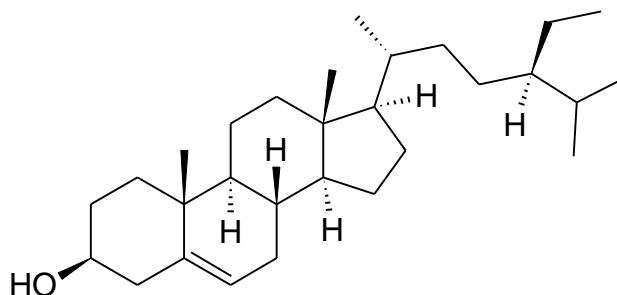


Figura 13  $\beta$ -sitosterol

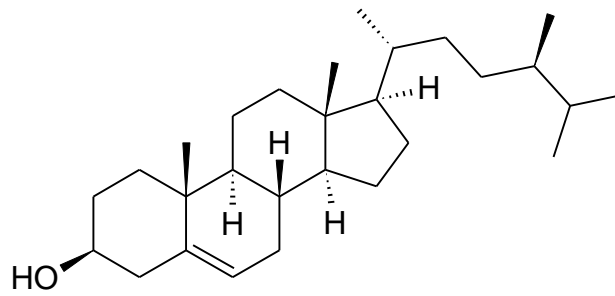


Figura 14 campesterol

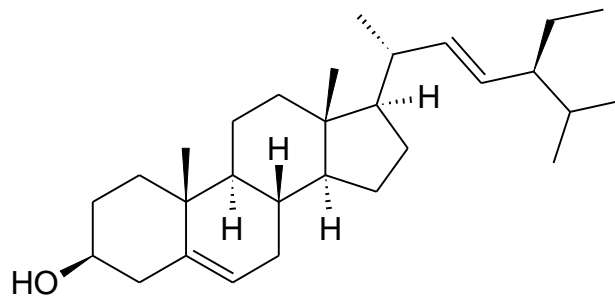


Figura 15 stigmasterol

#### 3.1.2.2.4 Lípidos polares

Los fosfolípidos y glicolípidos son lípidos polares presentes en el aceite de palma, donde los primeros reciben atención considerable por su posible efecto perjudicial sobre la calidad del aceite. Ambos tipos de lípidos constituyen una parte importante de las membranas celulares, además de poseer una estructura anfifílica, debido a esta propiedad, aunque las cantidades sean pequeñas pueden facilitar la dispersión de impurezas microparticuladas que incluyen hierro y otras sustancias indeseadas. El fosfolípido mayoritario en el aceite de palma es la fosfatidilcolina mientras que el glicolípidos corresponde al monogalactosildiglicérido. Ambos tipos de lípidos son eliminados casi por completo en el proceso de refinado, que puede incluir lavado, tratamiento con ácido fosfórico y adsorción con arcilla o tierras. [21] [31] [35] [36] [37] [38] [39] [40]

Por otra parte, estudios más detallados mostraron contrariamente que la mayor fuente de fósforo en el aceite de palma proviene del fosfato inorgánico comparado con el contenido de fosfolípidos. De manera general el contenido de fósforo inorgánico es cerca de ocho veces mayor que el fósforo proveniente de los fosfolípidos. Las dos formas de fósforo juegan un papel diferente; adicionalmente al efecto estabilizador de las dispersiones coloidales, los fosfolípidos han sido descritos como sinergistas de los antioxidantes mientras que el fosforo inorgánico puede ser indeseable. La adición de fosfolípidos ha demostrado una correlación positiva con la estabilidad oxidativa, limitando las cantidades de agua residual. El fosfato inorgánico no es deseado por acompañar al metal pro oxidante hierro en correlación con la cantidad de ácidos grasos libres en el aceite. Fósforo residual en aceite blanqueado y

desodorizado, remanente de un procesamiento deficiente, está correlacionado con el aumento de ácidos grasos libres durante el *transporte*. Como resultado, una buena práctica consiste en evitar el aumento del contenido de fósforo, es decir, remanentes de ácido fosfórico después del desgomado durante el refinado. Mientras que el fosfato o el ácido fosfórico pueden reaccionar con los fosfolípidos, su reacción con los glicéridos a alta temperatura no puede ser evitada. Los fosfolípidos y glicolípidos pueden formar micelas inversas, vesículas o gotas en emulsión, eliminando así los metales pro oxidantes y sus sales hidrofílicas de la fase lipídica, disminuyendo así su efectividad en la promoción de la autoxidación. El secuestro directo de iones metálicos por los lípidos polares tampoco se puede descartar en la acción sinérgica antioxidante. Los fosfolípidos no son en sí antioxidantes, pero trabajan en conjunción con antioxidantes como los tocoferoles. [35] [40] [41]

Fase hidrofóbica

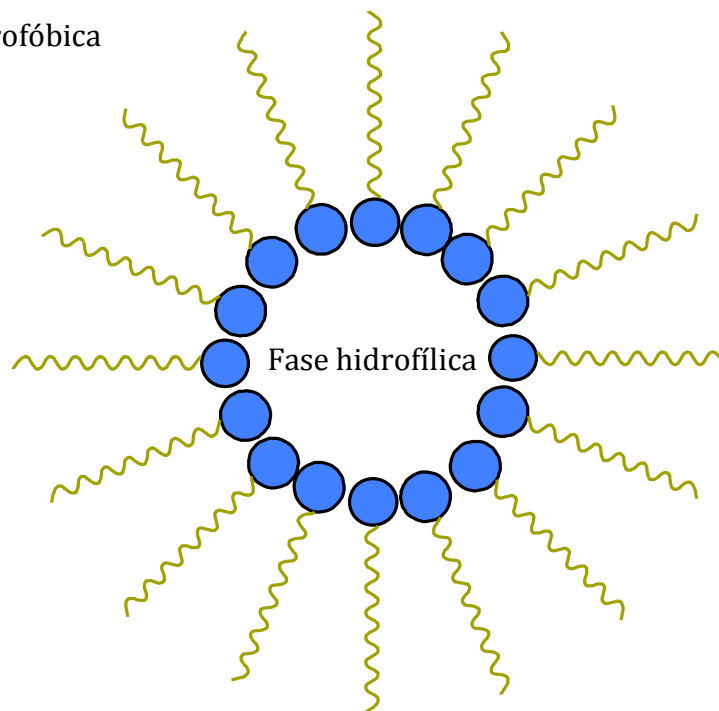


Figura 16 Esquema de una micela inversa formada por moléculas anfifílicas

Los glicolípidos, aunque en mayor proporción comparados con los fosfolípidos, es presumible su poca contribución a la calidad del aceite de palma crudo. En el peor de los casos, junto con los fosfolípidos, pueden contribuir a aumentar el microparticulado y otras impurezas en los aceites. [35] [40] [41]

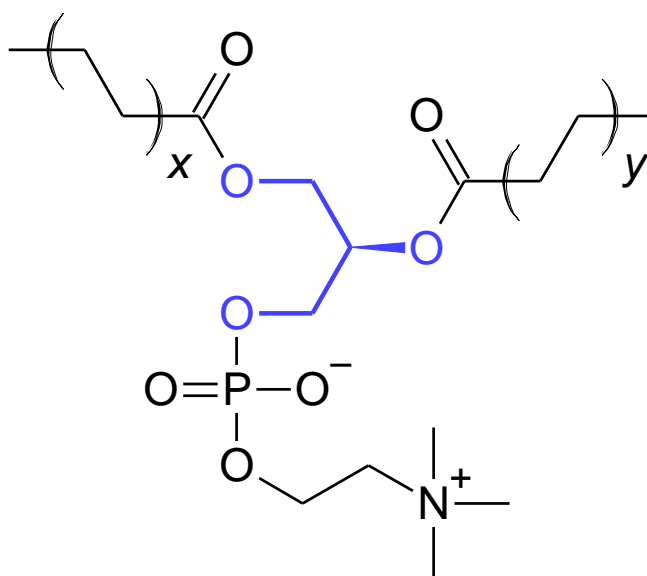


Figura 17 Fosfatidilcolina

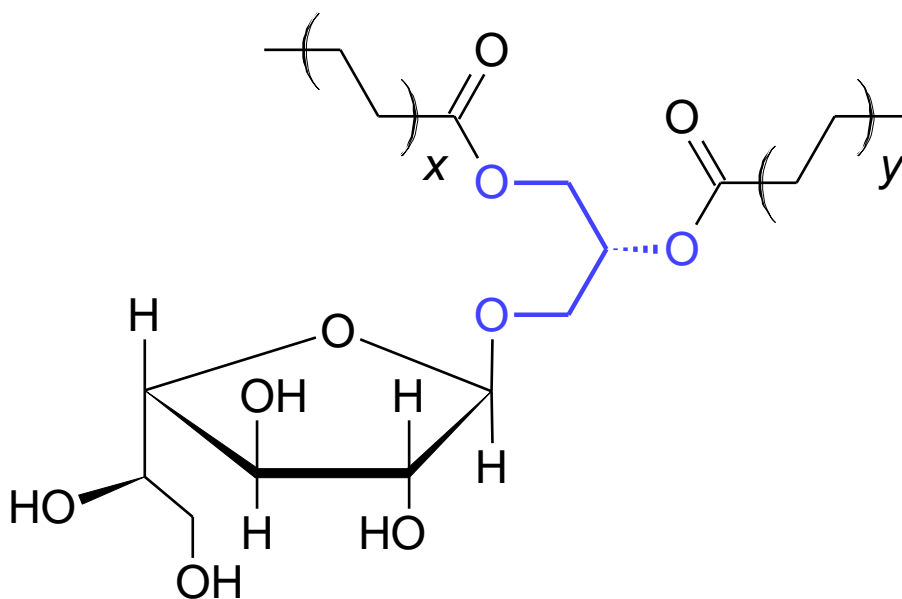


Figura 18 monogalactosil diglicérido

### 3.1.2.2.5 Impurezas

Los componentes no lipídicos, excluyendo humedad, pueden ser considerados como impurezas. La extracción del mesocarpio del fruto de palma también genera la acumulación de trazas de contaminantes inorgánicos y orgánicos. Contaminantes metálicos como el hierro y el cobre son conocidos como agentes pro oxidantes en cantidades catalíticas. Las impurezas de hierro son derivadas del desgaste y abrasión de la maquinaria de molienda y puede ser

minimizada utilizando acero inoxidable en puntos estratégicos en el proceso de extracción o con extracción magnética. La mayor parte del hierro residual se encuentra particulado y mezclado con material inorgánico (compuestos de Ca, Mg, fosfatos, etc.) tanto como proteico y celulósico. Existe una gran probabilidad que estos componentes se encuentren en suspensión coloidal tal como lo evidencia la separación de dichos componentes mediante centrifugación. La presencia de los lípidos polares (fosfo y glico lípidos) puede ser parcialmente responsable por el comportamiento coloidal. Se conoce menos sobre otras impurezas como compuestos fenólicos, taninos y trazas de flavonoides; la mayoría de estos se originan a partir de los sépalos, exocarpio, fibra y pericarpio del fruto de palma. La presencia de estas y otras impurezas polares debe ser tomada en cuenta al tener el potencial de formar compuestos coloreados al oxidarse. [21] [24] [42]

En resumen, el contenido principal de constituyentes menores se resume en la siguiente tabla:

*Tabla 3 Componentes minoritarios del aceite de palma crudo. [25]*

| <b>Constituyente</b>                       | <b>ppm</b> |
|--|------------|
| Tocoferoles y tocotrienoles                | 600-1000   |
| Carotenoides                               | 500-700    |
| Esteroles                                  | 326-527    |
| Escualeno                                  | 200-500    |
| Alcoholes alifáticos                       | 100-200    |
| Fosfolípidos                               | 5-130      |
| Alcoholes triterpénicos y metil esteroides | 40-80      |
| Hidrocarburos alifáticos                   | 50         |

## 3.2 Cinética de degradación del $\beta$ -caroteno

### 3.2.1 Introducción:

La cantidad de  $\beta$ -caroteno en las frutas, procesados derivados de éstas (por ejemplo aceite, jugo, puré, etc.) y vegetales es un parámetro importante desde el punto de vista nutricional y comercial, considerando éstos como las principales fuentes de  $\beta$ -caroteno y precursores de vitamina A. [12] [13] [14] [43] [44] [45] [46]

Por tanto, una justificación de interés comercial y de nutrición es la garantía de la máxima preservación del contenido de  $\beta$ -caroteno ya sea en productos terminados o en la búsqueda de la extracción directa del  $\beta$ -caroteno como producto final.

Planteado lo anterior, es de esencial importancia el conocimiento de la cinética de degradación del  $\beta$ -caroteno para la determinación del tiempo de caducidad (en productos de consumo; jugos, por ejemplo) o tiempos de operación industrial que busquen disminuir las pérdidas por degradación en el procesado. Diversos estudios indican pérdidas significativas durante el procesado y almacenaje por factores como tiempo, temperatura y oxígeno. [47] [48] [49] [50] [51] [52]



El conocimiento cuantitativo de los parámetros que afectan la degradación del compuesto en este estudio es, por tanto, importante para el diseño de los procesos y/o la elección de las mejores condiciones de guardado y *transporte* para asegurar los productos con la mayor concentración posible.

### 3.2.2 Modelos cinéticos del $\beta$ -caroteno

La mayoría de estudios en muestras alimenticias reportan una cinética de primer orden (Ecuación 1) respecto a la concentración de  $\beta$ -caroteno. [49] [53] [54] [55]

$$\ln\left(\frac{[\beta - \text{caroteno}]_t}{[\beta - \text{caroteno}]_{t=0}}\right) = -kt \quad (1)$$

Donde  $[\beta - \text{caroteno}]$  es el contenido de  $\beta$ -caroteno,  $k$  la constante cinética de reacción y  $t$  el tiempo *transcurrido*.

Algunos estudios representan el modelo como una inactivación cinética de microorganismos durante los procesos térmicos. [56] [57] [58]

$$\log\left(\frac{[\beta - \text{caroteno}]_t}{[\beta - \text{caroteno}]_{t=0}}\right) = -\frac{t}{D} \quad (2)$$

Donde  $D$  es el tiempo de reducción decimal en minutos (el tiempo requerido para reducir la concentración del  $\beta$ -caroteno en un 90%). La relación existente entre los dos modelos anteriores se deduce como sigue. [58]

$$D = \frac{\ln 10}{k} \quad (3)$$

Para un número considerable de muestras es aplicable el modelo de primer orden. Desde este modelo resulta sencillo obtener la constante cinética de reacción. Sin embargo, algunos estudios han logrado una mejor correlación entre el modelo y los datos experimentales con órdenes de reacción superiores a uno para la degradación del *trans*- $\beta$ -caroteno en solventes no polares. Se ha asociado lo anterior a las reacciones de isomerización que son particularmente importantes en dichos solventes. [59] [60] [61]

La concentración de  $\beta$ -caroteno puede ser obtenida mediante HPLC, espectrofotometría, o la medición de una propiedad física asociada al contenido de  $\beta$ -caroteno, como el color. Cada uno de los métodos realizados presenta las ventajas y desventajas de la técnica empleada; por ejemplo, el HPLC presenta los mejores datos en términos de exactitud y *precisión* (con ventaja de separación de las muestras complejas y los productos de degradación), pero adolece de un pre tratamiento de muestra, uso de solventes de calidad HPLC y tiempo de análisis mayores, lo cual incrementa los costos significativamente. Por otra parte, las técnicas espectrofotométricas ofrecen menores tiempos y tratamiento de muestra, menor uso de solventes, buena exactitud y buena *precisión*, pero presenta las desventajas de no separar la

muestra, lo que da pie a una absorción del isómero *cis* y productos de degradación que absorban entre 450-455 nm. [54] [62] [63] [64] [65] [66] [67] [68] [69] [70]

### 3.2.3 Mecanismo de degradación

El mecanismo de degradación del  $\beta$ -caroteno puede ser descrito como complejo y no comprendido completamente hasta el momento. Mas, sin embargo, algunas evidencias han permitido elucidar parte del problema, siendo uno de los factores primordiales en la oxidación la isomerización *cis-trans*, la cual da paso a la formación de un diradical singlete. [71] [72]

Una de las primeras evidencias sobre el mecanismo de degradación del  $\beta$ -caroteno fue el aislamiento de una serie de  $\beta$ -apocarotenales, lo cual fue confirmado al seguir una ruta oxidativa con  $H_2O_2/OsO_4$ ; se ha determinado que estos productos son los principales en la oxidación del  $\beta$ -caroteno en extractos de tejido vegetal y oxidación química. [73] [74]

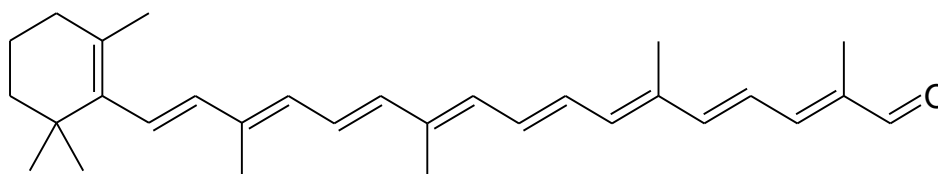


Figura 19  $\beta$ -apo-8'-carotenal

La identificación de estos productos condujo a la propuesta de un mecanismo de ruptura excéntrica (no central). En este proceso, el  $\beta$ -caroteno es escindido por un mecanismo  $\beta$ , empezando en cualquier extremo del sistema conjugado, produciendo una serie de apocarotenales. Cuando se alcanza el doble enlace central 15, 15', la oxidación subsecuente es bloqueada por el grupo metilo en posición  $C_{13}$ , el cual está en posición  $\beta$  desde el doble enlace central. Esto sin embargo ha dejado una interrogante sin responder, ¿en qué punto del sistema conjugado se da el ataque inicial? Es sabido que el primer paso de degradación debe ocasionar una isomerización de todo el  $\beta$ -caroteno *trans* al isómero *cis*, con el paso subsecuente de formación de una especie biradical o es un paso simultaneo y reversible (ver figura 20). [73]

Ha sido sugerido que la formación del isómero 15, 15' *cis* a 13'-*cis*- $\beta$ -caroteno puede dar lugar a sistemas conjugados más cortos, generando así un debilitamiento de la deslocalización  $\pi$  del sistema conjugado. Se ha observado que los productos de oxidación del  $\beta$ -caroteno son idénticos ya sea empleando oxígeno molecular u oxígeno singlete, como conclusión el mecanismo debe involucrar especies radicales para explicar la similitud de los productos en ambas reacciones. Si se forma la especie diradical de  $\beta$ -caroteno, esta solo puede originarse cuando el  $\beta$ -caroteno está en forma *cis*, como resultado el ataque del oxígeno será beneficiado

en cualquier extremo del enlace *cis* formando radicales  $\beta$ -carotenil peroxilo, seguidos por reacciones subsecuentes según figura 20. El ataque radical seguido por una sustitución interna homolítica genera epóxidos, que aparecen como productos iniciales. Los productos estables, apocarotenales y apocaronenonas, pueden generarse a partir de radicales peroxilo formados por el ataque del oxígeno en cualquier posición del diradical. Dicho radical peroxilo sufre una reacción de sustitución intramolecular de radicales ( $S_{H1}$ ) para formar dioxetanos, los cuales se descomponen para formar aldehídos y cetonas; esto se considera así por el hecho que todos los apocarotenales comienzan a aparecer al mismo tiempo. [72] [75] [76] [77] [78] [79]

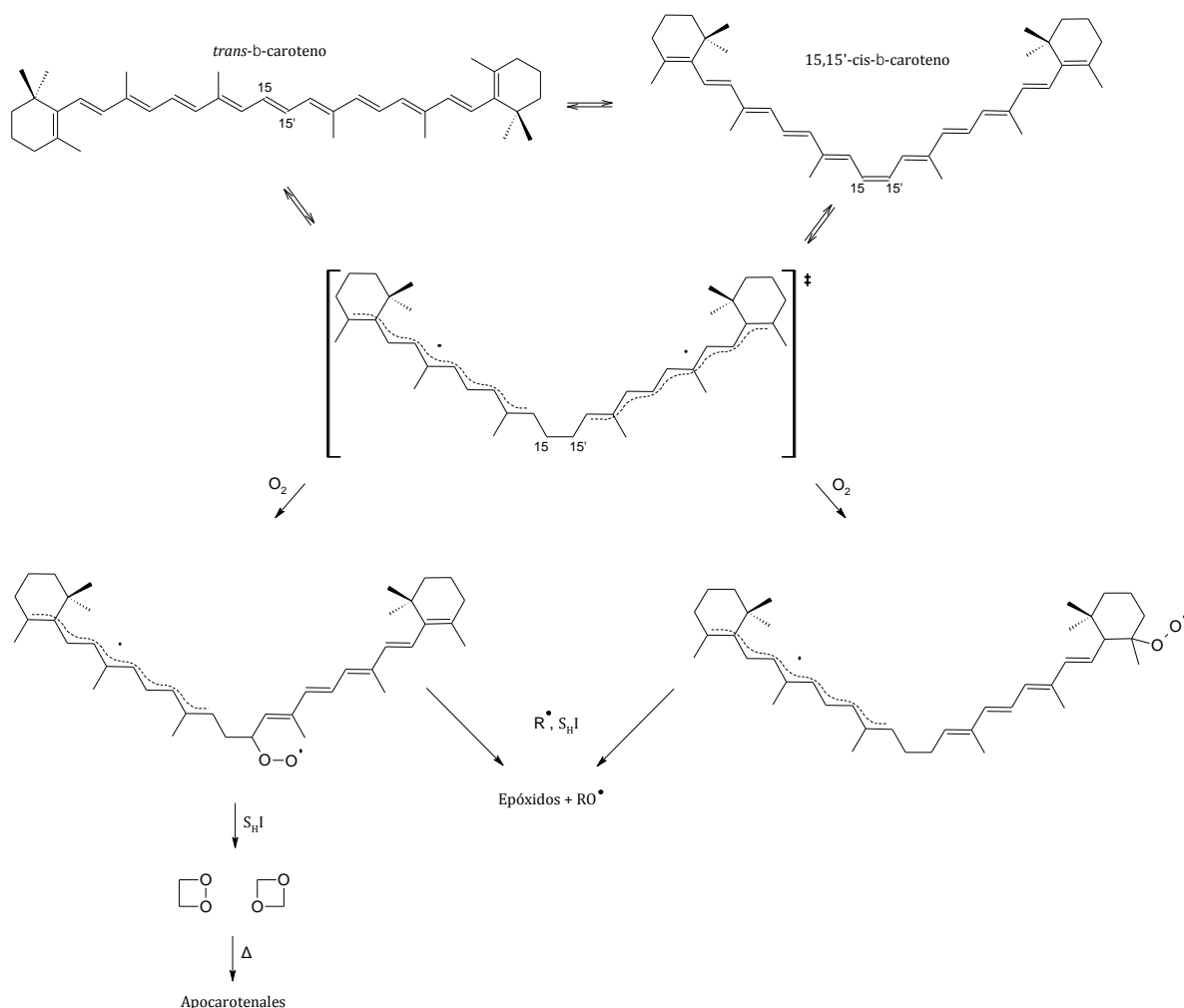


Figura 20 Primeras etapas de la oxidación del  $\beta$ -caroteno, primer etapa isomerización, segunda producción de radicales y luego la aparición de los productos de degradación [71]

Mediante modelado molecular se ha observado que la configuración *trans* del  $\beta$ -caroteno posee la menor energía estructural, mientras que en los isómeros *cis*, la menor energía corresponde al 9-*cis* y 13-*cis*- $\beta$ -caroteno. Esta significativa estabilidad permite explicar porque ambos isómeros *cis* se encuentran en grandes cantidades en alimentos procesados además de dar una idea de la sucesión de aparición de los productos intermedarios. La ruta

por la cual se forman los intermediarios posee dependencia con la temperatura; a baja temperatura los isómeros 13- y 15,15'-*cis*- $\beta$ -caroteno son los predominantes, mientras que el 9-*cis*- $\beta$ -caroteno es formado en condiciones más severas. Por tanto, la proporción de los isómeros formados es dependiente de la temperatura, e inclusive del solvente y el estado (sólido, disuelto, etc.) del  $\beta$ -caroteno. [75] [80]

### 3.2.4 Dependencia con la temperatura

En varios tipos de muestras alimenticias se ha confirmado la variable más importante frente a la degradación, siendo ésta la temperatura. Por tanto, el conocimiento de la dependencia de la temperatura es muy importante en el diseño de los procesos comunes que implique la dupla temperatura-tiempo, como lo es la esterilización, envasado, pasteurizado, desgomado, etc. Dicha dependencia es descrita por la ley de Arrhenius (Ecuación 4), la cual permite calcular la energía de activación. [55] [56] [60] [61] [63] [81] [82] [83] [84]

$$k = Ae^{-\frac{E_a}{RT}} \quad (4)$$

Donde las unidades de  $k$  la constante cinética de reacción y  $A$  el factor pre exponencial de Arrhenius dependen del orden de reacción.  $E_a$  la energía de activación ( $\text{J}\cdot\text{mol}^{-1}$ ),  $R$  la constante ideal de los gases ( $8.314 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ ) y  $T$  la temperatura absoluta (K). [85] [86]

La dependencia con la temperatura también puede ser descrita por el modelo de Bigelow. [87] [88]

$$\log\left(\frac{D_1}{D_2}\right) = \frac{T_2 - T_1}{z} \quad (5)$$

Donde  $D_1$  y  $D_2$  son los tiempos de reducción decimal para las temperaturas  $T_1$  y  $T_2$  respectivamente y  $z$  es la sensibilidad a la temperatura o la constante de resistencia térmica en  $^{\circ}\text{C}$ .

La relación entre los dos modelos anteriores se deduce como sigue.

$$E_a = \frac{\ln(10) T_1 T_2 R}{z} \quad (6)$$

Estudios realizados en la cinética para diversos tipos de sustrato y procesos reflejan una enorme diferencia entre las constantes cinéticas ( $k$ ) o los tiempos de reducción decimal ( $D$ ) atendiendo el tipo de proceso sometido. Cuando el proceso es almacenado  $D$  puede expresarse en meses. Mientras que los procesos térmicos en horas o minutos. Esto refleja la dependencia de la cinética con las temperaturas manejadas durante los procesos. Sin embargo, la temperatura no es el único factor, los datos cinéticos pueden variar para el mismo sustrato y/o el proceso de tratamiento, por ejemplo, el calentamiento convencional posee una

cinética de degradación lenta comparada con el calentamiento con microonda, esto puede asociarse con una *transferencia* térmica más eficiente y como resultado una degradación mayor del  $\beta$ -caroteno (ver tabla 4). [60] [64] [89] [90] [91]

Tabla 4 Datos cinéticos de diversos productos y procesos realizados [60] [64] [89] [90] [91]

| Producto               | Determinación $\beta$ -caroteno         | Proceso                       | Rango de temperatura (°C) | Datos cinéticos                            |                               |   |          |
|------------------------|---|-------------------------------|---------------------------|--|-------------------------------|---|----------|
|                        |   |                               |                           | $k$ (min <sup>-1</sup> )                   | $E_a$ (kJ·mol <sup>-1</sup> ) | $D$ (min)                                       | $z$ (°C) |
| Oleína de Palma        | <i>Trans</i> - $\beta$ -caroteno (HPLC) | Tratamiento térmico           | 120-180                   | -  | 88                            | -   | 34       |
| Puré de papaya         | Carotenoides totales 450 nm             | Tratamiento térmico           | 70-105                    | 0.002-0.006                                | 21                            | 1150  | 104      |
| Jugo de naranja        | <i>Trans</i> - $\beta$ -caroteno (HPLC) | Tratamiento térmico           | 75-100                    | 0.002-0.01                                 | 110                           | 1300-85   | 20       |
|                        |   | Microondas                    | 100-125                   | 0.58-0.78                                  | 14                            | 4-3   | 179      |
| Zanahoria deshidratada | Carotenoides totales 450 nm             | Guardado después de escaldado | 27-57                     | 2.7x10 <sup>-6</sup> -3.6x10 <sup>-5</sup> | 66                            | 8.3x10 <sup>5</sup><br>-<br>6.4x10 <sup>4</sup> | 25       |

El análisis de  $E_a$  y  $z$  muestra una sensibilidad térmica peculiar del  $\beta$ -caroteno frente a la elevación de temperatura (energías de activación arriba de 50 kJ mol<sup>-1</sup> con  $z$  inferior a 34°C). Es deducible que el calor activa casi todas las rutas de degradación del  $\beta$ -caroteno. Lo anterior se debe a la evidencia de la isomerización, térmicamente inducida, al isómero *cis* del  $\beta$ -caroteno y el aumento de oxidación (formación de radicales libres) con el aumento de temperatura.

Se observa la acusada dispersión entre los valores de  $E_a$  y  $z$ , reflejando la dependencia de los valores con los productos y procesos a los cuales se someten estos. De hecho, la degradación del  $\beta$ -caroteno es muy dependiente de la presencia de co-sustratos que pueden encontrarse en diferentes concentraciones en distintas matrices.

Un aspecto importante deducido de los estudios cinéticos es la difícil comparación que puede realizarse entre datos cinéticos a diferentes rangos de temperatura, procesos, sustratos y matrices. Por tanto, los valores de  $E_a$  deben ser tomados con precaución de la literatura. La mayoría han sido calculados de manera empírica y son valiosos para diseñar condiciones de procesado solo para una aplicación concreta. En este sentido, no dan información del mecanismo de degradación y por tanto no puede realizarse una *transposición* para otros productos o procesos. [60] [65] [89] [91]

### 3.2.5 Factores asociados a la cinética de degradación

Previamente se ha reconocido la importancia de la temperatura como factor predominante. Sin embargo, se analizarán otros factores asociados a la cinética de degradación del  $\beta$ -caroteno. Factores involucrados en la extracción de la materia prima, matriz, procesado, refinado y almacenado.

### 3.2.5.1 Efecto del oxígeno

La actividad antioxidante del  $\beta$ -caroteno consiste ya sea en extinción física del oxígeno singlete o el secuestro de las especies reactivas de oxígeno. Esta actividad antioxidante forma parte de las degradaciones que el  $\beta$ -caroteno puede sufrir; la presencia de oxígeno puede estar correlacionada con la cinética de degradación del  $\beta$ -caroteno. El efecto del oxígeno ha sido estudiado con mayor amplitud desde un punto de vista mecanístico; mostrando una dependencia de la presión parcial del oxígeno en el sistema sobre la autoxidación del  $\beta$ -caroteno, implicando que el oxígeno es el factor más importante en la degradación en sistemas lipídicos; siendo el radical peroxilo quien se une al  $\beta$ -caroteno para formar radicales estables que dan lugar a los productos de escisión del  $\beta$ -caroteno. [92] [93] [94] [95] [96] [97]

La mayoría de estudios en productos alimenticios consisten en la comparación de la degradación (o retención) del nivel de carotenoides cuando son sometidos a diferentes niveles de oxígeno. Por ejemplo, altas concentraciones de oxígeno están asociadas con altos niveles de degradación de carotenoides durante almacenamiento. Un problema del estudio de la influencia del oxígeno implica la diferenciación entre la presión parcial del oxígeno alrededor de la muestra y el oxígeno disuelto que está presente en la muestra durante el estudio; se han realizado estudios considerando el oxígeno disuelto en la muestra, evidenciando adicionalmente la necesidad de un modelo que incluya la *transferencia* de oxígeno atmosférico hacia la matriz (aceite). Por tanto, en el modelo cinético fue incluida la *transferencia* interna de oxígeno en el mecanismo (empleando n-decano como solvente); dicho mecanismo considera la degradación como una reacción en cadena (iniciación, propagación y terminación). Se parte de dos etapas de iniciación, seguidas de dos de propagación y finalmente dos de terminación tal como describe la figura 21. [63] [92] [93] [97] [98]

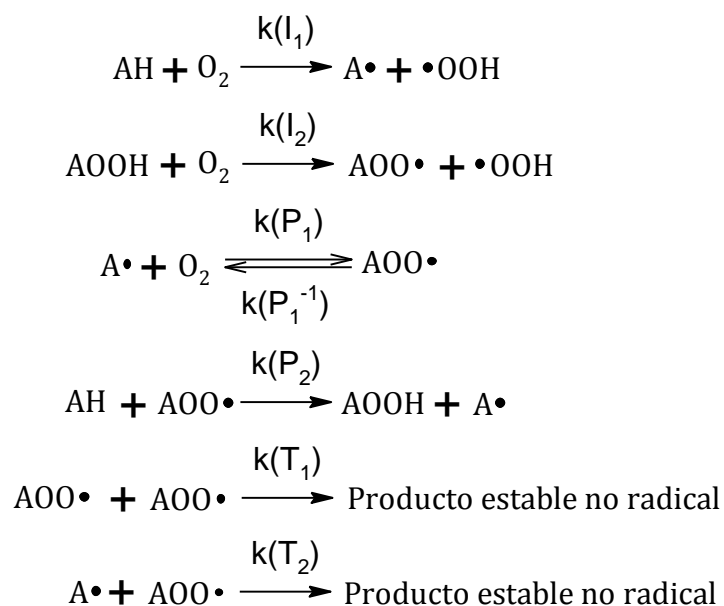


Figura 21 Mecanismo propuesto que incluye la concentración de oxígeno disuelto en el modelo. [98]

Donde:

$$[AH] = [\beta - \text{Caroteno}]$$

$$[O_2] = [\text{Oxígeno disuelto}]$$

$$[A \bullet] = [\text{Radical } \beta - \text{Caroteno}]$$

$$[\bullet OOH] = [\text{Hidroperóxido}]$$

$$[AOOH] = [\text{Hidroperóxido del } \beta - \text{Caroteno}]$$

$$[AOO \bullet] = [\text{Radical peróxido del } \beta - \text{Caroteno}]$$

Dicho modelo genera la siguiente ecuación cinética del consumo de  $\beta$ -caroteno en función del tiempo y concentración de las especies (incluido el oxígeno disuelto) en un pseudo estado estacionario [98]:

$$-\frac{dC_{AH}}{dt} = k_{I1}C_{AH}C_{O_2} + k_{P2}(2k_{T1})^{-\frac{1}{2}} \left(1 + \frac{k_{T2}k_{P1}^{-1}}{k_{T1}k_{P1}C_{O_2}}\right)^{-\frac{1}{2}} C_{AH}(k_{I1}C_{AH}C_{O_2} + k_{I2}C_{AOOH}C_{O_2})^{\frac{1}{2}} \quad (7)$$

Donde  $C_{AH}$  es la concentración residual del  $\beta$ -caroteno,  $C_{O_2}$  la concentración de oxígeno (disuelto),  $C_{AOOH}$  la concentración del hidroperóxido del  $\beta$ -caroteno y las constantes cinéticas asociadas al mecanismo descrito en la figura 21. [98]

Dicho modelo fue probado experimentalmente, obteniéndose el valor de todas las constantes cinéticas, mostrando buena correlación entre el valor predicho versus el obtenido al verificarse en un rango de 50-60 °C y una concentración de oxígeno disuelto entre 1.02-11.10 x 10<sup>-3</sup> mol/dm<sup>3</sup>. [98]

Empleando ácido oleico como solvente, se describe un modelo cinético que incluye 7 reacciones de oxidación del  $\beta$ -caroteno, 2 de oxidación del ácido oleico y 1 reacción entre el  $\beta$ -caroteno y el ácido oleico. Mostrando no solo la importancia del oxígeno en la degradación, también el efecto matriz, que en la gran mayoría de productos alimenticios es sumamente compleja y variable. [99]

Sin embargo, los modelos anteriores son de difícil aplicación en matrices complejas, donde la medición del oxígeno disuelto resulta impráctica (productos sólidos, como el fruto de palma) o la presencia de componentes oxidables que puedan interferir la medición. Considerando, adicionalmente, la disminución del oxígeno disuelto con la temperatura al mismo tiempo que los productos líquidos acuosos poseen una menor cantidad de oxígeno disuelto comparados con los oleosos. En los productos sólidos, la transferencia del oxígeno está muy limitada por los bajos coeficientes de difusión del oxígeno atmosférico hacia los alimentos; dichos coeficientes son difíciles de obtener experimentalmente y por tanto, el estudio del oxígeno disuelto es complicado en muestras alimenticias, siendo el factor limitante en los estudios cinéticos sobre la degradación del  $\beta$ -caroteno. [100] [101]

### 3.2.5.2 Efecto de la matriz

A causa de la diversidad de productos alimenticios (frutas, vegetales o derivados de éstas) y la complejidad de su composición, el efecto de la matriz en la degradación del  $\beta$ -caroteno es muy difícil de entender. Dos factores pueden ser identificados como los más generales: la **composición** en sí misma y la **estructura** en la cual se encuentra el  $\beta$ -caroteno en el sustrato; el cual es dependiente del tipo y estructura del producto: líquido, sólido, emulsión, etc. [62]

#### 3.2.5.2.1 Efecto de la composición alimenticia

La composición es muy diferente entre los diferentes vegetales y frutas atendiendo a los distintos géneros, especies y variedades. Incluso en la misma variedad pueden ocurrir variaciones en la composición por factores climáticos. Inclusive, en algunos casos, la composición puede diferir en función de las distintas partes. Lo anterior justifica la dificultad del modelado cinético en productos reales y los intentos de elucidar los parámetros cinéticos a través de modelaje. [62]

##### 3.2.5.2.1.1 Agua

Se ha encontrado evidencia que, a menor actividad del agua, la degradación del  $\beta$ -caroteno es más rápida. Obteniéndose un modelo de primer pseudo orden. Sin embargo el modelo es específico para la matriz estudiada, lo que implica cero *transposición* de resultados al estudiar otra muestra o matriz. [63] [102]

##### 3.2.5.2.1.2 Ácido

El efecto ácido en la degradación de carotenoides ha sido reportado en algunos estudios, como por ejemplo en el estudio de nano emulsiones de  $\beta$ -caroteno, fue concluido que la velocidad de degradación fue mayor en pH ácido. Adicionalmente un estudio en emulsiones de tipo O/W demostró que la degradación aumentaba drásticamente desde un pH 4 hacia abajo. El mecanismo descrito para la degradación en presencia ácida sugiere un primer paso de protonación del  $\beta$ -caroteno, seguido por una isomerización *cis-trans*; sin embargo, sugiere que la ruta no procede vía radicales libres, al contrario, mediante intermediarios iónicos, siendo los productos probables ésteres de los carotenoides. [81] [103] [104]

Sin embargo, otros estudios afirman que el pH ácido solo representa un efecto menor sobre la isomerización del  $\beta$ -caroteno en solventes o alimentos. [105] [106]

De manera general, el efecto del pH sobre el  $\beta$ -caroteno debe ser atribuido al tiempo de exposición al ácido, concentración del ácido, sustrato y matriz sobre la cual se realiza el



estudio. Reafirmando así la especificidad de los resultados cinéticos y la dificultad de generalizarlos.

#### 3.2.5.2.1.3 Insaturación de los lípidos

El efecto de los lípidos saturados e insaturados sobre la degradación del  $\beta$ -caroteno sigue sin esclarecerse. Se ha evidenciado que los carotenoides pueden reaccionar con los productos oxidativos de los lípidos, pero no se ha encontrado ninguna diferencia en la degradación de los carotenoides en diferentes sustratos de ácidos grasos. Se determinó una velocidad mayor de degradación en presencia de ácidos grasos saturados comparado a los insaturados; argumentando que los ácidos insaturados entran en competición con el  $\beta$ -caroteno frente a la reacción del oxígeno. Contrariamente, otros estudios, determinaron una mayor velocidad de degradación a medida el grado de insaturación del aceite aumentaba; fue considerado que los ácidos insaturados fueron oxidados más rápidamente comparado a los saturados, generando así radicales que podrían atacar con facilidad los carotenoides. [97] [107] [108] [109]

Por el momento la influencia de la insaturación de los lípidos sobre la degradación del  $\beta$ -caroteno permanece incierta.

#### 3.2.5.2.1.4 Antioxidantes

Diversos estudios reportan interacciones de los carotenoides con otros antioxidantes, en particular con vitamina E y C. Vitamina E es el nombre genérico que abarca ocho tococromanoles (cuatro tocoferoles y cuatro trienoles). Dichos compuestos son lipofílicos y pueden encontrarse en aceites que contienen  $\beta$ -caroteno como el aceite de palma. Estas moléculas han demostrado una mejor acción de ruptura de cadena que el  $\beta$ -caroteno en reacciones de peroxidación inducida por radicales libres. Lo anterior aunado al efecto protector reportado en modelos lipídicos purificados. Otros estudios han demostrado un efecto sinérgico entre carotenoides y tococromanoles en sus efectos protectivos; de igual manera el ácido ascórbico ha mostrado sinergia con el  $\beta$ -caroteno en la prevención de oxidación y degradación de éste último, aunque únicamente mediante estructuras anfifílicas por su diferente polaridad y correspondiente solubilidad. [21] [32] [37] [110] [111] [112] [113]

Se ha desarrollado un modelo cinético que involucra el  $\alpha$ -tocoferol; cinéticamente juega el papel de inhibidor. El modelo consta de 19 pasos elementales y fue comprobado a distintas temperaturas y concentraciones iniciales, con el agregado de incluir el oxígeno disuelto en el medio. [114]

### 3.2.5.2.1.5 Metales

Al contrario que los antioxidantes, los metales poseen un rol oxidante, se ha establecido que el  $\beta$ -caroteno ofrece poca protección ante la peroxidación de los lípidos inducida por metales, en particular el efecto es aumentado en pH bajo. [103] [115]

### 3.2.5.2.1.6 Efecto de la luz

De igual manera que la temperatura, la luz favorece la isomerización del  $\beta$ -caroteno, pero en menor proporción a ésta. Una comparación entre el efecto isomérico de la temperatura y la luz sobre el  $\beta$ -caroteno, describió un aumento de la constante cinética de 24 veces a 150°C comparado a un efecto prácticamente despreciable a -5°C y 2000 lx. Mientras que un estudio durante 21 días no encontró un efecto importante de la luz sobre el  $\beta$ -caroteno. [61] [70] [116]

En conclusión, la luz favorece la isomerización del  $\beta$ -caroteno, pero su efecto palidece comparado al de la temperatura. Por tanto, si el sistema permanece a temperatura constante (común durante el almacenamiento controlado), el efecto de la luz es de importancia a considerar; por otra parte, si el sistema será sometido a cambios de temperatura el efecto de la luz es despreciable comparado a la degradación térmica.

### 3.2.5.2.2 Efecto de la estructura

Durante el procesado (cortado, triturado, prensado, etc.) los micronutrientes son degradados primeramente por la ruptura en los tejidos; un ambiente oxidativo promueve las reacciones como resultado del contacto con el aire de igual manera la desorganización de la estructura celular y solubilización promueve reacción de degradación. [6] [31]

Estudios en plantas han revelado la ubicación de los carotenoides en los cromoplastos; inclusive dentro del cromoplasto los carotenoides pueden encontrarse en forma cristalina o parcialmente solubilizados en microgotas lipídicas en función del tipo de vegetal. En vegetales que contienen el  $\beta$ -caroteno preferentemente solubilizado muestran una mayor proporción del isómero *cis*- $\beta$ -caroteno de manera natural; contrariamente los vegetales que contienen el  $\beta$ -caroteno en forma cristalina mayoritariamente el isómero *trans*- $\beta$ -caroteno predomina. En un estudio se observó un aumento del isómero 13-*cis*- $\beta$ -caroteno al adicionar jugo de uva al jugo de zanahoria; lo anterior es atribuido a la disolución parcial del caroteno cristalino presente en la zanahoria, indicando que la solubilización de los carotenos es un prerrequisito para la formación de los isómeros *cis*. La reacción inversa, la isomerización de *cis* a *trans* ocurre en  $\beta$ -caroteno parcialmente fundido. Adicionalmente se encontró una correlación entre el solvente y el grado de isomerización, siendo mayor en solventes no polares. [61] [75] [77] [117] [118] [119] [120]

El efecto protector de la estructura vegetal sobre el  $\beta$ -caroteno ha sido estudiado mostrando el  $\beta$ -caroteno con mayor sensibilidad a la isomerización que el licopeno, debido a la deformación o cambios en la ultraestructura celular de la pared celular de los organelos inducida por el tratamiento térmico, mientras que los dos grupos voluminosos de los anillos  $\beta$ -ionona, presentes en el  $\beta$ -caroteno difícilmente puede reorganizarse cómo lo haría el licopeno frente a estos cambios estructurales. Como resultado se observó un aumento en el isómero *cis*- $\beta$ -caroteno mientras que la relación de isómeros *cis* y *trans* del licopeno permanecieron constantes. Los estudios anteriores muestran la crucial importancia de la estructura donde los carotenoides permanecen y el estado físico sobre la estabilidad de todas las configuraciones *trans*. [121] [122]

## 4 Metodología experimental

### 4.1 Muestra

El aceite crudo de palma a utilizar como muestra es comercializado en el país por Hondupalma. Dicho aceite es obtenido por extracción mecánica del mesocarpio del fruto de palma africana y comercializada a la planta aceitera Summa Industrial S.A. de C.V. [123] [124]

El muestreo se hizo en un tanque de almacenamiento en la planta industrial, fue proporcionado todo el aceite requerido. Se tomó 1L de aceite por cada viaje hecho hasta Lourdes Colón, Municipio donde están las instalaciones de Summa.

La muestra se almacenó y transportó en un recipiente ámbar de vidrio a 4-6°C sin exposición directa a la luz solar.

Previo a su uso, el aceite fue filtrado a vacío en papel filtro número 40 para eliminar los residuos del proceso de extracción y obtener una muestra más homogénea.

### 4.2 Elección del método

Con el fin de desarrollar la metodología experimental, se compararon los resultados mediante HPLC (Shimadzu) con detector UV-Vis con un espectrofotómetro UV-Vis (Shimadzu 1700).

Tal como se expuso en la sección 3.2.2, ambas técnicas presentan sus ventajas y desventajas para los estudios cinéticos, sin embargo, se contrastaron ambas técnicas, siendo la escogida el espectrofotómetro UV-Vis, ya que, a las condiciones estudiadas el cromatógrafo no presentó la resolución requerida para diferenciar entre el  $\beta$ -caroteno, demás carotenoides y productos de degradación (ver gráfico 4). Por tanto, al tener una separación insatisfactoria se optó por el método espectroscópico en aras de menor uso de solvente, menor tiempo de preparación de muestra y menor tiempo de respuesta.

Se empleó 450 nm de longitud de onda para el seguimiento de los carotenoides según referencias de estudios previos. [125] [126] [127] [128] [129] [130] [131] [132] [133] [134] [135] [136]

### 4.3 Curva de calibración HPLC

Para construir la curva de calibración se hicieron disoluciones de una muestra estándar, considerando este paso como análisis preliminar. El objetivo es elegir la técnica de análisis más eficiente para el desarrollo de esta investigación. A través de una función matemática que relaciona concentración vs absorbancia (variable independiente) se cuantificarán los carotenoides en la muestra real de aceite de palma (muestra problema).

Empleando estándar de  $\beta$ -caroteno (95% pureza), se realizaron disoluciones de 10 a 20 ppm (por triplicado) en la mezcla de elución (40% acetonitrilo-60% isopropanol en volumen), previamente sonicadas y microfiltradas. Se empleó una elución isocrática a 1.0 mL/min.

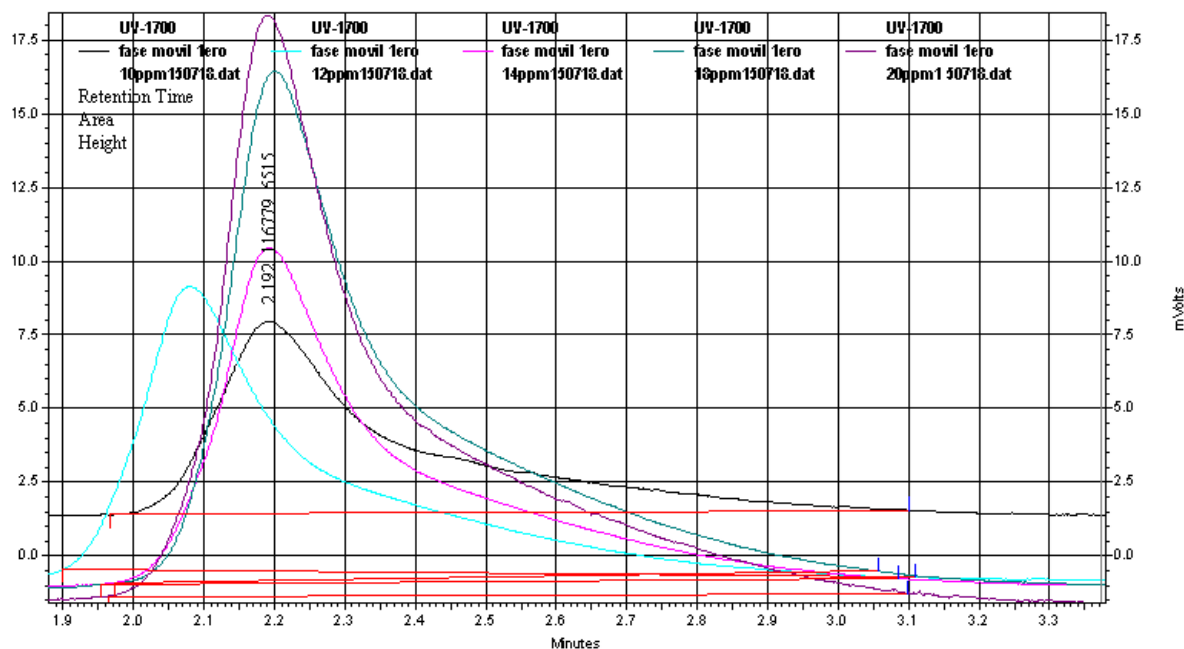


Gráfico 1 Cromatograma de la curva de calibración 10-20 ppm de estándar de  $\beta$ -caroteno. La curva negra solución de 10ppm, la curva aqua solución de 12ppm, la curva fucsia solución 14ppm, la curva azul solución 18ppm y la curva morada solución de 20ppm.

Se realizaron las mediciones de cada disolución por triplicado en más de una ocasión hasta obtener el rango de concentraciones adecuadas, es decir, las concentraciones que permitían la lectura de la señal emitida. Se inició con una concentración de 2 ppm sin embargo no

detectaba señal por lo tanto se modificó la concentración hasta optimizar la metodología. Se concluyó que los mejores resultados eran el juego de soluciones desde los 10ppm hasta los 20ppm, con lo que se procedió a graficar la curva de calibración (absorbancia vs la concentración). El resultado fue un dato de  $R^2$  aceptable, se presenta a continuación en el Gráfico 2.

La curva de calibración nos servirá para determinar la muestra desconocida. Se construye a partir de las disoluciones del estándar de  $\beta$ -caroteno (10ppm-20ppm) y a partir de la señal analítica emitida por el detector del HPLC.

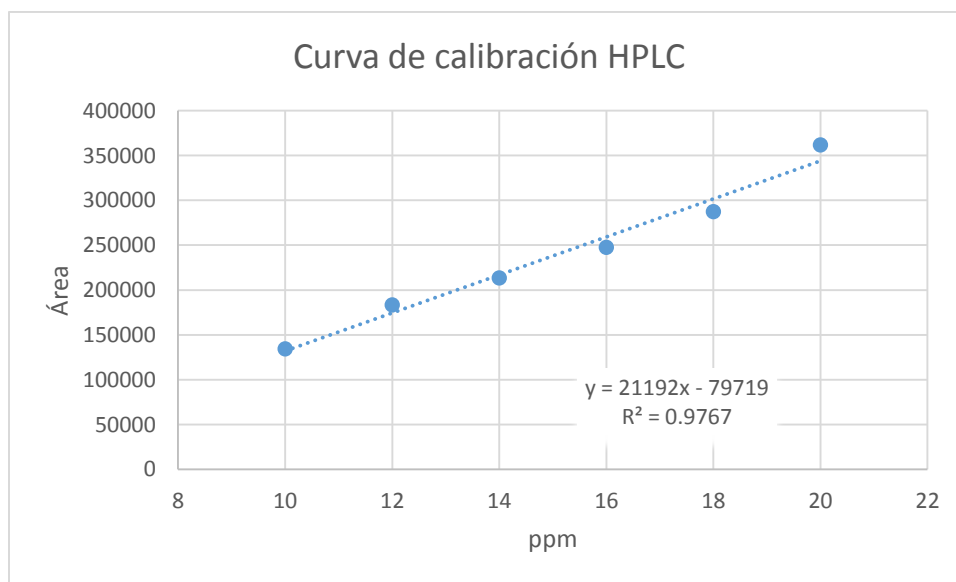


Gráfico 2 Curva de calibración HPLC con detector UV-Vis a 450 nm.

#### 4.4 Curva de calibración UV-Vis

De igual manera se realizó la curva de calibración empleando las mismas soluciones y por triplicado con el espectrofotómetro UV-Vis a 450 nm. Sin embargo, la curva se extendió hasta una concentración de 40 ppm por las absorbancias observadas durante los ensayos preliminares. (Ver Gráfico 4 en sección 5.2)

#### 4.5 Resolución HPLC

Para evaluar la resolución del HPLC se preparó una muestra cinética según el siguiente procedimiento.

- a) Se filtró el aceite de palma crudo con papel filtro número 40 para eliminar residuos del prensado.
- b) Se calentó una muestra de aceite de palma crudo en un Erlenmeyer de 25 ml a 90°C empleando un Hot Plate durante 6 horas a presión ambiente. Esto se hizo utilizando un baño de María para asegurarse que calentara toda la muestra de aceite.
- c) Se tomó una muestra del aceite calentado del procedimiento anterior, se diluyó en un factor (157,5 veces) que permitiera que la concentración de la muestra fuera cercana a 20 ppm empleando la mezcla de fase móvil como solvente de dilución.
- d) Esta disolución fue filtrada (microfiltro), sonicada por 30 minutos e inyectada en el HPLC.
- e) Se varió la velocidad de elución en cada inyección de disolución, desde los 0.10 ml/min hasta los 2 ml/min.

El paso b) fue realizado a la máxima temperatura que puede manipularse y el tiempo máximo disponible para trabajar en el laboratorio en una sesión. Esto con el objetivo de obtener la máxima concentración posible de productos de degradación. Empleando 450 nm como longitud de onda en ambos detectores, se estableció la concentración de carotenoides para la construcción de la curva de calibración, con ella se estimó una concentración de carotenoides en el aceite de palma crudo aproximadamente a 3150 ppm. Con este dato se realizó la dilución en la mezcla de elución respectiva. Luego del estudio de la disolución, no se observó la aparición de nuevas señales.

**La concentración de Betacaroteno en la muestra se determinó de la siguiente manera:**

Se pesó en un balón de 25 ml una alícuota de 335µL de aceite de palma crudo filtrado, se aforó hasta la marca con el solvente isopropanol-acetonitrilo mezcla 60:40. Luego de homogenizar se determinó la absorbancia según la siguiente tabla:

*Tabla 5 Masa de aceite de palma crudo y su absorbancia*

| Masa (g) | Absorbancia |
|----------|-------------|
| 0.252    | 1.471       |
| 0.251    | 1.476       |
| 0.250    | 1.472       |
| 0.251    | 1.472       |
| 0.251    | 1.473       |
| PROMEDIO | 0.251       |
|          | 1.472       |

Empleando la curva de calibración se convierte la absorbancia promedio en la concentración promedio de la disolución resultante. Siendo 31.63 mg/L

Por tanto, la concentración de Betacaroteno en el aceite se calcula:

$$\frac{31.63 \text{ mg}}{\text{L}} * 25 \text{ mL} * \frac{1 \text{ L}}{1000 \text{ mL}} * \frac{1}{0.251 \text{ g}} * \frac{1000 \text{ g}}{1 \text{ kg}} = 3150 \text{ ppm}$$

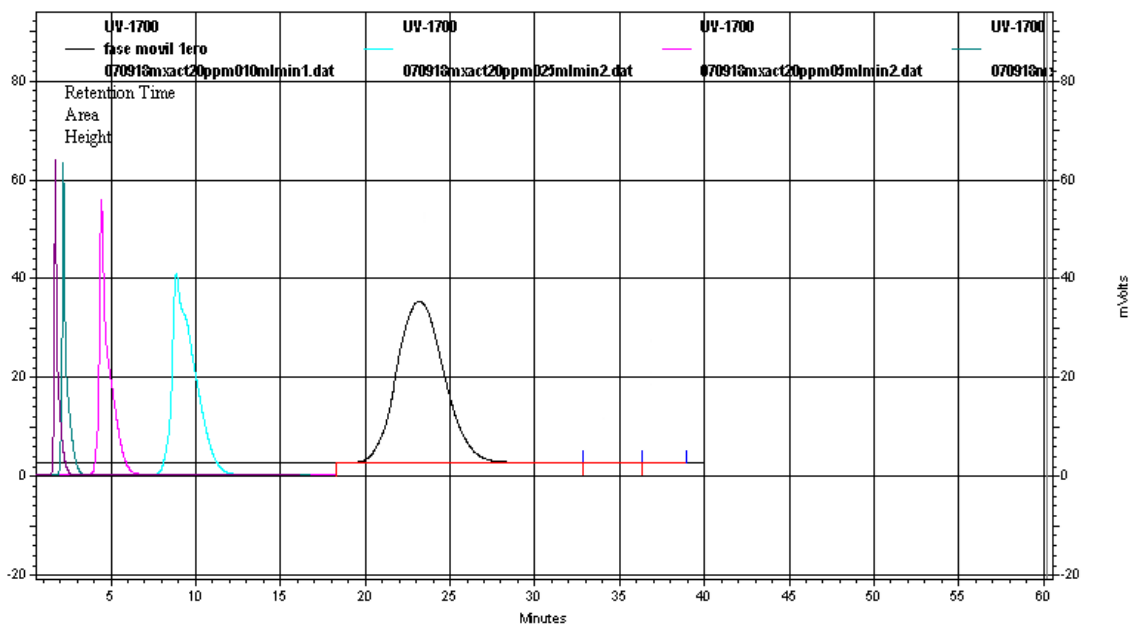


Gráfico 3 Cromatogramas a distintas velocidades de elución de la muestra de aceite de palma crudo calentado a 90° durante 6 horas.

Las señales que se observan superpuestas en el gráfico 3 corresponden a lecturas de una muestra de solución estándar a una concentración de 20ppm la cual se eluyó a diferentes velocidades. En el gráfico se presenta la curva negra que corresponde a la primera velocidad 0.1 ml/min, la curva azul 0.25 ml/min, la curva morada 0.5 ml/min, la curva azul 1 ml/min y la curva morada de 1.25 ml/min. Lo que se busca es verificar si con este cambio se podían observar otras señales en los Cromatogramas, es decir, si el HPLC nos permitiría separar el  $\beta$ -Caroteno de los productos de degradación u otras especies similares, sin embargo se logró concluir que no hay mayor beneficio en usar este equipo sobre utilizar el Espectrofotómetro UV/VIS.

Con el uso del HPLC se requiere solventes de alta pureza y un mayor tratamiento de la muestra, al usar el Espectrofotómetro UV/VIS disminuye el tiempo de preparación de muestras, el uso del equipo es más práctico y más accesible ante la realidad de un país como el nuestro. El HPLC permite analizar muestras complejas como una matriz de aceite de palma que contiene más de un componente además del analito pero a pesar que esta ventaja fue el principal motivo para usarlo en este estudio, al realizar los ensayos preliminares no se observó otro componente que absorbiera a 450 nm y por tanto con esta premisa se decidió emplear al Espectrofotómetro UV/VIS ya que no habría otro elemento en la muestra que nos represente algún error en las lecturas con este equipo.

## 4.6 Diseño experimental para el estudio de la cinética:

### PRIMERA PARTE: TRATAMIENTO DE MUESTRA

- i. Se filtró la muestra de aceite de palma crudo con papel filtro 40 mediante vacío.
- ii. Se procedió a guardar el aceite filtrado en un frasco de vidrio ámbar y se almacenó alejado de la luz hasta su posterior uso, en refrigeración.



Figura 22 Filtrado de aceite de palma crudo

### SEGUNDA PARTE: ORDEN DE REACCIÓN.

En el laboratorio de la escuela de química no se dispone de un termostato, la temperatura se controló utilizando un volumen relativamente grande de agua calentada para estabilizar los cambios en la distribución de calor.

- i. Se armó un sistema para calentar la muestra:  
Llenando con agua del grifo un beaker de 1L, aproximadamente hasta los 800 ml. Y usando un Hot Plate se calentó el agua hasta una temperatura estable de 42°C.  
Se colocó con la ayuda de un soporte un Erlenmeyer de 25 ml en el baño de agua, tal como muestra el esquema siguiente:

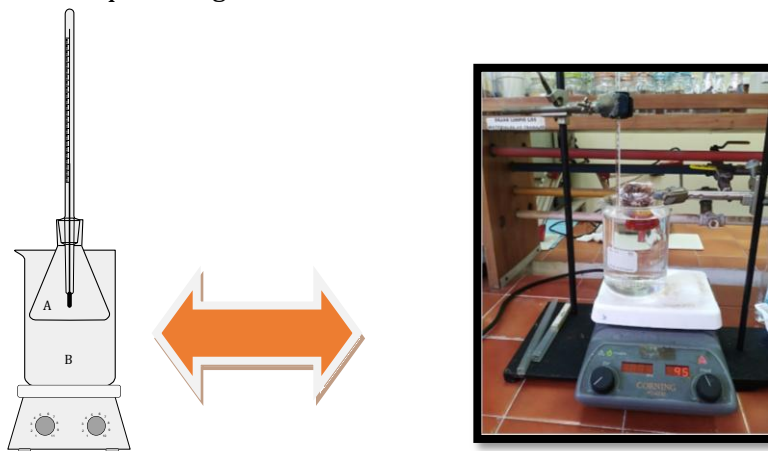
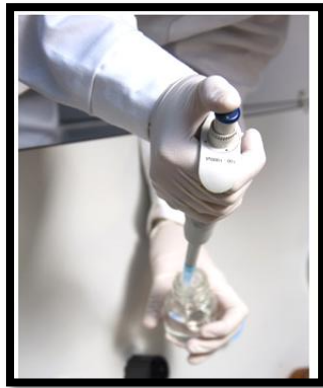


Figura 23 Montaje experimental propuesto.



- ii. Una vez la temperatura se estabilizó en 42°C se agregaron 6 mL del aceite filtrado en el Erlenmeyer de 25 ml y se inició la cuenta en el cronometro.
- iii. La primera alícuota se tomó en el tiempo 0 ( $T_0$ ), para ello se procedió de la siguiente manera:
  - a. Con una micropipeta se tomó una pequeña porción del aceite.
  - b. Dentro de un balón volumétrico de 25 ml se agregó la muestra tomada con la micropipeta hasta que se pesó aproximadamente 0.25g del aceite del Erlenmeyer en el baño de maría, el remanente en la micropipeta se devolvió.
  - c. Se aforó con el solvente isopropanol-acetonitrilo mezcla 60:40. Se homogenizó y se procedió a su lectura en el Espectrofotómetro UV/VIS
- iv. Se tomaron alícuotas cada dos horas en un lapso de 6 horas ( $T_2$ ,  $T_4$  y  $T_6$ ) y se hicieron sus mediciones en el espectrofotómetro.



*Figura 24 Lecturas en Espectrofotómetro*

- v. Utilizando la curva de calibración (Gráfico 4) se convirtieron las absorbancias en concentraciones. Obteniéndose así la gráfica de concentración de  $\beta$ -caroteno vs Tiempo.
- vi. El orden de reacción se determinó aplicando los modelos integrados a la curva de concentración vs tiempo.

### TERCERA PARTE: ENERGIA DE ACTIVACIÓN.

- i. Se repitieron los pasos del i. al vi. de la segunda parte con las temperaturas 60, 80 y 90°C.
- ii. Con las constantes obtenidas a diferentes temperaturas se aplicó el Modelo de Arrhenius para obtener la energía de activación respectiva a la degradación cinética estudiada.

## CUARTA PARTE: TIEMPO DE REDUCCIÓN DECIMAL, TIEMPO DE VIDA MEDIA Y FACTOR Z.

El tiempo de reducción decimal lo que indicará es el tiempo que tardó en degradarse el  $\beta$ -caroteno desde el 100% hasta un 90% de su concentración inicial. Mientras que el tiempo de vida media implica el tiempo que tardó en degradarse hasta un 50%.

- i. Una vez conocidas las constantes cinéticas a las diferentes temperaturas se procedió a calcular el tiempo de reducción decimal y el factor z según las ecuaciones (3) y (5).
- ii. El tiempo de vida media se calculó utilizando la Ecuación (3) modificada.

### 4.7 Conclusiones de los ensayos preliminares

- i. El contenido de carotenoides, medidos a 450 nm, en el aceite de palma crudo empleado es aproximadamente 3150 ppm, valor que sobrepasa los valores registrados en literatura, sin embargo, como se mencionó en la sección 3.1.2.2.1 la carga de carotenoides no es un estándar y depende de muchos factores de cosecha, procesado y transporte. Por tanto, no es un dato alarmante o que pueda afectar el estudio cinético.
- ii. El uso del HPLC no ofrece la ventaja de resolución en la separación del  $\beta$ -caroteno de la matriz en las condiciones estudiadas sobre el uso del espectrofotómetro UV-Vis.
- iii. Las limitaciones de equipo obligan emplear un baño agua relativamente grande para aminorar las fluctuaciones de temperatura. Unos 800 mL de agua por 6 mL de aceite son sugeridos, ver *figura 23*.

## 5 Análisis y discusión de resultados

### 5.1 Curva de calibración

Se midió la absorbancia de una serie de disoluciones desde 8 hasta 40 ppm del estándar de  $\beta$ -caroteno disuelto en mezcla 60:40 isopropanol/acetonitrilo.

Tabla 6 Curva de calibración del estándar  $\beta$ -caroteno en UV-Vis

| ppm | abs1  | abs2  | abs3  | abs(promedio) |
|-----|-------|-------|-------|---------------|
| 8   | 0.372 | 0.305 | 0.316 | 0.331         |
| 10  | 0.486 | 0.389 | 0.398 | 0.424         |
| 12  | 0.520 | 0.432 | 0.443 | 0.465         |
| 14  | 0.632 | 0.537 | 0.507 | 0.558         |
| 16  | 0.690 | 0.602 | 0.584 | 0.625         |
| 18  | 0.832 | 0.711 | 0.731 | 0.758         |
| 20  | 0.855 | 0.784 | 0.790 | 0.809         |
| 22  | 1.068 | 0.888 | 0.927 | 0.961         |
| 24  | 1.165 | 1.148 | 1.108 | 1.140         |
| 26  | 1.284 | 1.257 | 1.263 | 1.268         |
| 28  | 1.362 | 1.384 | 1.366 | 1.370         |
| 30  | 1.449 | 1.457 | 1.432 | 1.446         |
| 34  | 1.596 | 1.631 | 1.612 | 1.613         |
| 38  | 1.754 | 1.783 | 1.719 | 1.752         |
| 40  | 1.851 | 1.842 | 1.798 | 1.830         |

Obteniéndose de la relación A vs C un coeficiente de correlación lineal y los parámetros de la ecuación:

Tabla 7 Parámetros de regresión lineal de A vs C de la curva de calibración del estándar de  $\beta$ -caroteno en UV-Vis

| Coeficiente de correlación (r) | Parámetros ecuación: $A = mC + b$ |         |
|--------------------------------|-----------------------------------|---------|
|                                | m                                 | b       |
| 0.9942                         | 0.0501                            | -0.1119 |

Siendo la gráfica de dispersión la siguiente:

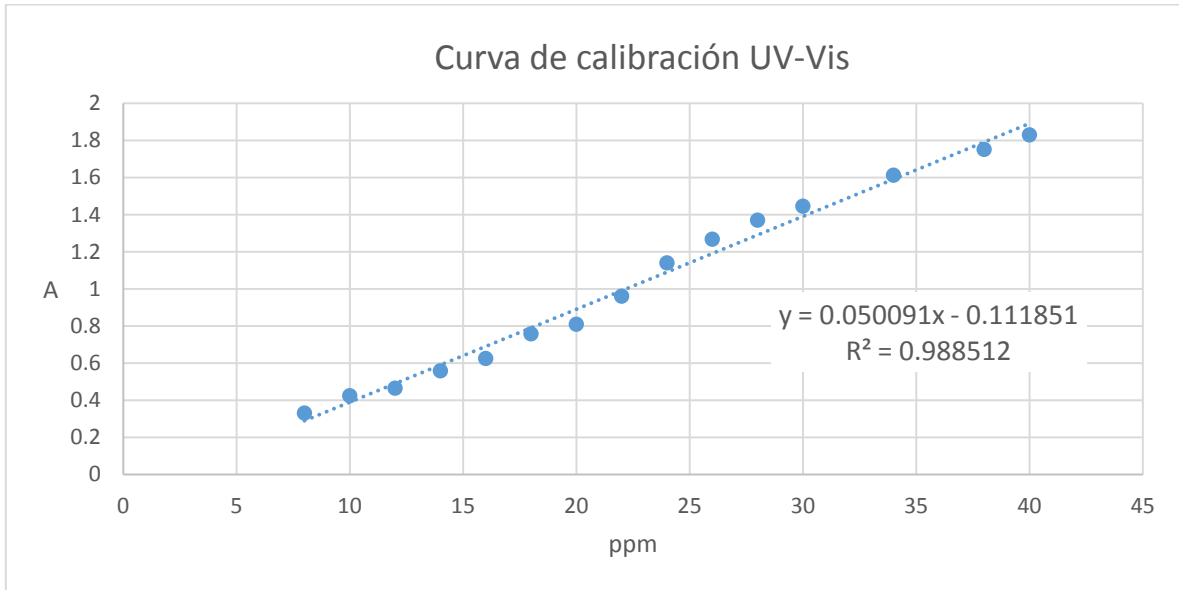


Gráfico 4 Curva de calibración en UV-Vis

Esto permite obtener la siguiente ecuación que se utilizará para calcular la concentración a partir de la absorbancia durante el estudio cinético:

$$C = \frac{A - b}{m} \quad (8)$$

## 5.2 Estudio cinético

El estudio de la concentración de  $\beta$ -caroteno en función del tiempo se realizó midiendo la absorbancia a los tiempos 0, 6, 24, 30, 48, 54, 72 y 78 horas respectivamente. Cada experimento se realizó por triplicado a cada temperatura.

### 5.2.1 42°C

A la temperatura de trabajo de 42°C se obtuvieron los siguientes resultados:

Tabla 8 A vs t de la degradación de  $\beta$ -caroteno a 42°C

| A1    | A2    | A3    | A prom | t (h) | t (s)  |
|-------|-------|-------|--------|-------|--------|
| 1.557 | 1.549 | 1.554 | 1.553  | 0     | 0      |
| 1.541 | 1.556 | 1.554 | 1.550  | 6     | 21600  |
| 1.549 | 1.546 | 1.550 | 1.548  | 24    | 86400  |
| 1.532 | 1.541 | 1.557 | 1.543  | 30    | 108000 |
| 1.535 | 1.534 | 1.539 | 1.536  | 48    | 172800 |
| 1.528 | 1.530 | 1.532 | 1.530  | 54    | 194400 |
| 1.500 | 1.546 | 1.521 | 1.522  | 72    | 259200 |
| 1.533 | 1.500 | 1.525 | 1.519  | 78    | 280800 |

Siendo el gráfico de dispersión de A promedio vs tiempo en segundos:

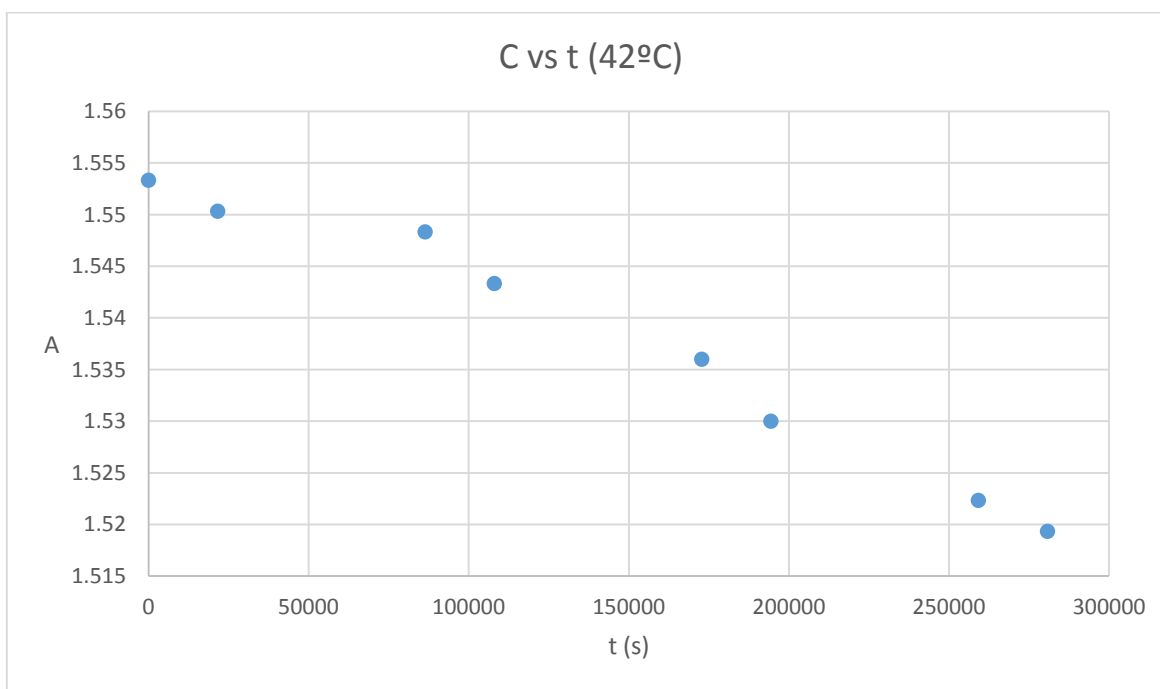


Gráfico 5 Estudio cinético de A vs t para 42°C

## 5.2.2 60°C

A la temperatura de trabajo de 60°C se obtuvieron los siguientes resultados:

Tabla 9 A vs t de la degradación de  $\beta$ -caroteno a 60°C

| A1    | A2    | A3    | A prom | t (h) | t (s)  |
|-------|-------|-------|--------|-------|--------|
| 1.456 | 1.452 | 1.455 | 1.454  | 0     | 0      |
| 1.431 | 1.439 | 1.440 | 1.436  | 6     | 21600  |
| 1.402 | 1.400 | 1.400 | 1.400  | 24    | 86400  |
| 1.395 | 1.395 | 1.398 | 1.396  | 30    | 108000 |
| 1.362 | 1.366 | 1.357 | 1.361  | 48    | 172800 |
| 1.341 | 1.323 | 1.345 | 1.336  | 54    | 194400 |
| 1.268 | 1.247 | 1.300 | 1.271  | 72    | 259200 |
| 1.244 | 1.253 | 1.272 | 1.256  | 78    | 280800 |

Siendo el gráfico de dispersión de A promedio vs tiempo en segundos:

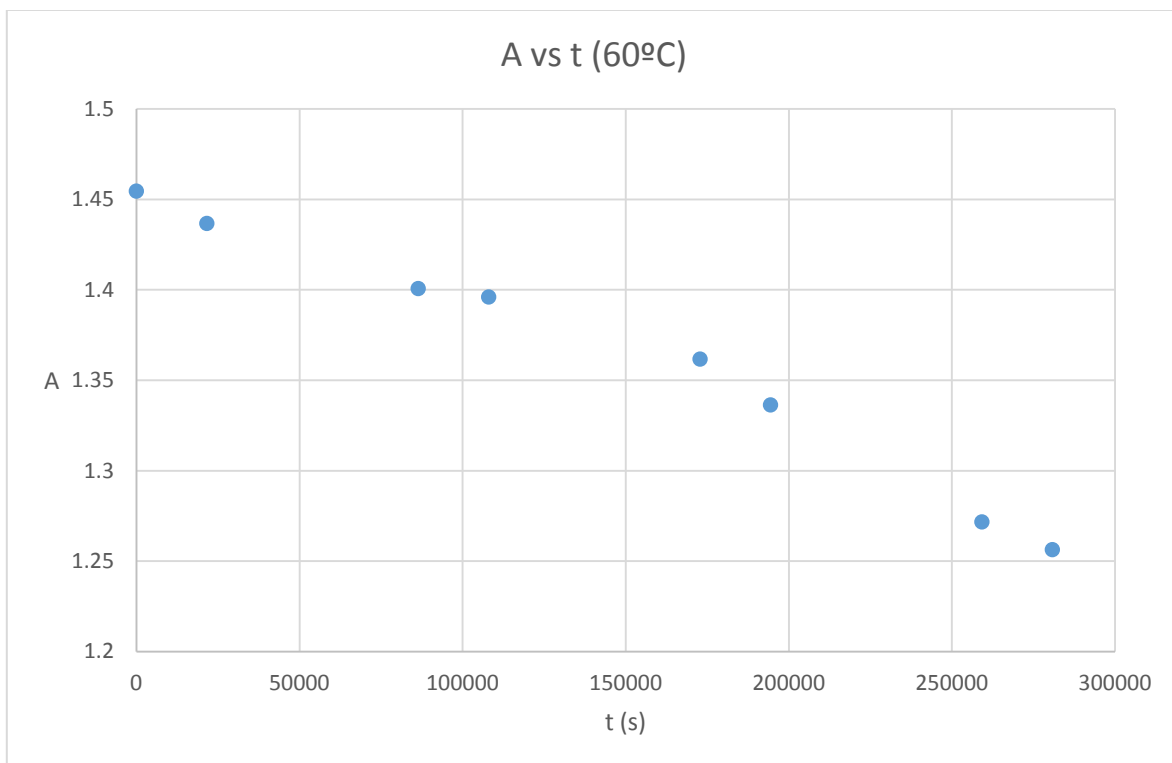


Gráfico 6 Estudio cinético de A vs t para 60°C

### 5.2.3 80°C

A la temperatura de trabajo de 80°C se obtuvieron los siguientes resultados:

Tabla 10 A vs t de la degradación de  $\beta$ -caroteno a 80°C

| A1    | A2    | A3    | A prom | t (h) | t (s)  |
|-------|-------|-------|--------|-------|--------|
| 1.465 | 1.468 | 1.479 | 1.470  | 0     | 0      |
| 1.423 | 1.428 | 1.429 | 1.426  | 6     | 21600  |
| 1.289 | 1.263 | 1.289 | 1.280  | 24    | 86400  |
| 1.245 | 1.240 | 1.241 | 1.242  | 30    | 108000 |
| 1.158 | 1.191 | 1.166 | 1.171  | 48    | 172800 |
| 1.132 | 1.130 | 1.139 | 1.133  | 54    | 194400 |
| 1.040 | 1.010 | 1.030 | 1.026  | 72    | 259200 |
| 0.880 | 0.950 | 1.090 | 0.973  | 78    | 280800 |

Siendo el gráfico de dispersión de A promedio vs tiempo en segundos:

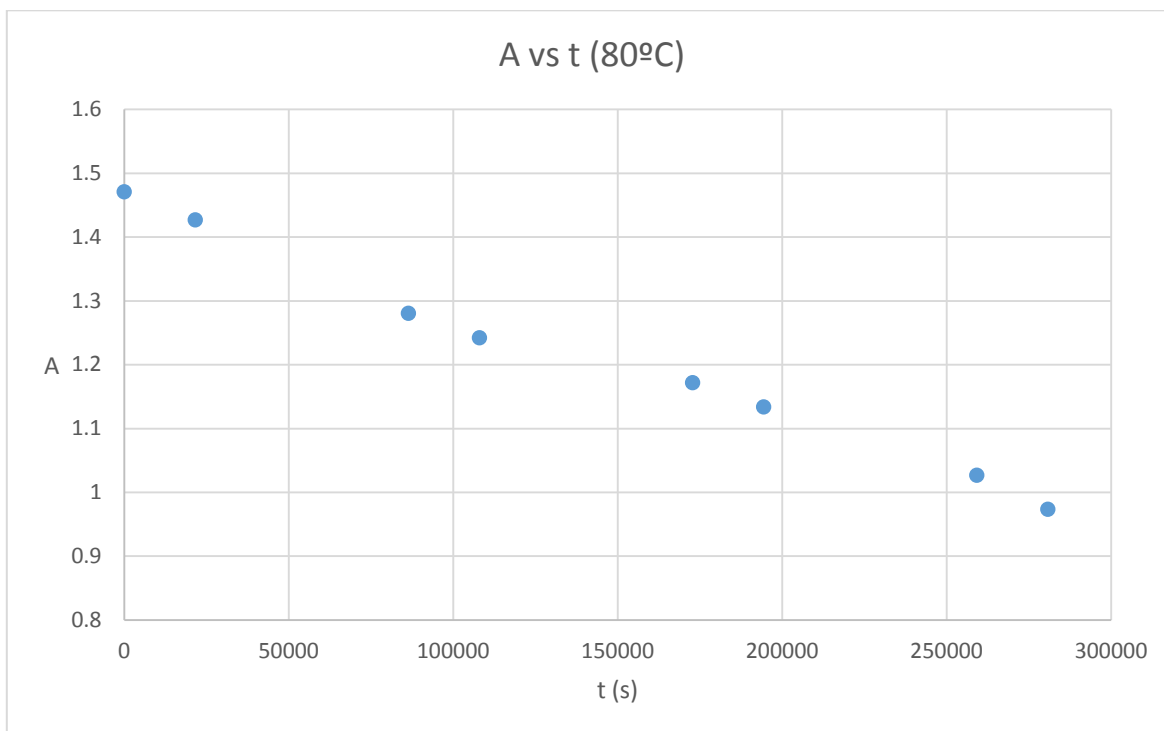


Gráfico 7 Estudio cinético de A vs t para 80°C

## 5.2.4 90°C

A la temperatura de trabajo de 90°C se obtuvieron los siguientes resultados:

Tabla 11 A vs t de la degradación de  $\beta$ -caroteno a 90°C

| A1    | A2    | A3    | A prom | t (h) | t (s)  |
|-------|-------|-------|--------|-------|--------|
| 1.472 | 1.472 | 1.473 | 1.473  | 0     | 0      |
| 1.285 | 1.302 | 1.301 | 1.296  | 6     | 21600  |
| 0.990 | 0.980 | 0.935 | 0.968  | 24    | 86400  |
| 0.888 | 0.891 | 0.876 | 0.885  | 30    | 108000 |
| 0.583 | 0.594 | 0.605 | 0.594  | 48    | 172800 |
| 0.501 | 0.495 | 0.517 | 0.504  | 54    | 194400 |
| 0.397 | 0.397 | 0.388 | 0.394  | 72    | 259200 |
| 0.321 | 0.351 | 0.392 | 0.355  | 78    | 280800 |

Siendo el gráfico de dispersión de A promedio vs tiempo en segundos:

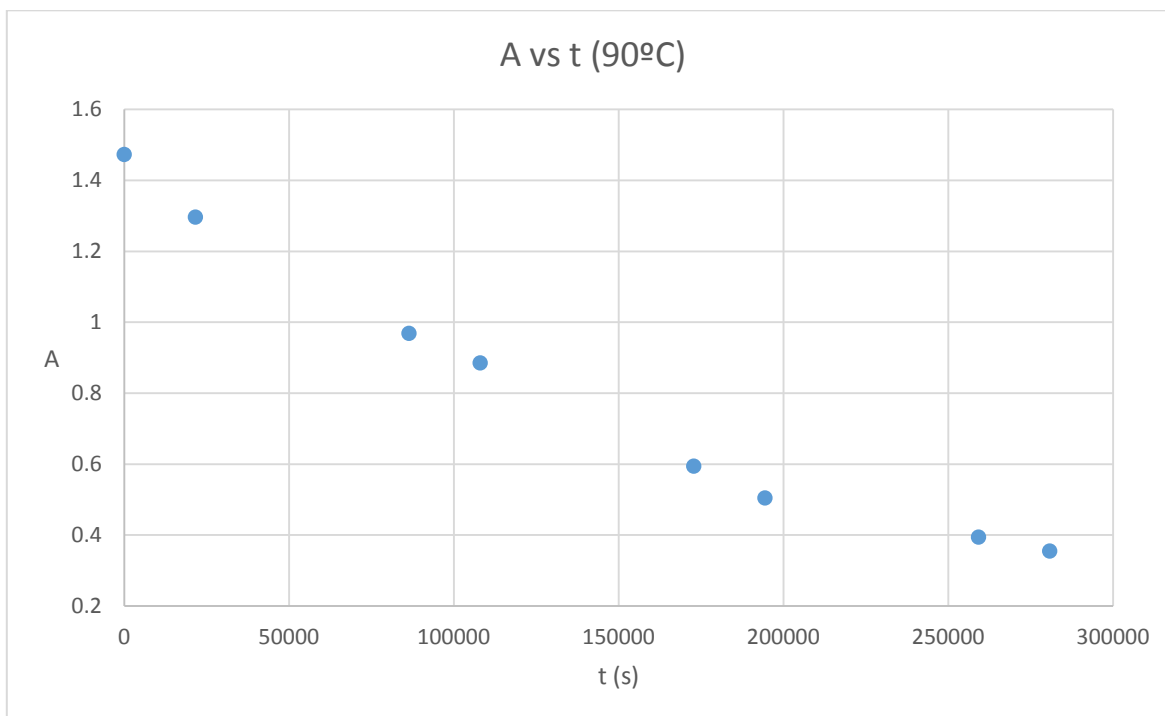


Gráfico 8 Estudio cinético de A vs t para 90°C



### 5.3 Orden de reacción

Para determinar el orden de reacción. Debe de considerarse el modelo general de descomposición para una reacción del tipo:



Donde A representa el  $\beta$ -caroteno y P los productos de descomposición térmica. Para la Ecuación (9) el modelo cinético para la descomposición térmica será:

$$\frac{d[A]}{dt} = -k[A]^n \quad (10)$$

Donde [A] es la concentración de  $\beta$ -caroteno,  $k$  la constante cinética y  $n$  el orden de reacción.

Resolviendo la Ecuación (10) se obtiene la siguiente expresión:

$$\int [A]^{-n} d[A] = -k \int dt \quad (11)$$

Obteniéndose la expresión:

$$[A]^{1-n} = (n-1)kt + C \quad (12)$$

Donde C es la constante de integración. Utilizando las condiciones iniciales donde  $t = 0$  puede demostrarse que dicha constante es igual a  $C = [A]_0^{1-n}$ , donde  $[A]_0$  es igual a la concentración inicial de  $\beta$ -caroteno.

La Ecuación (12) es válida para cualquier valor de  $n$  excepto 1. Cuando  $n$  es igual a 1, la resolución de la Ecuación (11) es igual a:

$$[A] = [A]_0 e^{-kt} \quad (13)$$

Por tanto para determinar el orden de reacción, se estudiará la dependencia lineal entre  $[A]^{1-n}$  vs  $t$  para cualquier valor de  $n$  excepto 1. Para un orden de reacción 1 se estudiará la dependencia lineal entre  $\ln[A]$  vs  $t$ . La relación que presente el mayor coeficiente de correlación ( $r$ ) determinará el orden de reacción que mejor describe los resultados cinéticos obtenidos.

Se determinarán los órdenes de reacción entre 0 y 3.5 en incrementos de 0.01; a pesar que un orden de 3 es muy poco probable desde el punto de vista cinético se verificará con los datos experimentales para observar/descartar cualquier concordancia con órdenes superiores de reacción.

### 5.3.1 42°C

Tabla 12 Multiorden para  $0 \geq n \geq 3.5; n \neq 1$  a 42°C

| A prom                                    | t (s)  | C (ppm) | n               |                 |                 |     |                 |
|---|--------|---------|-----------------|-----------------|-----------------|-----|-----------------|
|   |        |         | 0               | 0.01            | 0.02            | ... | 3.5             |
| 1.553                                     | 0      | 33.24   | 33.24           | 32.09           | 30.99           | ... | 0.0001570       |
| 1.550                                     | 21600  | 33.18   | 33.18           | 32.04           | 30.94           | ... | 0.0001577       |
| 1.548                                     | 86400  | 33.14   | 33.14           | 32.00           | 30.90           | ... | 0.0001581       |
| 1.543                                     | 108000 | 33.04   | 33.04           | 31.91           | 30.81           | ... | 0.0001593       |
| 1.536                                     | 172800 | 32.90   | 32.90           | 31.77           | 30.68           | ... | 0.0001611       |
| 1.530                                     | 194400 | 32.78   | 32.78           | 31.65           | 30.57           | ... | 0.0001626       |
| 1.522                                     | 259200 | 32.62   | 32.62           | 31.51           | 30.43           | ... | 0.0001645       |
| 1.519                                     | 280800 | 32.56   | 32.56           | 31.45           | 30.37           | ... | 0.0001652       |
| <b>r</b><br><b>[A]<sup>1-n</sup> vs t</b> |        |         | <b>0.985235</b> | <b>0.985233</b> | <b>0.985230</b> | ... | <b>0.984341</b> |

Siendo el mayor valor obtenido de r cuando el orden es 0.

Tabla 13 Mejor ajuste multiorden a 42°C

| Mejor ajuste multiorden (n) | Coefficiente de correlación lineal para [A] <sup>1-n</sup> vs t |
|-----------------------------|---|
| 0                           | 0.985235  |

Ahora comprobando los datos para orden 1.

Tabla 14 ajuste para orden 1 a 42°C

| A prom                       | t (s)  | C (ppm) | Ln (C)          |
|------------------------------|--------|---------|-----------------|
| 1.553                        | 0      | 33.24   | 3.50364040      |
| 1.550                        | 21600  | 33.18   | 3.50203737      |
| 1.548                        | 86400  | 33.14   | 3.50083341      |
| 1.543                        | 108000 | 33.04   | 3.49781715      |
| 1.536                        | 172800 | 32.90   | 3.49337678      |
| 1.530                        | 194400 | 32.78   | 3.48972903      |
| 1.522                        | 259200 | 32.62   | 3.48504856      |
| 1.519                        | 280800 | 32.56   | 3.48321110      |
| <b>r</b><br><b>ln C vs t</b> |        |         | <b>0.984987</b> |

Tabla 15 Comparación entre el ajuste de 1 orden y multiorden a 42°C

| Coefficiente de correlación lineal |                         |
|------------------------------------|-------------------------|
| 1 orden                            | Mejor ajuste multiorden |
| 0.984987                           | 0.985235                |

Para esta temperatura, comparando los coeficientes según la tabla 15, se observa que los datos se ajustan mejor a una tendencia de orden 0.

### 5.3.2 60°C

Tabla 16 Multiorden para  $0 \geq n \geq 3.5; n \neq 1$  a 60°C

| A prom                                    | t (s)  | C (ppm) | n               |                 |                 |     |                 |
|---|--------|---------|-----------------|-----------------|-----------------|-----|-----------------|
|   |        |         | 0               | 0.01            | 0.02            | ... | 3.5             |
| 1.455                                     | 0      | 31.27   | 31.27           | 30.21           | 29.19           | ... | 0.0001829       |
| 1.437                                     | 21600  | 30.91   | 30.91           | 29.87           | 28.86           | ... | 0.0001882       |
| 1.401                                     | 86400  | 30.20   | 30.20           | 29.18           | 28.21           | ... | 0.0001996       |
| 1.396                                     | 108000 | 30.10   | 30.10           | 29.09           | 28.12           | ... | 0.0002011       |
| 1.362                                     | 172800 | 29.42   | 29.42           | 28.44           | 27.49           | ... | 0.0002131       |
| 1.336                                     | 194400 | 28.91   | 28.91           | 27.95           | 27.03           | ... | 0.0002225       |
| 1.272                                     | 259200 | 27.62   | 27.62           | 26.72           | 25.85           | ... | 0.0002494       |
| 1.256                                     | 280800 | 27.31   | 27.31           | 26.43           | 25.57           | ... | 0.0002565       |
| <b>r</b><br><b>[A]<sup>1-n</sup> vs t</b> |        |         | <b>0.987174</b> | <b>0.987147</b> | <b>0.987120</b> | ... | <b>0.975730</b> |

Siendo el mayor valor obtenido de r cuando el orden es 0.

Tabla 17 Mejor ajuste multiorden a 60°C

| Mejor ajuste multiorden (n) | Coefficiente de correlación lineal para [A] <sup>1-n</sup> vs t |
|-----------------------------|---|
| 0                           | 0.987174  |

Ahora comprobando los datos para orden 1.

Tabla 18 ajuste para orden 1 a 60°C

| A prom                       | t (s)  | C (ppm) | Ln (C)          |
|------------------------------|--------|---------|-----------------|
| 1.553                        | 0      | 31.27   | 3.44267474      |
| 1.550                        | 21600  | 30.91   | 3.43120288      |
| 1.548                        | 86400  | 30.20   | 3.40768033      |
| 1.543                        | 108000 | 30.10   | 3.40459020      |
| 1.536                        | 172800 | 29.42   | 3.38155724      |
| 1.530                        | 194400 | 28.91   | 3.36421531      |
| 1.522                        | 259200 | 27.62   | 3.31853400      |
| 1.519                        | 280800 | 27.31   | 3.30738926      |
| <b>r</b><br><b>ln C vs t</b> |        |         | <b>0.984311</b> |

Tabla 19 Comparación entre el ajuste de 1 orden y multiorden a 60°C

| Coeficiente de correlación lineal |                         |
|-----------------------------------|-------------------------|
| 1 orden                           | Mejor ajuste multiorden |
| 0.984311                          | 0.987174                |

Para esta temperatura, comparando los coeficientes según la tabla 19, se observa que los datos se ajustan mejor a una tendencia de orden 0.

### 5.3.3 80°C

Tabla 20 Multiorden para  $0 \geq n \geq 3.5; n \neq 1$  a 80°C

| A<br>prom                                 | t (s)  | C<br>(ppm) | n         |           |           |     |           |
|---|--------|------------|-----------|-----------|-----------|-----|-----------|
|   |        |            | 0         | 0.01      | 0.02      | ... | 3.5       |
| 1.471                                     | 0      | 31.59      | 31.59     | 30.52     | 29.48     | ... | 0.0001783 |
| 1.427                                     | 21600  | 30.71      | 30.71     | 29.68     | 28.68     | ... | 0.0001913 |
| 1.280                                     | 86400  | 27.79      | 27.79     | 26.88     | 26.00     | ... | 0.0002456 |
| 1.242                                     | 108000 | 27.03      | 27.03     | 26.15     | 25.30     | ... | 0.0002633 |
| 1.172                                     | 172800 | 25.62      | 25.62     | 24.81     | 24.01     | ... | 0.0003009 |
| 1.134                                     | 194400 | 24.86      | 24.86     | 24.08     | 23.32     | ... | 0.0003244 |
| 1.027                                     | 259200 | 22.73      | 22.73     | 22.03     | 21.35     | ... | 0.0004060 |
| 0.973                                     | 280800 | 21.66      | 21.66     | 21.01     | 20.37     | ... | 0.0004578 |
| <b>r</b><br><b>[A]<sup>1-n</sup> vs t</b> |        |            | 0.9947018 | 0.9947293 | 0.9947564 | ... | 0.9828830 |

Siendo el mayor valor obtenido de r cuando el orden es 0.79.

Tabla 21 Mejor ajuste multiorden a 80°C

| Mejor ajuste multiorden<br>(n) | Coeficiente de correlación<br>lineal para [A] <sup>1-n</sup> vs t |
|--------------------------------|---|
| 0.79                           | 0.995796  |

Ahora comprobando los datos para orden 1.

Tabla 22 ajuste para orden 1 a 80°C

| <b>A prom</b>          | <b>t (s)</b> | <b>C (ppm)</b> | <b>Ln (C)</b>   |
|------------------------|--------------|----------------|-----------------|
| 1.553                  | 0            | 31.59          | 3.45292179      |
| 1.550                  | 21600        | 30.71          | 3.42472414      |
| 1.548                  | 86400        | 27.79          | 3.32477869      |
| 1.543                  | 108000       | 27.03          | 3.29685782      |
| 1.536                  | 172800       | 25.62          | 3.24350917      |
| 1.530                  | 194400       | 24.86          | 3.21345591      |
| 1.522                  | 259200       | 22.73          | 3.12363176      |
| 1.519                  | 280800       | 21.66          | 3.07565448      |
| <b>r<br/>ln C vs t</b> |              |                | <b>0.995714</b> |

Tabla 23 Comparación entre el ajuste de 1 orden y multiorden a 80°C

| <b>Coefficiente de correlación lineal</b> |                                |
|---|--------------------------------|
| <b>1 orden</b>                            | <b>Mejor ajuste multiorden</b> |
| 0.995714                                  | 0.995796                       |

Para esta temperatura, comparando los coeficientes según la tabla 23, se observa que los datos se ajustan mejor a una tendencia de orden 0.79.

### 5.3.4 90°C

Tabla 24 Multiorden para  $0 \geq n \geq 3.5; n \neq 1$  a 90°C

| <b>A prom</b>                       | <b>t (s)</b> | <b>C (ppm)</b> | <b>n</b> |             |             |            |            |
|-------------------------------------|--------------|----------------|----------|-------------|-------------|------------|------------|
|                                     |              |                | <b>0</b> | <b>0.01</b> | <b>0.02</b> | <b>...</b> | <b>3.5</b> |
| 1.473                               | 0            | 31.63          | 31.63    | 30.56       | 29.519      | ...        | 0.0001777  |
| 1.296                               | 21600        | 28.11          | 28.11    | 27.18       | 26.292      | ...        | 0.0002388  |
| 0.968                               | 86400        | 21.56          | 21.56    | 20.91       | 20.280      | ...        | 0.0004631  |
| 0.885                               | 108000       | 19.90          | 19.90    | 19.31       | 18.745      | ...        | 0.0005660  |
| 0.594                               | 172800       | 14.09          | 14.09    | 13.72       | 13.365      | ...        | 0.001342   |
| 0.504                               | 194400       | 12.30          | 12.30    | 12.00       | 11.699      | ...        | 0.001884   |
| 0.394                               | 259200       | 10.10          | 10.10    | 9.868       | 9.642       | ...        | 0.003086   |
| 0.355                               | 280800       | 9.313          | 9.313    | 9.108       | 8.907       | ...        | 0.003778   |
| <b>r<br/>[A]<sup>1-n</sup> vs t</b> |              |                | 0.980766 | 0.981039    | 0.981309    | ...        | 0.9489642  |

Siendo el mayor valor obtenido de r cuando el orden es 1.19.

Tabla 25 Mejor ajuste multiorden a 90°C

| Mejor ajuste multiorden (n) | Coefficiente de correlación lineal para $[A]^{1-n}$ vs t |
|-----------------------------|--|
| 1.19                        | 0.997556   |

Ahora comprobando los datos para orden 1.

Tabla 26 ajuste para orden 1 a 90°C

| A prom                 | t (s)  | C (ppm) | Ln (C)          |
|------------------------|--------|---------|-----------------|
| 1.553                  | 0      | 31.63   | 3.45412169      |
| 1.550                  | 21600  | 28.11   | 3.33596914      |
| 1.548                  | 86400  | 21.56   | 3.07103631      |
| 1.543                  | 108000 | 19.90   | 2.9907506       |
| 1.536                  | 172800 | 14.09   | 2.64555326      |
| 1.530                  | 194400 | 12.30   | 2.50969515      |
| 1.522                  | 259200 | 10.10   | 2.31239097      |
| 1.519                  | 280800 | 9.313   | 2.23144462      |
| <b>r<br/>ln C vs t</b> |        |         | <b>0.997113</b> |

Tabla 27 Comparación entre el ajuste de 1 orden y multiorden a 90°C

| Coefficiente de correlación lineal |                         |
|------------------------------------|-------------------------|
| 1 orden                            | Mejor ajuste multiorden |
| 0.997113                           | 0.997556                |

Para esta temperatura, comparando los coeficientes según la tabla 27, se observa que los datos se ajustan mejor a una tendencia de orden 1.19.

### 5.3.5 Comparativa entre los órdenes de reacción predichos.

El estudio cinético y el ajuste de los datos de las tablas 7-10 con las ecuaciones (12) y (13) se resumen en la siguiente tabla:

Tabla 28 Comparación entre los coeficientes de correlación entre los resultados del análisis de multiorden y orden 1

| Temperatura (°C) | Multiorden sugerido (n) | Coef correlación multiorden | Coef correlación orden 1 |
|------------------|-------------------------|-----------------------------|--------------------------|
| 42               | 0                       | 0.985235                    | 0.984987                 |
| 60               | 0                       | 0.987174                    | 0.984311                 |
| 80               | 0.79                    | 0.995796                    | 0.995714                 |
| 90               | 1.19                    | 0.997556                    | 0.997113                 |

Considerando los coeficientes de correlación y los órdenes estudiados los datos experimentales muestra un cambio en el orden de reacción a medida la temperatura aumenta.

Este cambio en el orden de reacción puede deberse a dos factores, el primero un cambio en el mecanismo de reacción. Esto es poco probable ya que la literatura referenciada muestra que el  $\beta$ -caroteno obedece a una descomposición de orden establecido en un amplio rango de temperatura.

La segunda causa, la más probable, es que a las temperaturas de 42 y 60 °C la degradación fue relativamente lenta en el intervalo de tiempo estudiado, por lo que el orden cinético predominante fue cero. Ya en las temperaturas de 80 y 90 °C la degradación fue más extensa y permitió definir mejor el orden de reacción. En ésta última temperatura, la cinética logró sobrepasar un tiempo de vida media.

Es sugerido que la reacción transcurra a modo de sobrepasar varios tiempos de vida media para obtener datos cinéticos que puedan analizarse mediante las ecuaciones integradas de velocidad. Considerando la existencia del error experimental, es importante que la reacción transcurra de preferencia entre un 70 a 90% ya que en los momentos iniciales aunado al error experimental los datos podrían ajustarse al orden incorrecto. [137] [138]

Sin embargo darle seguimiento a la reacción a modo de alcanzar el 70% es prácticamente inviable por lo lento de la cinética a temperaturas debajo de 90°C (ver Tabla 32). Por otra parte utilizar el método de las velocidades iniciales resultó inviable al no poder tener un verdadero control en la concentración inicial de  $\beta$ -caroteno en las muestras de aceite al ser una matriz compleja.

*Tabla 29 Comparación entre los coeficientes de correlación entre los órdenes obtenidos.*

| <b>Temperatura (°C)</b> | <b>Coefficiente de correlación orden 0</b> | <b>Coefficiente de correlación orden 0.79</b> | <b>Coefficiente de correlación orden 1</b> | <b>Coefficiente de correlación orden 1.19</b> |
|-------------------------|--|---|--|---|
| 42                      | 0.985235                                   | 0.985039                                      | 0.984987                                   | 0.984939                                      |
| 60                      | 0.987174                                   | 0.984940                                      | 0.984311                                   | 0.983729                                      |
| 80                      | 0.994702                                   | 0.995796                                      | 0.995714                                   | 0.995504                                      |
| 90                      | 0.980766                                   | 0.995613                                      | 0.997113                                   | 0.997556                                      |
| <b>Suma</b>             | <b>3.947877</b>                            | <b>3.961388</b>                               | <b>3.962125</b>                            | <b>3.961728</b>                               |

Se observa en la Tabla 28 la compilación de los coeficientes de correlación lineal entre los órdenes sugeridos según el análisis de multiorden y el análisis de orden 1. A simple vista es difícil determinar cuál es el orden que gobernó el sistema es estudio. Como se mencionó anteriormente, los órdenes de reacción predichos para las temperaturas 42 y 60 °C son cero debido al poco avance de reacción en el tiempo estudiado sin embargo, en las temperaturas de 80 y 90 °C el avance de reacción ya fue considerable y el modelo cinético logra definirse mejor. Pero al observar los coeficientes según la tabla 28 es difícil, a simple vista, establecer un orden de reacción global.

Una manera de determinar el orden de reacción global puede considerarse al sumar los coeficientes de correlación para cada temperatura y cada orden predicho. El orden de reacción que obtenga la mayor suma refleja una mayor correlación global entre el orden de reacción predicho y las temperaturas de estudio. Se observa que la suma que da el valor mayor es la respectiva a orden 1. Por lo tanto, el sistema obedece de manera general en el rango de temperaturas estudiadas una cinética de primer orden.

## 5.4 Energía de Activación

Según el análisis en 5.3.5 la degradación térmica del b-caroteno en el rango de temperaturas de 42-90 °C obedece una cinética de primer orden, por lo que, la constante cinética estará dada por la resolución de la Ecuación (10) cuando  $n = 1$ :

$$\frac{d[\beta - \text{Caroteno}]}{dt} = -k[\beta - \text{Caroteno}] \quad (14)$$

Siendo la resolución:

$$\ln[\beta - \text{Caroteno}] = -kt + C \quad (15)$$

Donde C es igual a  $\ln[\beta - \text{Caroteno}]_0$ , y  $[\beta - \text{Caroteno}]_0$  es igual a la concentración de b-caroteno al inicio del estudio cinético. Ajustando los datos de cada temperatura al modelo de  $\ln[\beta - \text{Caroteno}]$  vs  $t$ , se obtiene la constante cinética como el negativo de la pendiente:

*Tabla 30 Constantes cinéticas de primer orden para las temperaturas estudiadas.*

| Temperatura | Constante cinética de orden 1 (s <sup>-1</sup> ) | Error típico de la regresión en la pendiente. |
|-------------|--|---|
| <b>42</b>   | $7.44886 \times 10^{-8}$                         | $\pm 5.32955 \times 10^{-9}$                  |
| <b>60</b>   | $4.69321 \times 10^{-7}$                         | $\pm 3.43446 \times 10^{-8}$                  |
| <b>80</b>   | $1.27646 \times 10^{-6}$                         | $\pm 4.84003 \times 10^{-8}$                  |
| <b>90</b>   | $4.42908 \times 10^{-6}$                         | $\pm 1.37696 \times 10^{-7}$                  |

Con los datos obtenidos en la tabla 29, es posible calcular la energía de activación según el modelo de Arrhenius. Para utilizar este modelo, basta obtener la ecuación integrada a partir de la Ecuación (4):

$$\ln k = -\frac{E_a}{R} \left( \frac{1}{T} \right) + \ln A \quad (16)$$



Donde  $k$  es la constante cinética a la temperatura  $T$ ,  $E_a$  la energía de activación,  $R$  la constante universal de los gases,  $T$  la temperatura de estudio y  $A$  el parámetro pre exponencial de la Ecuación (4).

Una representación de  $\ln K$  vs  $1/T$  da como resultado:

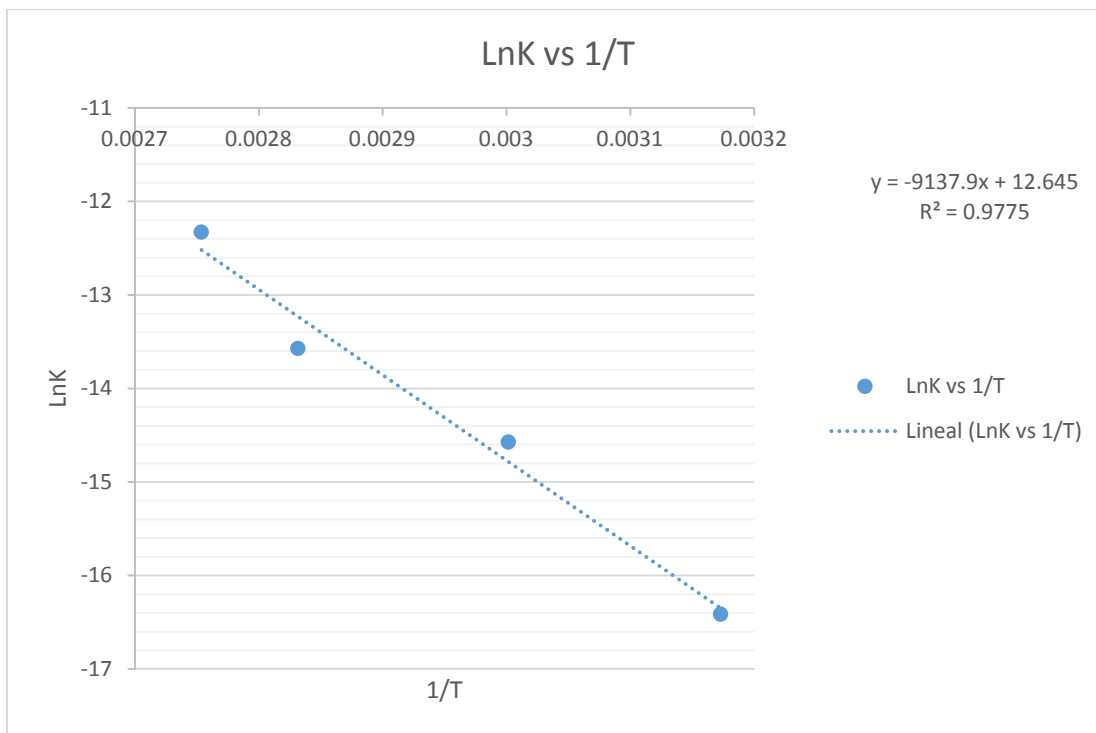


Gráfico 9 Dependencia de la constante cinética con la temperatura sobre el modelo de Arrhenius.

Del negativo de la pendiente puede obtenerse la energía de activación y del antilogaritmo natural del intercepto el factor pre exponencial:

Tabla 31 Energía de activación y factor pre exponencial.

| Energía de activación     | Error típico de regresión de pendiente | Factor pre exponencial | Error típico de regresión de intercepto |
|---------------------------|--|------------------------|---|
| $75972.8 \frac{J}{mol K}$ | $\pm 981.102$                          | $3.10173 \times 10^5$  | $\pm 2.88882$                           |

Comparando este resultado con los observados en la Tabla 4 se observa que el valor de energía de activación obtenido es menor comparado con la oleína de palma. Esto permite establecer que en la muestra de aceite de palma crudo la degradación térmica del  $\beta$ -caroteno ocurre con mayor facilidad y por tanto con una cinética más rápida.

## 5.5 Tiempo de vida media, tiempo de reducción decimal y resistencia térmica.

El tiempo de vida media se refiere al tiempo necesario para que la cantidad de  $\beta$ -caroteno se reduzca al 50% respecto a la inicial. Considerando la Ecuación (15), el tiempo de vida media quedaría expresado por:

$$t_{50\%} = t_{1/2} = \frac{\ln 2}{k} \quad (17)$$

Donde  $t_{1/2}$  representa el tiempo de reacción para un avance del 50% y  $k$  es la constante cinética a la temperatura específica. El tiempo de vida media es un parámetro importante, que permite establecer una rápida comparación entre sistemas cinéticos y a la vez permite establecer un diseño cinético según lo discutido en 5.3.5,

De manera similar al tiempo de vida media, el tiempo de reducción decimal es el tiempo necesario para que únicamente quede el 10% de  $\beta$ -caroteno en el sistema. En otras palabras, es el tiempo necesario para que la reacción avance en un 90%. Este parámetro es importante en el ámbito de los alimentos y la esterilización de preparados. Comúnmente se utiliza en poblaciones de microorganismos que se desea reducir su población como en la esterilización de alimentos [139]. Dicho parámetro se expresa por la Ecuación (3)

La resistencia térmica (o parámetro  $z$ ) se define como el cambio de temperatura que debe realizarse sobre una temperatura de referencia para disminuir el tiempo de reducción decimal en un factor de 10 [140]. Por ejemplo, si el tiempo de reducción decimal a 25°C es de 15 minutos y el factor  $z$  es igual a 20°C, quiere decir que a 45°C el tiempo de reducción decimal debe ser igual a 1.5 minutos (10 veces menos que la temperatura de referencia). En otras palabras, el factor  $z$  nos dice cuanto debemos sumarle a la temperatura de inicio para que la cinética sea 10 veces más rápida.

Puede observarse que entre mayor sea el valor de  $z$  mayor será la resistencia térmica del analito estudiado, ya que se requerirá un mayor aumento de temperatura para acelerar la descomposición en un factor de 10. De igual forma que el tiempo de reducción decimal, la resistencia térmica tiene su mayor aplicación en la industria de alimentos y los procesos de esterilización, ya que es un valor de referencia que permite ajustar los procesos de esterilización y pasteurizado de manera rápida.

Por tanto, considerando el tiempo de reducción decimal para una  $T$  dada, el tiempo de reducción decimal que cumpla la definición del factor  $z$  debe de cumplir:

$$D_1 = 10D_2 \quad (18)$$

Ya que el sistema obedece una cinética de orden 1, puede usarse la Ecuación (18) en la Ecuación (3), dando como resultado:

$$\frac{k_2}{k_1} = 10 \quad (19)$$

Donde  $k_1$  es la constante cinética a la temperatura de referencia y  $k_2$  la constante cinética a la nueva temperatura que cumple la condición de la Ecuación (18). Usando la Ecuación (4) con la Ecuación (19) podemos obtener la relación que permitirá calcular la nueva temperatura:

$$10 = \frac{Ae^{-\frac{E_a}{RT_2}}}{Ae^{-\frac{E_a}{RT_1}}} \quad (20)$$

De la cual se puede despejar la nueva temperatura:

$$T_2 = \left( T_1^{-1} - \frac{R \ln 10}{E_a} \right)^{-1} \quad (21)$$

Pero, según lo discutido, el factor z no es más que la diferencia entre estas dos temperaturas, obtenemos la expresión para calcular la resistencia térmica para cada temperatura de estudio:

$$z = \left( T_1^{-1} - \frac{R \ln 10}{E_a} \right)^{-1} - T_1 \quad (22)$$

Así por ejemplo, para la temperatura inicial de 42°C, la resistencia térmica es igual a 27.19°C. Lo cual significa que debe subirse la temperatura en dicho valor para que, a la nueva temperatura (69.19°C) la cinética sea 10 veces más rápida comparada a 42°C.

La resistencia térmica no solo afecta el tiempo de reducción decimal, si no que cualquier tiempo fraccionario que se estudie. Ya que es la cinética global la que aumenta, el parámetro z también tiene significado para el tiempo de vida media, ya que es el aumento de temperatura necesario para reducir también el tiempo de vida media en un factor de 10.

Siendo los resultados para cada temperatura:

Tabla 32 Parámetros cinéticos para la degradación térmica del  $\beta$ -caroteno considerando un modelo de orden 1.

| Temperatura (°C) | Tiempo de vida media (s) | Tiempo de vida media (días) | Tiempo de reducción decimal (s) | Tiempo de reducción decimal (días) | Resistencia térmica z (°C) |
|------------------|--------------------------|-----------------------------|---------------------------------|------------------------------------|----------------------------|
| 42               | 9305417                  | 107.7                       | 30911927                        | 357.8                              | 27.2                       |
| 60               | 1476916                  | 17.09                       | 4906209.9                       | 56.785                             | 30.5                       |
| 80               | 543024.6                 | 6.285                       | 1803888.8                       | 20.878                             | 34.5                       |
| 90               | 156499.2                 | 1.811                       | 519879.09                       | 6.0171                             | 36.6                       |

Los resultados de los parámetros cinéticos muestran la dificultad de realizar un estudio cinético con las temperaturas de 42 y 60 °C por el tiempo que debe esperarse para alcanzar como mínimo un tiempo de vida media, ya que el diseño experimental dadas las limitantes de tiempo y el uso de los recursos de la escuela de química limitaron el tiempo máximo de estudio a 3 días por cada replica de temperatura.

Por otra parte, la degradación térmica del  $\beta$ -caroteno a la temperatura de 42°C es relativamente lenta comparado al tiempo promedio de transporte, almacenamiento y procesamiento industrial del aceite de palma crudo. Además de ser impráctica a nivel de laboratorio, ya que el tiempo para alcanzar el primer tiempo de vida media es considerablemente grande y los datos arrojados en tiempos inferiores no son conclusivos porque se confunden con un orden de reacción igual a cero por el poco avance de reacción.

## 6 Conclusiones

1. La cinética de degradación del  $\beta$ -caroteno en aceite de palma crudo puede seguirse mediante el estudio de absorción vs tiempo empleando una longitud de onda de 450 nm. El análisis mediante HPLC mostró que no existe ninguna otra sustancia que absorba de manera cuantitativa en la matriz estudiada.
2. La degradación del  $\beta$ -caroteno en aceite de palma crudo es fuertemente activada por la temperatura. Durante este estudio fue la única variable considerada y pudo observarse un aumento de aproximadamente 60 veces la velocidad de reacción al comparar las constantes cinéticas a 42 y 90 °C.
3. La cinética de degradación obedece un modelo de orden 1, estando en concordancia con la mayoría de fuentes citadas. Dicho orden puede no ser un orden verdadero ya que la matriz del aceite de palma crudo es muy compleja y en ella existen efectos sinérgicos y antagonicos con la degradación térmica del  $\beta$ -caroteno. Dicho orden de reacción debe ser considerado de mejor manera como un pseudo orden 1.
4. En el rango de temperaturas de 42 a 90 °C y con un tiempo de estudio de 6 horas para cada temperatura no es posible determinar de manera conclusiva el orden global de reacción. Debido a la cinética relativamente lenta a las temperaturas más bajas estudiadas que se solapan con un orden 0 por el poco avance de reacción.
5. Los parámetros cinéticos pudieron obtenerse satisfactoriamente y tener relación con estudios cinéticos de degradación de  $\beta$ -caroteno no solo en aceite de palma crudo si no en otras matrices complejas de alimentos, ver tabla 4.
6. Con el fin de obtener un aceite de palma con la mayor cantidad de  $\beta$ -caroteno posible debe trabajarse a bajas temperaturas y tiempos largos en contra de altas temperaturas y tiempos cortos.
7. Considerando los parámetros cinéticos es posible diseñar un método de extracción del  $\beta$ -caroteno del aceite de palma crudo siempre y cuando la relación entre el tiempo del procesado y temperatura de éste considere los tiempos de reducción media y decimal.

## 7 Recomendaciones

1. Para realizar un estudio cinético deben de tenerse en cuenta que el sistema sea lo suficientemente rápido para que la concentración disminuya de manera fácil y cuantitativa de medir. Lo suficientemente lenta para tomar mediciones durante un lapso de 8 horas a 3 días.
2. Es importante que durante el estudio cinético logre alcanzarse como mínimo un tiempo de vida media. Con esto se evita que el orden de reacción pueda confundirse con un orden cero sin serlo necesariamente debido al poco avance de reacción.
3. Si la reacción es muy lenta, es preferible utilizar el método de las velocidades iniciales utilizando diferentes valores de concentración iniciales y medir su variación durante poco tiempo. Esto tiene el inconveniente de poderse usar en matrices complejas donde la concentración inicial no es tan fácil de manipular, además de requerir técnicas de medición que permitan cuantificar la pequeña variación en el reactante o en uno de los productos.
4. De preferencia utilizar un termostato automático, para tener un control térmico mas adecuado.
5. Ampliar el rango de temperatura arriba de los 90°C para obtener una cinética con mayor grado de avance y poder alcanzar cinco tiempos de vida media, tiempo considerado como el final de una cinética de orden 1.
6. Estudiar la correlación entre la temperatura, la acidez, presión, impurezas como el hierro y agua que son agentes comúnmente presentes durante el transporte y procesado del aceite de palma en las plantas aceiteras del país.

## 8 Anexos

Tabla 33 Proceso de Refinación del Aceite de Palma [124]

| Temperaturas                                      | Proceso   | Tiempo      |
|---|---|-------------|
| Almacenamiento a temperatura ambiente $\pm 40$ °C | Se recibe de cisternas de acero inoxidable que contienen volúmenes de hasta 24T. Posteriormente se descargan a tanques designados, generalmente de hierro.  |             |
| 85-105 °C   | <b>Desgomado</b><br>Se le adiciona una solución de ácido cítrico 0.1% Separación de gomas (fosfátidos y fosforo). Se traslada a la planta a través de un intercambiador de calor, que son tuberías de acero inoxidable que a su vez contiene internamente un tubo que refluja aceite térmico y eleva la temperatura.  | 45 min      |
| 95-110 °C<br>1% de tierra                         | <b>Blanqueo con arcillas</b><br>Del intercambiador de calor pasa a un contenedor denominado Tanque Slurry donde se le dosifica la arcilla blanqueadora (bentonitas o montmorillonitas), siendo éste un proceso de adsorción que remueve color y otras impurezas menores.<br>Se traslada del Slurry a otro tanque denominado blanqueo utilizando vacío.  | 1 - 2 horas |
| 110-160 °C  | <b>Filtros (placas)</b><br>Pasa el contenido de blanqueo por filtros donde se descarta la tierra, agua, solidos, metales, etc. Estos residuos son enviados a MIDES. Se dosifica ácido cítrico aquí también para evitar obstrucciones.   | 45 min      |
| 245-255 °C<br>3-5 mm Hg                           | <b>Desodorizado</b><br>Después de ser filtrado el aceite va hacia la planta de desodorizado para eliminar el color residual.<br>Se calienta utilizando vapor. Se evaporan en este punto los ácidos grasos volátiles y se inhibe la producción de grasas trans.<br>Algunos tocoferoles y tocotrienoles, monoglicéridos, productos de oxidación y de descomposición de pigmentos se remueven durante la etapa de desodorización y se condensan, a medida que el ácido graso de la palma se destila. | 3 horas     |

- Un aceite de buena calidad es aquel que está libre de jabones, arcilla de blanqueo, o catalizador residual (si fue hidrogenado); porcentaje de AGL menor de 0.1%, fósforo menor a 1 ppm; y hierro de menor a 0.1 ppm.
- Para mantener el calor o temperaturas se utiliza aceite térmico grado alimenticio. Pasa por tubería especial para su flujo en los tanques y/o contenedores. En la caldera.

Tabla 34 Multiorden para  $0 \leq n \leq 3.5$ ;  $n \neq 1$  a 42ª. Análisis completo.

| t (s)        | 0                         | 21600      | 86400      | 108000     | 172800     | 194400     | 259200     | 280800     | r          |
|--------------|---------------------------|------------|------------|------------|------------|------------|------------|------------|------------|
| experimental | 33.2362251                | 33.1829891 | 33.1430621 | 33.0432447 | 32.8968458 | 32.7770648 | 32.6240114 | 32.564121  |            |
| n            | C <sup>Λ</sup> (1-n)(ppm) |            |            |            |            |            |            |            |            |
| 0            | 33.2362251                | 33.1829891 | 33.1430621 | 33.0432447 | 32.8968458 | 32.7770648 | 32.6240114 | 32.564121  | 0.98523562 |
| 0.01         | 32.0919107                | 32.0410212 | 32.0028536 | 31.9074325 | 31.7674764 | 31.6529622 | 31.5066325 | 31.4493711 | 0.98523317 |
| 0.02         | 30.9869947                | 30.9383533 | 30.9018712 | 30.8106622 | 30.676879  | 30.5674112 | 30.427524  | 30.3727819 | 0.98523072 |
| 0.03         | 29.9201207                | 29.8736329 | 29.8387656 | 29.7515917 | 29.6237225 | 29.5190896 | 29.3853752 | 29.333047  | 0.98522826 |
| 0.04         | 28.8899789                | 28.845554  | 28.8122335 | 28.7289252 | 28.6067215 | 28.5067205 | 28.3789202 | 28.3289048 | 0.98522581 |
| 0.05         | 27.8953045                | 27.8528557 | 27.8210169 | 27.7414114 | 27.6246348 | 27.5290711 | 27.4069364 | 27.3591368 | 0.98522335 |
| 0.06         | 26.9348766                | 26.8943204 | 26.8639007 | 26.7878418 | 26.6762638 | 26.5849505 | 26.4682434 | 26.4225664 | 0.98522089 |
| 0.07         | 26.0075159                | 25.9687724 | 25.9397118 | 25.8670498 | 25.7604509 | 25.673209  | 25.5617007 | 25.5180571 | 0.98521843 |
| 0.08         | 25.1120841                | 25.0750764 | 25.0473175 | 24.9779086 | 24.8760785 | 24.792736  | 24.6862073 | 24.6445113 | 0.98521598 |
| 0.09         | 24.2474817                | 24.2121363 | 24.1856239 | 24.1193303 | 24.0220671 | 23.9424591 | 23.8406997 | 23.8008692 | 0.98521352 |
| 0.1          | 23.4126473                | 23.3788936 | 23.3535748 | 23.2902643 | 23.1973745 | 23.1213429 | 23.024151  | 22.986107  | 0.98521106 |
| 0.11         | 22.606556                 | 22.5743263 | 22.5501503 | 22.4896963 | 22.400994  | 22.3283871 | 22.2355692 | 22.1992361 | 0.9852086  |
| 0.12         | 21.8282183                | 21.7974477 | 21.7743658 | 21.7166466 | 21.6319539 | 21.5626261 | 21.4739965 | 21.4393017 | 0.98520614 |
| 0.13         | 21.0766785                | 21.0473047 | 21.0252704 | 20.9701693 | 20.8893153 | 20.8231272 | 20.7385078 | 20.7053818 | 0.98520368 |
| 0.14         | 20.3510141                | 20.3229774 | 20.3019457 | 20.2493511 | 20.172172  | 20.1089897 | 20.0282097 | 19.9965857 | 0.98520122 |
| 0.15         | 19.6503341                | 19.6235772 | 19.6035054 | 19.5533099 | 19.4796487 | 19.4193438 | 19.3422395 | 19.3120535 | 0.98519875 |
| 0.16         | 18.9737783                | 18.9482464 | 18.9290932 | 18.8811941 | 18.8109001 | 18.7533496 | 18.6797639 | 18.6509545 | 0.98519629 |
| 0.17         | 18.3205161                | 18.2961566 | 18.2778826 | 18.2321813 | 18.1651101 | 18.110196  | 18.0399782 | 18.0124865 | 0.98519383 |
| 0.18         | 17.6897456                | 17.666508  | 17.6490754 | 17.6054773 | 17.5414905 | 17.4890995 | 17.4221054 | 17.3958749 | 0.98519137 |
| 0.19         | 17.0806923                | 17.0585282 | 17.0419007 | 17.0003153 | 16.9392801 | 16.8893038 | 16.8253947 | 16.8003713 | 0.9851889  |
| 0.2          | 16.4926086                | 16.4714717 | 16.4556145 | 16.4159549 | 16.357744  | 16.3100784 | 16.2491216 | 16.2252534 | 0.98518644 |
| 0.21         | 15.9247725                | 15.9046182 | 15.8894981 | 15.8516809 | 15.7961724 | 15.7507177 | 15.6925859 | 15.6698231 | 0.98518397 |
| 0.22         | 15.3764868                | 15.3572726 | 15.3428575 | 15.3068031 | 15.2538799 | 15.2105405 | 15.1551117 | 15.1334066 | 0.9851815  |
| 0.23         | 14.8470784                | 14.8287635 | 14.8150229 | 14.7806546 | 14.7302046 | 14.6888889 | 14.6360461 | 14.6153529 | 0.98517904 |
| 0.24         | 14.3358974                | 14.3184426 | 14.3053471 | 14.2725917 | 14.2245074 | 14.1851276 | 14.1347585 | 14.1150335 | 0.98517657 |
| 0.25         | 13.8423163                | 13.8256841 | 13.8132055 | 13.7819927 | 13.7361712 | 13.6986429 | 13.6506402 | 13.6318412 | 0.9851741  |
| 0.26         | 13.365729                 | 13.3498834 | 13.3379949 | 13.3082573 | 13.2645998 | 13.2288425 | 13.183103  | 13.1651898 | 0.98517163 |
| 0.27         | 12.9055505                | 12.8904571 | 12.8791328 | 12.8508058 | 12.8092178 | 12.775154  | 12.7315791 | 12.7145131 | 0.98516917 |
| 0.28         | 12.4612158                | 12.4468416 | 12.4360567 | 12.4090786 | 12.3694693 | 12.337025  | 12.29552   | 12.2792641 | 0.9851667  |
| 0.29         | 12.0321795                | 12.0184928 | 12.0082237 | 11.982535  | 11.9448176 | 11.9139217 | 11.8743959 | 11.8589147 | 0.98516423 |
| 0.3          | 11.6179147                | 11.6048853 | 11.5951092 | 11.5706533 | 11.5347446 | 11.505329  | 11.4676955 | 11.4529549 | 0.98516175 |
| 0.31         | 11.217913                 | 11.2055118 | 11.1962069 | 11.1729294 | 11.1387495 | 11.1107491 | 11.0749246 | 11.0608922 | 0.98515928 |
| 0.32         | 10.8316832                | 10.8198825 | 10.8110279 | 10.7888766 | 10.7563493 | 10.7297015 | 10.6956062 | 10.6822507 | 0.98515681 |
| 0.33         | 10.4587512                | 10.4475243 | 10.4391001 | 10.4180251 | 10.3870771 | 10.3617221 | 10.3292796 | 10.316571  | 0.98515434 |
| 0.34         | 10.0986592                | 10.0879805 | 10.0799676 | 10.0599211 | 10.0304822 | 10.0063627 | 9.97549966 | 9.96340943 | 0.98515187 |
| 0.35         | 9.75096504                | 9.74081013 | 9.7331902  | 9.71412631 | 9.68612944 | 9.66319045 | 9.63383679 | 9.62233746 | 0.98514939 |



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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.36 | 9.4152419  | 9.40558739 | 9.39834285 | 9.38021773 | 9.35359854 | 9.33178746 | 9.30387594 | 9.29294122 | 0.98514692 |
| 0.37 | 9.09107762 | 9.0819011  | 9.07501513 | 9.05778677 | 9.03248363 | 9.01175006 | 8.98521632 | 8.97482102 | 0.98514444 |
| 0.38 | 8.77807423 | 8.76935422 | 8.76281073 | 8.74643888 | 8.7223928  | 8.70268847 | 8.67747085 | 8.66759086 | 0.98514197 |
| 0.39 | 8.47584746 | 8.46756342 | 8.46134698 | 8.44579311 | 8.42294758 | 8.40422627 | 8.38026573 | 8.37087794 | 0.98513949 |
| 0.4  | 8.18402627 | 8.17615852 | 8.17025438 | 8.15548159 | 8.13378251 | 8.11599996 | 8.09323994 | 8.08432223 | 0.98513702 |
| 0.41 | 7.90225242 | 7.8947821  | 7.88917614 | 7.8751491  | 7.85454465 | 7.83765848 | 7.81604485 | 7.80757603 | 0.98513454 |
| 0.42 | 7.63017996 | 7.62308904 | 7.61776772 | 7.60445262 | 7.5848932  | 7.56886284 | 7.54834374 | 7.54030353 | 0.98513206 |
| 0.43 | 7.36747489 | 7.3607461  | 7.35569647 | 7.34306092 | 7.32449906 | 7.30928565 | 7.28981145 | 7.28218042 | 0.98512958 |
| 0.44 | 7.11381468 | 7.1074315  | 7.10264115 | 7.09065417 | 7.07304441 | 7.05861076 | 7.04013394 | 7.03289351 | 0.9851271  |
| 0.45 | 6.86888793 | 6.86283453 | 6.85829161 | 6.84692353 | 6.83022236 | 6.81653287 | 6.79900794 | 6.79214029 | 0.98512462 |
| 0.46 | 6.63239393 | 6.62665518 | 6.62234833 | 6.61157077 | 6.59573654 | 6.58275714 | 6.56614055 | 6.55962865 | 0.98512214 |
| 0.47 | 6.40404237 | 6.39860377 | 6.39452213 | 6.3843079  | 6.36930076 | 6.35699884 | 6.34124892 | 6.33507645 | 0.98511966 |
| 0.48 | 6.18355289 | 6.17840058 | 6.17453374 | 6.16485686 | 6.15063867 | 6.13898301 | 6.12405987 | 6.11821123 | 0.98511718 |
| 0.49 | 5.9706548  | 5.96577552 | 5.96211353 | 5.95294911 | 5.93948339 | 5.92844412 | 5.91430958 | 5.90876984 | 0.9851147  |
| 0.5  | 5.76508674 | 5.76046779 | 5.75700114 | 5.74832538 | 5.7355772  | 5.72512575 | 5.71174329 | 5.70649813 | 0.98511222 |
| 0.51 | 5.56659633 | 5.56222557 | 5.55894516 | 5.55073529 | 5.53867123 | 5.52878026 | 5.51611494 | 5.51115069 | 0.98510974 |
| 0.52 | 5.37493989 | 5.37080571 | 5.36770282 | 5.35993706 | 5.34852517 | 5.33916852 | 5.32718689 | 5.32249047 | 0.98510725 |
| 0.53 | 5.18988214 | 5.18597343 | 5.18303972 | 5.17569723 | 5.16490695 | 5.15605959 | 5.14472967 | 5.14028855 | 0.98510477 |
| 0.54 | 5.01119587 | 5.00750201 | 5.00472951 | 4.99779037 | 4.98759245 | 4.97923046 | 4.96852164 | 4.96432385 | 0.98510228 |
| 0.55 | 4.83866172 | 4.83517255 | 4.83255365 | 4.82599879 | 4.81636527 | 4.80846575 | 4.79834878 | 4.79438286 | 0.9850998  |
| 0.56 | 4.67206788 | 4.66877368 | 4.66630109 | 4.6601123  | 4.65101643 | 4.64355749 | 4.63400437 | 4.63025936 | 0.98509731 |
| 0.57 | 4.51120982 | 4.50810131 | 4.50576805 | 4.4999279  | 4.49134412 | 4.48430482 | 4.47528878 | 4.47175421 | 0.98509483 |
| 0.58 | 4.35589007 | 4.35295835 | 4.35075778 | 4.3452496  | 4.33715346 | 4.33051378 | 4.32200924 | 4.31867508 | 0.98509234 |
| 0.59 | 4.20591793 | 4.20315453 | 4.20108026 | 4.19588814 | 4.18825626 | 4.18199708 | 4.17397956 | 4.17083623 | 0.98508985 |
| 0.6  | 4.06110929 | 4.05850609 | 4.05655205 | 4.05166075 | 4.04447079 | 4.03857381 | 4.03101992 | 4.02805826 | 0.98508736 |
| 0.61 | 3.92128637 | 3.91883562 | 3.91699598 | 3.91239097 | 3.90562157 | 3.9000693  | 3.89295668 | 3.89016794 | 0.98508487 |
| 0.62 | 3.78627752 | 3.78397181 | 3.78224102 | 3.77790838 | 3.77153913 | 3.76631485 | 3.75962213 | 3.75699794 | 0.98508239 |
| 0.63 | 3.65591699 | 3.65374923 | 3.65212197 | 3.64804842 | 3.64205983 | 3.63714757 | 3.63085431 | 3.62838667 | 0.9850799  |
| 0.64 | 3.53004473 | 3.52800817 | 3.52647937 | 3.52265221 | 3.51702563 | 3.51241014 | 3.50649682 | 3.50417809 | 0.9850774  |
| 0.65 | 3.40850623 | 3.40659439 | 3.4051592  | 3.4015663  | 3.39628393 | 3.39195062 | 3.3863986  | 3.38422147 | 0.98507491 |
| 0.66 | 3.29115226 | 3.28935898 | 3.28801276 | 3.28464254 | 3.27968737 | 3.27562231 | 3.27041377 | 3.26837125 | 0.98507242 |
| 0.67 | 3.17783876 | 3.17615813 | 3.17489647 | 3.17173786 | 3.16709365 | 3.16328353 | 3.15840144 | 3.15648688 | 0.98506993 |
| 0.68 | 3.06842662 | 3.06685301 | 3.06567168 | 3.06271411 | 3.05836534 | 3.05479745 | 3.05022556 | 3.04843258 | 0.98506744 |
| 0.69 | 2.9627815  | 2.96130955 | 2.96020451 | 2.95743789 | 2.95336974 | 2.95003194 | 2.94575472 | 2.94407725 | 0.98506494 |
| 0.7  | 2.86077372 | 2.85939828 | 2.85836568 | 2.85578038 | 2.8519787  | 2.84885941 | 2.84486203 | 2.84329426 | 0.98506245 |
| 0.71 | 2.76227804 | 2.76099421 | 2.76003038 | 2.7576172  | 2.75406848 | 2.75115664 | 2.74742493 | 2.74596131 | 0.98505996 |
| 0.72 | 2.66717354 | 2.66597665 | 2.66507808 | 2.66282823 | 2.65951958 | 2.65680461 | 2.65332507 | 2.65196031 | 0.98505746 |
| 0.73 | 2.57534346 | 2.57422905 | 2.57339238 | 2.57129749 | 2.56821661 | 2.56568843 | 2.56244816 | 2.5611772  | 0.98505496 |
| 0.74 | 2.48667507 | 2.48563887 | 2.48486091 | 2.48291298 | 2.48004812 | 2.47769712 | 2.47468379 | 2.47350182 | 0.98505247 |
| 0.75 | 2.4010595  | 2.40009745 | 2.39937516 | 2.39756655 | 2.39490651 | 2.3927235  | 2.38992537 | 2.38882777 | 0.98504997 |
| 0.76 | 2.31839166 | 2.31749988 | 2.31683034 | 2.31515379 | 2.31268787 | 2.31066409 | 2.30806995 | 2.30705233 | 0.98504747 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.77 | 2.23857005 | 2.23774485 | 2.23712528 | 2.23557383 | 2.23329184 | 2.23141893 | 2.22901809 | 2.22807627 | 0.98504498 |
| 0.78 | 2.16149668 | 2.16073452 | 2.16016228 | 2.15872932 | 2.15662153 | 2.15489153 | 2.15267377 | 2.15180375 | 0.98504248 |
| 0.79 | 2.08707692 | 2.08637445 | 2.08584702 | 2.08452623 | 2.08258336 | 2.08098866 | 2.07894426 | 2.07814222 | 0.98503998 |
| 0.8  | 2.01521941 | 2.01457343 | 2.01408839 | 2.01287375 | 2.01108697 | 2.00962031 | 2.00774    | 2.00700231 | 0.98503748 |
| 0.81 | 1.94583594 | 1.94524338 | 1.94479845 | 1.94368423 | 1.94204509 | 1.94069958 | 1.9389745  | 1.93829769 | 0.98503498 |
| 0.82 | 1.87884133 | 1.87829927 | 1.87789227 | 1.87687299 | 1.87537346 | 1.87414251 | 1.87256424 | 1.871945   | 0.98503248 |
| 0.83 | 1.81415332 | 1.813659   | 1.81328783 | 1.81235828 | 1.81099072 | 1.80986804 | 1.80842854 | 1.80786373 | 0.98502998 |
| 0.84 | 1.7516925  | 1.75124328 | 1.75090596 | 1.75006117 | 1.74881827 | 1.74779789 | 1.74648949 | 1.74597611 | 0.98502747 |
| 0.85 | 1.69138219 | 1.69097554 | 1.69067019 | 1.68990544 | 1.68878024 | 1.68785646 | 1.68667188 | 1.68620706 | 0.98502497 |
| 0.86 | 1.63314835 | 1.63278187 | 1.63250669 | 1.63181746 | 1.63080336 | 1.62997074 | 1.62890303 | 1.62848405 | 0.98502247 |
| 0.87 | 1.57691949 | 1.5765909  | 1.57634416 | 1.57572617 | 1.57481685 | 1.57407024 | 1.57311277 | 1.57273705 | 0.98501997 |
| 0.88 | 1.52262657 | 1.5223337  | 1.52211377 | 1.52156294 | 1.5207524  | 1.52008687 | 1.51923334 | 1.51889839 | 0.98501746 |
| 0.89 | 1.47020294 | 1.46994371 | 1.46974905 | 1.46926149 | 1.46854402 | 1.46795488 | 1.4671993  | 1.46690277 | 0.98501496 |
| 0.9  | 1.41958424 | 1.41935669 | 1.41918582 | 1.41875782 | 1.41812798 | 1.41761078 | 1.41694742 | 1.41668709 | 0.98501245 |
| 0.91 | 1.37070833 | 1.37051059 | 1.37036209 | 1.36999014 | 1.36944276 | 1.36899325 | 1.36841669 | 1.36819041 | 0.98500994 |
| 0.92 | 1.32351521 | 1.32334549 | 1.32321803 | 1.32289878 | 1.32242893 | 1.32204307 | 1.32154814 | 1.32135389 | 0.98500744 |
| 0.93 | 1.27794693 | 1.27780354 | 1.27769585 | 1.27742611 | 1.27702911 | 1.27670307 | 1.27628485 | 1.27612071 | 0.98500493 |
| 0.94 | 1.23394755 | 1.23382888 | 1.23373975 | 1.23351649 | 1.2331879  | 1.23291803 | 1.23257184 | 1.23243596 | 0.98500242 |
| 0.95 | 1.19146307 | 1.19136757 | 1.19129586 | 1.19111621 | 1.19085179 | 1.19063461 | 1.19035601 | 1.19024665 | 0.98499991 |
| 0.96 | 1.15044131 | 1.15036754 | 1.15031215 | 1.15017337 | 1.1499691  | 1.14980132 | 1.14958607 | 1.14950158 | 0.98499741 |
| 0.97 | 1.11083192 | 1.1107785  | 1.11073838 | 1.11063788 | 1.11048994 | 1.11036842 | 1.11021252 | 1.11015132 | 0.9849949  |
| 0.98 | 1.07258627 | 1.07255188 | 1.07252606 | 1.07246136 | 1.07236612 | 1.07228789 | 1.07218752 | 1.07214812 | 0.98499239 |
| 0.99 | 1.03565741 | 1.03564081 | 1.03562834 | 1.0355971  | 1.03555112 | 1.03551335 | 1.03546488 | 1.03544585 | 0.98498987 |
| 1.01 | 0.96557027 | 0.96558574 | 0.96559737 | 0.96562649 | 0.96566937 | 0.9657046  | 0.9657498  | 0.96576754 | 0.98498485 |
| 1.02 | 0.93232594 | 0.93235583 | 0.93237828 | 0.93243453 | 0.93251734 | 0.93258537 | 0.93267267 | 0.93270695 | 0.98498234 |
| 1.03 | 0.9002262  | 0.9002695  | 0.90030201 | 0.90038348 | 0.90050343 | 0.90060198 | 0.90072845 | 0.9007781  | 0.98497983 |
| 1.04 | 0.86923165 | 0.86928739 | 0.86932925 | 0.86943415 | 0.86958858 | 0.86971547 | 0.86987832 | 0.86994225 | 0.98497731 |
| 1.05 | 0.83930424 | 0.83937151 | 0.83942204 | 0.83954865 | 0.83973506 | 0.83988823 | 0.84008481 | 0.84016199 | 0.9849748  |
| 1.06 | 0.81040721 | 0.81048516 | 0.81054371 | 0.81069042 | 0.81090643 | 0.81108393 | 0.81131174 | 0.81140119 | 0.98497228 |
| 1.07 | 0.78250511 | 0.78259292 | 0.78265888 | 0.78282414 | 0.7830675  | 0.78326748 | 0.78352415 | 0.78362493 | 0.98496977 |
| 1.08 | 0.75556367 | 0.75566057 | 0.75573335 | 0.75591573 | 0.75618431 | 0.75640501 | 0.75668829 | 0.75679953 | 0.98496725 |
| 1.09 | 0.72954981 | 0.72965507 | 0.72973414 | 0.72993226 | 0.73022402 | 0.73046379 | 0.73077156 | 0.73089242 | 0.98496474 |
| 1.1  | 0.7044316  | 0.70454453 | 0.70462936 | 0.70484193 | 0.70515497 | 0.70541224 | 0.70574249 | 0.70587218 | 0.98496222 |
| 1.11 | 0.68017821 | 0.68029816 | 0.68038826 | 0.68061404 | 0.68094656 | 0.68121985 | 0.68157067 | 0.68170844 | 0.9849597  |
| 1.12 | 0.65675985 | 0.6568862  | 0.65698111 | 0.65721895 | 0.65756924 | 0.65785714 | 0.65822673 | 0.65837189 | 0.98495718 |
| 1.13 | 0.63414779 | 0.63427995 | 0.63437923 | 0.63462803 | 0.63499447 | 0.63529567 | 0.63568234 | 0.6358342  | 0.98495466 |
| 1.14 | 0.61231425 | 0.61245168 | 0.61255492 | 0.61281364 | 0.61319472 | 0.61350795 | 0.61391009 | 0.61406803 | 0.98495215 |
| 1.15 | 0.59123243 | 0.59137461 | 0.59148142 | 0.59174909 | 0.59214336 | 0.59246744 | 0.59288354 | 0.59304698 | 0.98494963 |
| 1.16 | 0.57087645 | 0.57102289 | 0.5711329  | 0.5714086  | 0.5718147  | 0.57214854 | 0.57257716 | 0.57274552 | 0.9849471  |
| 1.17 | 0.55122133 | 0.55137156 | 0.55148443 | 0.55176728 | 0.55218395 | 0.55252647 | 0.55296628 | 0.55313904 | 0.98494458 |
| 1.18 | 0.53224292 | 0.53239652 | 0.53251191 | 0.5328011  | 0.53322712 | 0.53357735 | 0.53402707 | 0.53420373 | 0.98494206 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.19 | 0.51391794 | 0.51407449 | 0.5141921  | 0.51448686 | 0.5149211  | 0.5152781  | 0.51573654 | 0.51591662 | 0.98493954 |
| 1.2  | 0.49622388 | 0.496383   | 0.49650254 | 0.49680215 | 0.49724354 | 0.49760643 | 0.49807246 | 0.49825553 | 0.98493702 |
| 1.21 | 0.47913902 | 0.47930035 | 0.47942155 | 0.47972531 | 0.48017286 | 0.48054082 | 0.48101338 | 0.48119902 | 0.98493449 |
| 1.22 | 0.4626424  | 0.46280558 | 0.46292818 | 0.46323547 | 0.46368822 | 0.46406048 | 0.46453857 | 0.4647264  | 0.98493197 |
| 1.23 | 0.44671374 | 0.44687847 | 0.44700224 | 0.44731245 | 0.44776951 | 0.44814534 | 0.44862803 | 0.44881767 | 0.98492944 |
| 1.24 | 0.4313335  | 0.43149948 | 0.43162418 | 0.43193675 | 0.4323973  | 0.43277602 | 0.43326243 | 0.43345354 | 0.98492692 |
| 1.25 | 0.41648281 | 0.41664975 | 0.41677517 | 0.41708957 | 0.41755283 | 0.41793379 | 0.41842311 | 0.41861536 | 0.98492439 |
| 1.26 | 0.40214341 | 0.40231106 | 0.40243701 | 0.40275274 | 0.40321798 | 0.40360058 | 0.40409203 | 0.40428513 | 0.98492187 |
| 1.27 | 0.38829772 | 0.38846582 | 0.38859212 | 0.38890871 | 0.38937526 | 0.38975894 | 0.3902518  | 0.39044546 | 0.98491934 |
| 1.28 | 0.37492873 | 0.37509706 | 0.37522353 | 0.37554056 | 0.37600776 | 0.376392   | 0.3768856  | 0.37707955 | 0.98491681 |
| 1.29 | 0.36202004 | 0.36218837 | 0.36231485 | 0.36263191 | 0.36309918 | 0.36348348 | 0.36397719 | 0.36417119 | 0.98491429 |
| 1.3  | 0.34955578 | 0.34972393 | 0.34985027 | 0.35016698 | 0.35063375 | 0.35101767 | 0.3515109  | 0.35170472 | 0.98491176 |
| 1.31 | 0.33752067 | 0.33768844 | 0.3378145  | 0.33813052 | 0.33859628 | 0.33897938 | 0.33947158 | 0.339665   | 0.98490923 |
| 1.32 | 0.32589992 | 0.32606714 | 0.32619279 | 0.32650778 | 0.32697206 | 0.32735395 | 0.32784461 | 0.32803743 | 0.9849067  |
| 1.33 | 0.31467928 | 0.31484578 | 0.3149709  | 0.31528457 | 0.3157469  | 0.31612721 | 0.31661586 | 0.31680791 | 0.98490417 |
| 1.34 | 0.30384495 | 0.3040106  | 0.30413507 | 0.30444713 | 0.30490711 | 0.3052855  | 0.30577171 | 0.30596279 | 0.98490164 |
| 1.35 | 0.29338365 | 0.2935483  | 0.29367203 | 0.29398222 | 0.29443946 | 0.29481561 | 0.29529896 | 0.29548894 | 0.9848991  |
| 1.36 | 0.28328253 | 0.28344606 | 0.28356894 | 0.28387702 | 0.28433117 | 0.28470479 | 0.28518492 | 0.28537362 | 0.98489657 |
| 1.37 | 0.27352919 | 0.27369147 | 0.27381342 | 0.27411917 | 0.2745699  | 0.27494073 | 0.27541727 | 0.27560458 | 0.98489404 |
| 1.38 | 0.26411165 | 0.26427258 | 0.26439352 | 0.26469673 | 0.26514374 | 0.26551152 | 0.26598418 | 0.26616996 | 0.98489151 |
| 1.39 | 0.25501836 | 0.25517784 | 0.25529768 | 0.25559818 | 0.25604119 | 0.2564057  | 0.25687417 | 0.25705831 | 0.98488897 |
| 1.4  | 0.24623814 | 0.24639608 | 0.24651477 | 0.24681237 | 0.24725114 | 0.24761216 | 0.24807617 | 0.24825857 | 0.98488644 |
| 1.41 | 0.23776023 | 0.23791654 | 0.23803401 | 0.23832857 | 0.23876285 | 0.23912021 | 0.23957952 | 0.23976007 | 0.9848839  |
| 1.42 | 0.22957421 | 0.22972882 | 0.22984502 | 0.23013638 | 0.23056597 | 0.23091948 | 0.23137387 | 0.2315525  | 0.98488137 |
| 1.43 | 0.22167003 | 0.22182288 | 0.22193774 | 0.22222578 | 0.2226505  | 0.22300001 | 0.22344927 | 0.22362589 | 0.98487883 |
| 1.44 | 0.21403799 | 0.21418901 | 0.2143025  | 0.2145871  | 0.21500677 | 0.21535213 | 0.21579608 | 0.21597062 | 0.98487629 |
| 1.45 | 0.20666871 | 0.20681785 | 0.20692993 | 0.20721099 | 0.20762545 | 0.20796654 | 0.20840503 | 0.20857742 | 0.98487376 |
| 1.46 | 0.19955317 | 0.19970037 | 0.199811   | 0.20008842 | 0.20049754 | 0.20083425 | 0.20126711 | 0.2014373  | 0.98487122 |
| 1.47 | 0.1926826  | 0.19282783 | 0.19293697 | 0.19321068 | 0.19361433 | 0.19394656 | 0.19437367 | 0.19454161 | 0.98486868 |
| 1.48 | 0.18604859 | 0.1861918  | 0.18629943 | 0.18656936 | 0.18696743 | 0.18729508 | 0.18771634 | 0.18788197 | 0.98486614 |
| 1.49 | 0.17964299 | 0.17978415 | 0.17989024 | 0.18015631 | 0.18054872 | 0.18087172 | 0.18128701 | 0.18145031 | 0.9848636  |
| 1.5  | 0.17345793 | 0.17359701 | 0.17370155 | 0.17396371 | 0.17435037 | 0.17466865 | 0.1750779  | 0.17523882 | 0.98486106 |
| 1.51 | 0.16748582 | 0.1676228  | 0.16772576 | 0.16798397 | 0.16836481 | 0.16867832 | 0.16908144 | 0.16923996 | 0.98485852 |
| 1.52 | 0.16171933 | 0.16185419 | 0.16195555 | 0.16220977 | 0.16258474 | 0.16289343 | 0.16329037 | 0.16344647 | 0.98485598 |
| 1.53 | 0.15615137 | 0.1562841  | 0.15638385 | 0.15663405 | 0.15700311 | 0.15730693 | 0.15769764 | 0.15785129 | 0.98485344 |
| 1.54 | 0.15077512 | 0.15090569 | 0.15100384 | 0.15124999 | 0.15161309 | 0.15191203 | 0.15229647 | 0.15244765 | 0.9848509  |
| 1.55 | 0.14558397 | 0.14571239 | 0.14580891 | 0.146051   | 0.14640812 | 0.14670215 | 0.14708028 | 0.147229   | 0.98484835 |
| 1.56 | 0.14057156 | 0.1406978  | 0.1407927  | 0.14103071 | 0.14138184 | 0.14167094 | 0.14204275 | 0.14218899 | 0.98484581 |
| 1.57 | 0.13573171 | 0.13585579 | 0.13594906 | 0.13618299 | 0.13652811 | 0.13681228 | 0.13717776 | 0.13732151 | 0.98484326 |
| 1.58 | 0.13105851 | 0.13118042 | 0.13127205 | 0.1315019  | 0.13184101 | 0.13212024 | 0.13247939 | 0.13262066 | 0.98484072 |
| 1.59 | 0.1265462  | 0.12666594 | 0.12675595 | 0.12698172 | 0.12731483 | 0.12758913 | 0.12794195 | 0.12808073 | 0.98483817 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.6  | 0.12218925 | 0.12230683 | 0.12239521 | 0.12261692 | 0.12294403 | 0.12321341 | 0.12355991 | 0.12369621 | 0.98483563 |
| 1.61 | 0.1179823  | 0.11809773 | 0.11818449 | 0.11840214 | 0.11872328 | 0.11898775 | 0.11932796 | 0.11946178 | 0.98483308 |
| 1.62 | 0.1139202  | 0.11403348 | 0.11411864 | 0.11433225 | 0.11464744 | 0.11490702 | 0.11524095 | 0.11537231 | 0.98483053 |
| 1.63 | 0.10999796 | 0.1101091  | 0.11019265 | 0.11040225 | 0.11071152 | 0.11096624 | 0.11129393 | 0.11142283 | 0.98482799 |
| 1.64 | 0.10621076 | 0.10631978 | 0.10640174 | 0.10660733 | 0.10691072 | 0.10716061 | 0.10748209 | 0.10760856 | 0.98482544 |
| 1.65 | 0.10255395 | 0.10266087 | 0.10274124 | 0.10294287 | 0.10324041 | 0.10348549 | 0.1038008  | 0.10392485 | 0.98482289 |
| 1.66 | 0.09902305 | 0.09912787 | 0.09920667 | 0.09940436 | 0.0996961  | 0.09993641 | 0.10024561 | 0.10036725 | 0.98482034 |
| 1.67 | 0.09561371 | 0.09571646 | 0.0957937  | 0.09598748 | 0.09627347 | 0.09650905 | 0.09681217 | 0.09693143 | 0.98481779 |
| 1.68 | 0.09232175 | 0.09242245 | 0.09249814 | 0.09268806 | 0.09296835 | 0.09319924 | 0.09349634 | 0.09361323 | 0.98481524 |
| 1.69 | 0.08914314 | 0.0892418  | 0.08931596 | 0.08950204 | 0.08977668 | 0.09000293 | 0.09029407 | 0.09040862 | 0.98481269 |
| 1.7  | 0.08607397 | 0.08617061 | 0.08624326 | 0.08642554 | 0.08669459 | 0.08691625 | 0.08720148 | 0.08731371 | 0.98481014 |
| 1.71 | 0.08311046 | 0.08320511 | 0.08327626 | 0.08345479 | 0.08371831 | 0.08393542 | 0.08421481 | 0.08432475 | 0.98480758 |
| 1.72 | 0.08024899 | 0.08034167 | 0.08041134 | 0.08058616 | 0.08084421 | 0.08105682 | 0.08133044 | 0.08143811 | 0.98480503 |
| 1.73 | 0.07748604 | 0.07757677 | 0.07764498 | 0.07781613 | 0.07806878 | 0.07827694 | 0.07854485 | 0.07865028 | 0.98480248 |
| 1.74 | 0.07481822 | 0.07490702 | 0.07497379 | 0.07514132 | 0.07538863 | 0.0755924  | 0.07585468 | 0.07595789 | 0.98479992 |
| 1.75 | 0.07224224 | 0.07232915 | 0.07239449 | 0.07255845 | 0.07280049 | 0.07299993 | 0.07325664 | 0.07335766 | 0.98479737 |
| 1.76 | 0.06975496 | 0.06984    | 0.06990393 | 0.07006436 | 0.0703012  | 0.07049637 | 0.07074758 | 0.07084645 | 0.98479481 |
| 1.77 | 0.06735332 | 0.06743651 | 0.06749905 | 0.067656   | 0.06788772 | 0.06807867 | 0.06832446 | 0.0684212  | 0.98479226 |
| 1.78 | 0.06503436 | 0.06511573 | 0.06517691 | 0.06533043 | 0.06555709 | 0.06574388 | 0.06598434 | 0.06607898 | 0.9847897  |
| 1.79 | 0.06279525 | 0.06287482 | 0.06293465 | 0.06308479 | 0.06330648 | 0.06348917 | 0.06372436 | 0.06381693 | 0.98478714 |
| 1.8  | 0.06063322 | 0.06071103 | 0.06076953 | 0.06091635 | 0.06113312 | 0.06131178 | 0.06154179 | 0.06163232 | 0.98478459 |
| 1.81 | 0.05854564 | 0.0586217  | 0.0586789  | 0.05882244 | 0.05903439 | 0.05920907 | 0.05943397 | 0.05952249 | 0.98478203 |
| 1.82 | 0.05652993 | 0.05660428 | 0.05666019 | 0.05680051 | 0.0570077  | 0.05717847 | 0.05739834 | 0.05748489 | 0.98477947 |
| 1.83 | 0.05458362 | 0.05465629 | 0.05471093 | 0.05484807 | 0.05505059 | 0.05521751 | 0.05543244 | 0.05551704 | 0.98477691 |
| 1.84 | 0.05270432 | 0.05277533 | 0.05282873 | 0.05296275 | 0.05316067 | 0.05332381 | 0.05353387 | 0.05361656 | 0.98477435 |
| 1.85 | 0.05088972 | 0.05095911 | 0.05101128 | 0.05114224 | 0.05133563 | 0.05149505 | 0.05170032 | 0.05178113 | 0.98477179 |
| 1.86 | 0.0491376  | 0.04920539 | 0.04925636 | 0.0493843  | 0.04957324 | 0.049729   | 0.04992958 | 0.05000854 | 0.98476923 |
| 1.87 | 0.04744581 | 0.04751202 | 0.04756181 | 0.04768679 | 0.04787136 | 0.04802353 | 0.04821948 | 0.04829662 | 0.98476667 |
| 1.88 | 0.04581226 | 0.04587693 | 0.04592556 | 0.04604763 | 0.04622791 | 0.04637654 | 0.04656795 | 0.04664331 | 0.98476411 |
| 1.89 | 0.04423496 | 0.04429811 | 0.0443456  | 0.04446481 | 0.04464088 | 0.04478604 | 0.04497299 | 0.0450466  | 0.98476154 |
| 1.9  | 0.04271196 | 0.04277362 | 0.04282    | 0.0429364  | 0.04310833 | 0.04325008 | 0.04343265 | 0.04350454 | 0.98475898 |
| 1.91 | 0.0412414  | 0.0413016  | 0.04134688 | 0.04146052 | 0.04162839 | 0.0417668  | 0.04194508 | 0.04201527 | 0.98475642 |
| 1.92 | 0.03982147 | 0.03988024 | 0.03992444 | 0.04003538 | 0.04019926 | 0.04033439 | 0.04050845 | 0.04057699 | 0.98475385 |
| 1.93 | 0.03845042 | 0.03850779 | 0.03855093 | 0.03865922 | 0.0388192  | 0.03895111 | 0.03912103 | 0.03918794 | 0.98475129 |
| 1.94 | 0.03712659 | 0.03718257 | 0.03722468 | 0.03733037 | 0.03748651 | 0.03761527 | 0.03778112 | 0.03784644 | 0.98474872 |
| 1.95 | 0.03584833 | 0.03590296 | 0.03594405 | 0.03604719 | 0.03619957 | 0.03632524 | 0.03648711 | 0.03655086 | 0.98474615 |
| 1.96 | 0.03461408 | 0.03466739 | 0.03470748 | 0.03480812 | 0.03495682 | 0.03507945 | 0.03523742 | 0.03529964 | 0.98474359 |
| 1.97 | 0.03342233 | 0.03347434 | 0.03351345 | 0.03361165 | 0.03375673 | 0.03387638 | 0.03403053 | 0.03409124 | 0.98474102 |
| 1.98 | 0.03222716 | 0.03223234 | 0.0323605  | 0.0324563  | 0.03259784 | 0.03271458 | 0.03286498 | 0.03292421 | 0.98473845 |
| 1.99 | 0.0311605  | 0.03120999 | 0.03124721 | 0.03134066 | 0.03147874 | 0.03159262 | 0.03173935 | 0.03179714 | 0.98473588 |
| 2    | 0.03008765 | 0.03013592 | 0.03017223 | 0.03026337 | 0.03039805 | 0.03050914 | 0.03065227 | 0.03070864 | 0.98473332 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.01 | 0.02905174 | 0.02909882 | 0.02913422 | 0.02922311 | 0.02935447 | 0.02946282 | 0.02960242 | 0.02965741 | 0.98473075 |
| 2.02 | 0.0280515  | 0.0280974  | 0.02813193 | 0.02821861 | 0.02834671 | 0.02845238 | 0.02858853 | 0.02864217 | 0.98472818 |
| 2.03 | 0.02708569 | 0.02713045 | 0.02716412 | 0.02724864 | 0.02737355 | 0.02747659 | 0.02760937 | 0.02766167 | 0.9847256  |
| 2.04 | 0.02615314 | 0.02619678 | 0.0262296  | 0.02631201 | 0.0264338  | 0.02653427 | 0.02666374 | 0.02671475 | 0.98472303 |
| 2.05 | 0.02525269 | 0.02529524 | 0.02532723 | 0.02540757 | 0.02552631 | 0.02562427 | 0.02575051 | 0.02580024 | 0.98472046 |
| 2.06 | 0.02438325 | 0.02442472 | 0.02445591 | 0.02453423 | 0.02464998 | 0.02474547 | 0.02486855 | 0.02491703 | 0.98471789 |
| 2.07 | 0.02354374 | 0.02358416 | 0.02361456 | 0.0236909  | 0.02380373 | 0.02389682 | 0.02401679 | 0.02406406 | 0.98471532 |
| 2.08 | 0.02273314 | 0.02277253 | 0.02280216 | 0.02287656 | 0.02298653 | 0.02307726 | 0.02319421 | 0.02324029 | 0.98471274 |
| 2.09 | 0.02195044 | 0.02198883 | 0.0220177  | 0.02209021 | 0.02219739 | 0.02228582 | 0.02239981 | 0.02244472 | 0.98471017 |
| 2.1  | 0.02119469 | 0.0212321  | 0.02126024 | 0.02133089 | 0.02143534 | 0.02152152 | 0.02163261 | 0.02167638 | 0.98470759 |
| 2.11 | 0.02046497 | 0.02050141 | 0.02052883 | 0.02059768 | 0.02069945 | 0.02078343 | 0.02089169 | 0.02093434 | 0.98470502 |
| 2.12 | 0.01976036 | 0.01979587 | 0.01982258 | 0.01988966 | 0.01998882 | 0.02007065 | 0.02017614 | 0.02021771 | 0.98470244 |
| 2.13 | 0.01908002 | 0.01911461 | 0.01914063 | 0.01920598 | 0.01930259 | 0.01938232 | 0.01948511 | 0.01952561 | 0.98469986 |
| 2.14 | 0.0184231  | 0.0184568  | 0.01848215 | 0.01854581 | 0.01863992 | 0.0187176  | 0.01881774 | 0.0188572  | 0.98469729 |
| 2.15 | 0.0177888  | 0.01782162 | 0.01784631 | 0.01790832 | 0.018      | 0.01807567 | 0.01817323 | 0.01821167 | 0.98469471 |
| 2.16 | 0.01717633 | 0.0172083  | 0.01723235 | 0.01729275 | 0.01738205 | 0.01745576 | 0.01755079 | 0.01758824 | 0.98469213 |
| 2.17 | 0.01658496 | 0.01661609 | 0.01663951 | 0.01669834 | 0.01678532 | 0.01685711 | 0.01694967 | 0.01698615 | 0.98468955 |
| 2.18 | 0.01601394 | 0.01604426 | 0.01606707 | 0.01612436 | 0.01620907 | 0.01627899 | 0.01636914 | 0.01640467 | 0.98468697 |
| 2.19 | 0.01546258 | 0.01549211 | 0.01551432 | 0.01557011 | 0.0156526  | 0.01572069 | 0.0158085  | 0.0158431  | 0.98468439 |
| 2.2  | 0.01493021 | 0.01495896 | 0.01498059 | 0.01503491 | 0.01511523 | 0.01518154 | 0.01526705 | 0.01530075 | 0.98468181 |
| 2.21 | 0.01441617 | 0.01444416 | 0.01446522 | 0.01451811 | 0.01459632 | 0.01466089 | 0.01474415 | 0.01477697 | 0.98467923 |
| 2.22 | 0.01391982 | 0.01394707 | 0.01396757 | 0.01401907 | 0.01409522 | 0.01415809 | 0.01423916 | 0.01427112 | 0.98467665 |
| 2.23 | 0.01344057 | 0.0134671  | 0.01348705 | 0.01353718 | 0.01361132 | 0.01367253 | 0.01375147 | 0.01378258 | 0.98467407 |
| 2.24 | 0.01297781 | 0.01300364 | 0.01302306 | 0.01307186 | 0.01314404 | 0.01320362 | 0.01328048 | 0.01331077 | 0.98467148 |
| 2.25 | 0.01253099 | 0.01255612 | 0.01257504 | 0.01262254 | 0.01269279 | 0.0127508  | 0.01282562 | 0.01285511 | 0.9846689  |
| 2.26 | 0.01209955 | 0.01212401 | 0.01214242 | 0.01218866 | 0.01225704 | 0.01231351 | 0.01238634 | 0.01241505 | 0.98466632 |
| 2.27 | 0.01168297 | 0.01170678 | 0.01172469 | 0.01176969 | 0.01183625 | 0.01189121 | 0.0119621  | 0.01199005 | 0.98466373 |
| 2.28 | 0.01128073 | 0.0113039  | 0.01132133 | 0.01136512 | 0.0114299  | 0.0114834  | 0.0115524  | 0.0115796  | 0.98466115 |
| 2.29 | 0.01089233 | 0.01091488 | 0.01093185 | 0.01097446 | 0.01103751 | 0.01108957 | 0.01115673 | 0.0111832  | 0.98465856 |
| 2.3  | 0.01051731 | 0.01053925 | 0.01055576 | 0.01059723 | 0.01065858 | 0.01070925 | 0.01077461 | 0.01080037 | 0.98465597 |
| 2.31 | 0.0101552  | 0.01017655 | 0.01019262 | 0.01023297 | 0.01029267 | 0.01034197 | 0.01040557 | 0.01043065 | 0.98465339 |
| 2.32 | 0.00980556 | 0.00982633 | 0.00984196 | 0.00988123 | 0.00993931 | 0.00998729 | 0.01004918 | 0.01007358 | 0.9846508  |
| 2.33 | 0.00946796 | 0.00948817 | 0.00950337 | 0.00954157 | 0.00959809 | 0.00964477 | 0.00970499 | 0.00972874 | 0.98464821 |
| 2.34 | 0.00914198 | 0.00916164 | 0.00917643 | 0.0092136  | 0.00926858 | 0.009314   | 0.0093726  | 0.0093957  | 0.98464562 |
| 2.35 | 0.00882723 | 0.00884635 | 0.00886074 | 0.00889689 | 0.00895039 | 0.00899457 | 0.00905158 | 0.00907406 | 0.98464303 |
| 2.36 | 0.00852331 | 0.00854191 | 0.00855591 | 0.00859108 | 0.00864311 | 0.0086861  | 0.00874156 | 0.00876344 | 0.98464044 |
| 2.37 | 0.00822985 | 0.00824795 | 0.00826156 | 0.00829577 | 0.00834639 | 0.0083882  | 0.00844216 | 0.00846344 | 0.98463785 |
| 2.38 | 0.0079465  | 0.0079641  | 0.00797734 | 0.00801062 | 0.00805985 | 0.00810053 | 0.00815302 | 0.00817372 | 0.98463526 |
| 2.39 | 0.0076729  | 0.00769002 | 0.0077029  | 0.00773526 | 0.00778315 | 0.00782272 | 0.00787378 | 0.00789391 | 0.98463267 |
| 2.4  | 0.00740873 | 0.00742537 | 0.0074379  | 0.00746937 | 0.00751595 | 0.00755443 | 0.0076041  | 0.00762368 | 0.98463008 |
| 2.41 | 0.00715365 | 0.00716983 | 0.00718202 | 0.00721263 | 0.00725793 | 0.00729535 | 0.00734366 | 0.00736271 | 0.98462748 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.42 | 0.00690735 | 0.00692309 | 0.00693494 | 0.0069647  | 0.00700876 | 0.00704515 | 0.00709213 | 0.00711066 | 0.98462489 |
| 2.43 | 0.00666953 | 0.00668484 | 0.00669636 | 0.0067253  | 0.00676814 | 0.00680354 | 0.00684923 | 0.00686725 | 0.9846223  |
| 2.44 | 0.0064399  | 0.00645478 | 0.00646598 | 0.00649413 | 0.00653579 | 0.00657021 | 0.00661464 | 0.00663217 | 0.9846197  |
| 2.45 | 0.00621818 | 0.00623265 | 0.00624354 | 0.0062709  | 0.00631141 | 0.00634488 | 0.00638809 | 0.00640513 | 0.98461711 |
| 2.46 | 0.00600409 | 0.00601815 | 0.00602874 | 0.00605535 | 0.00609473 | 0.00612728 | 0.00616929 | 0.00618587 | 0.98461451 |
| 2.47 | 0.00579737 | 0.00581104 | 0.00582134 | 0.00584721 | 0.0058855  | 0.00591714 | 0.00595799 | 0.00597411 | 0.98461192 |
| 2.48 | 0.00559777 | 0.00561106 | 0.00562107 | 0.00564622 | 0.00568345 | 0.00571421 | 0.00575393 | 0.0057696  | 0.98460932 |
| 2.49 | 0.00540504 | 0.00541796 | 0.00542769 | 0.00545214 | 0.00548833 | 0.00551824 | 0.00555686 | 0.00557209 | 0.98460672 |
| 2.5  | 0.00521894 | 0.00523151 | 0.00524096 | 0.00526473 | 0.00529991 | 0.00532899 | 0.00536653 | 0.00538135 | 0.98460412 |
| 2.51 | 0.00503926 | 0.00505147 | 0.00506066 | 0.00508376 | 0.00511796 | 0.00514623 | 0.00518273 | 0.00519713 | 0.98460152 |
| 2.52 | 0.00486575 | 0.00487763 | 0.00488656 | 0.00490901 | 0.00494226 | 0.00496974 | 0.00500522 | 0.00501922 | 0.98459893 |
| 2.53 | 0.00469823 | 0.00470977 | 0.00471845 | 0.00474027 | 0.00477259 | 0.0047993  | 0.00483379 | 0.0048474  | 0.98459633 |
| 2.54 | 0.00453647 | 0.00454768 | 0.00455612 | 0.00457733 | 0.00460874 | 0.00463471 | 0.00466823 | 0.00468146 | 0.98459373 |
| 2.55 | 0.00438028 | 0.00439118 | 0.00439938 | 0.00442    | 0.00445052 | 0.00447576 | 0.00450834 | 0.0045212  | 0.98459112 |
| 2.56 | 0.00422947 | 0.00424006 | 0.00424803 | 0.00426806 | 0.00429773 | 0.00432226 | 0.00435393 | 0.00436643 | 0.98458852 |
| 2.57 | 0.00408385 | 0.00409414 | 0.00410189 | 0.00412136 | 0.00415019 | 0.00417402 | 0.00420481 | 0.00421696 | 0.98458592 |
| 2.58 | 0.00394324 | 0.00395324 | 0.00396077 | 0.00397969 | 0.00400771 | 0.00403087 | 0.00406079 | 0.0040726  | 0.98458332 |
| 2.59 | 0.00380748 | 0.0038172  | 0.00382451 | 0.0038429  | 0.00387012 | 0.00389263 | 0.00392171 | 0.00393319 | 0.98458072 |
| 2.6  | 0.00367639 | 0.00368583 | 0.00369294 | 0.0037108  | 0.00373726 | 0.00375913 | 0.00378739 | 0.00379854 | 0.98457811 |
| 2.61 | 0.00354981 | 0.00355898 | 0.00356589 | 0.00358325 | 0.00360896 | 0.00363021 | 0.00365767 | 0.00366851 | 0.98457551 |
| 2.62 | 0.00342759 | 0.0034365  | 0.00344321 | 0.00346008 | 0.00348506 | 0.00350571 | 0.0035324  | 0.00354293 | 0.9845729  |
| 2.63 | 0.00330958 | 0.00331824 | 0.00332476 | 0.00334114 | 0.00336541 | 0.00338548 | 0.00341141 | 0.00342164 | 0.9845703  |
| 2.64 | 0.00319563 | 0.00320404 | 0.00321038 | 0.0032263  | 0.00324988 | 0.00326938 | 0.00329457 | 0.00330451 | 0.98456769 |
| 2.65 | 0.00308561 | 0.00309378 | 0.00309993 | 0.0031154  | 0.00313831 | 0.00315725 | 0.00318173 | 0.00319139 | 0.98456508 |
| 2.66 | 0.00297937 | 0.00298731 | 0.00299329 | 0.00300831 | 0.00303057 | 0.00304897 | 0.00307276 | 0.00308214 | 0.98456248 |
| 2.67 | 0.00287679 | 0.0028845  | 0.00289031 | 0.0029049  | 0.00292653 | 0.00294441 | 0.00296751 | 0.00297663 | 0.98455987 |
| 2.68 | 0.00277774 | 0.00278524 | 0.00279087 | 0.00280505 | 0.00282606 | 0.00284343 | 0.00286587 | 0.00287474 | 0.98455726 |
| 2.69 | 0.00268211 | 0.00268938 | 0.00269486 | 0.00270863 | 0.00272904 | 0.00274591 | 0.00276772 | 0.00277633 | 0.98455465 |
| 2.7  | 0.00258976 | 0.00259683 | 0.00260215 | 0.00261553 | 0.00263535 | 0.00265174 | 0.00267292 | 0.00268129 | 0.98455204 |
| 2.71 | 0.0025006  | 0.00250746 | 0.00251263 | 0.00252562 | 0.00254487 | 0.0025608  | 0.00258138 | 0.0025895  | 0.98454943 |
| 2.72 | 0.0024145  | 0.00242117 | 0.00242619 | 0.00243881 | 0.00245751 | 0.00247297 | 0.00249296 | 0.00250085 | 0.98454682 |
| 2.73 | 0.00233137 | 0.00233785 | 0.00234272 | 0.00235498 | 0.00237314 | 0.00238816 | 0.00240758 | 0.00241524 | 0.98454421 |
| 2.74 | 0.0022511  | 0.00225739 | 0.00226213 | 0.00227403 | 0.00229167 | 0.00230626 | 0.00232512 | 0.00233256 | 0.9845416  |
| 2.75 | 0.0021736  | 0.00217971 | 0.0021843  | 0.00219586 | 0.00221299 | 0.00222717 | 0.00224548 | 0.00225271 | 0.98453899 |
| 2.76 | 0.00209876 | 0.00210469 | 0.00210916 | 0.00212038 | 0.00213702 | 0.00215078 | 0.00216857 | 0.0021756  | 0.98453637 |
| 2.77 | 0.0020265  | 0.00203226 | 0.0020366  | 0.0020475  | 0.00206365 | 0.00207702 | 0.0020943  | 0.00210112 | 0.98453376 |
| 2.78 | 0.00195673 | 0.00196232 | 0.00196653 | 0.00197712 | 0.00199281 | 0.00200579 | 0.00202257 | 0.0020292  | 0.98453115 |
| 2.79 | 0.00188936 | 0.00189479 | 0.00189888 | 0.00190916 | 0.00192439 | 0.001937   | 0.0019533  | 0.00195973 | 0.98452853 |
| 2.8  | 0.00182431 | 0.00182958 | 0.00183355 | 0.00184353 | 0.00185833 | 0.00187057 | 0.0018864  | 0.00189264 | 0.98452592 |
| 2.81 | 0.0017615  | 0.00176662 | 0.00177047 | 0.00178017 | 0.00179453 | 0.00180642 | 0.00182179 | 0.00182786 | 0.9845233  |
| 2.82 | 0.00170085 | 0.00170582 | 0.00170956 | 0.00171897 | 0.00173292 | 0.00174447 | 0.00175939 | 0.00176528 | 0.98452068 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.83 | 0.00164229 | 0.00164712 | 0.00165075 | 0.00165989 | 0.00167343 | 0.00168464 | 0.00169913 | 0.00170485 | 0.98451807 |
| 2.84 | 0.00158575 | 0.00159043 | 0.00159396 | 0.00160283 | 0.00161598 | 0.00162686 | 0.00164093 | 0.00164649 | 0.98451545 |
| 2.85 | 0.00153115 | 0.0015357  | 0.00153912 | 0.00154774 | 0.0015605  | 0.00157107 | 0.00158473 | 0.00159013 | 0.98451283 |
| 2.86 | 0.00147844 | 0.00148285 | 0.00148617 | 0.00149454 | 0.00150693 | 0.00151719 | 0.00153045 | 0.00153569 | 0.98451021 |
| 2.87 | 0.00142753 | 0.00143182 | 0.00143505 | 0.00144316 | 0.0014552  | 0.00146516 | 0.00147804 | 0.00148312 | 0.98450759 |
| 2.88 | 0.00137838 | 0.00138254 | 0.00138568 | 0.00139356 | 0.00140524 | 0.00141491 | 0.00142741 | 0.00143235 | 0.98450497 |
| 2.89 | 0.00133093 | 0.00133496 | 0.00133801 | 0.00134565 | 0.001357   | 0.00136638 | 0.00137852 | 0.00138332 | 0.98450235 |
| 2.9  | 0.0012851  | 0.00128902 | 0.00129197 | 0.0012994  | 0.00131041 | 0.00131952 | 0.00133131 | 0.00133597 | 0.98449973 |
| 2.91 | 0.00124086 | 0.00124466 | 0.00124753 | 0.00125474 | 0.00126542 | 0.00127427 | 0.00128571 | 0.00129023 | 0.98449711 |
| 2.92 | 0.00119813 | 0.00120183 | 0.00120461 | 0.00121161 | 0.00122198 | 0.00123057 | 0.00124168 | 0.00124606 | 0.98449449 |
| 2.93 | 0.00115688 | 0.00116047 | 0.00116317 | 0.00116996 | 0.00118003 | 0.00118836 | 0.00119915 | 0.00120341 | 0.98449186 |
| 2.94 | 0.00111705 | 0.00112053 | 0.00112315 | 0.00112974 | 0.00113952 | 0.00114761 | 0.00115808 | 0.00116221 | 0.98448924 |
| 2.95 | 0.00107859 | 0.00108197 | 0.00108451 | 0.00109091 | 0.0011004  | 0.00110825 | 0.00111841 | 0.00112243 | 0.98448662 |
| 2.96 | 0.00104146 | 0.00104473 | 0.0010472  | 0.00105341 | 0.00106262 | 0.00107024 | 0.00108011 | 0.001084   | 0.98448399 |
| 2.97 | 0.0010056  | 0.00100878 | 0.00101118 | 0.0010172  | 0.00102614 | 0.00103354 | 0.00104311 | 0.0010469  | 0.98448137 |
| 2.98 | 0.00097098 | 0.00097406 | 0.00097639 | 0.00098224 | 0.00099091 | 0.00099809 | 0.00100739 | 0.00101106 | 0.98447874 |
| 2.99 | 0.00093755 | 0.00094054 | 0.0009428  | 0.00094847 | 0.00095689 | 0.00096386 | 0.00097288 | 0.00097645 | 0.98447612 |
| 3    | 0.00090527 | 0.00090817 | 0.00091036 | 0.00091587 | 0.00092404 | 0.00093081 | 0.00093956 | 0.00094302 | 0.98447349 |
| 3.01 | 0.0008741  | 0.00087692 | 0.00087904 | 0.00088439 | 0.00089232 | 0.00089889 | 0.00090738 | 0.00091074 | 0.98447086 |
| 3.02 | 0.000844   | 0.00084674 | 0.0008488  | 0.00085399 | 0.00086168 | 0.00086806 | 0.0008763  | 0.00087956 | 0.98446823 |
| 3.03 | 0.00081494 | 0.0008176  | 0.0008196  | 0.00082464 | 0.0008321  | 0.00083829 | 0.00084629 | 0.00084945 | 0.9844656  |
| 3.04 | 0.00078689 | 0.00078946 | 0.00079141 | 0.00079629 | 0.00080354 | 0.00080954 | 0.0008173  | 0.00082037 | 0.98446298 |
| 3.05 | 0.00075979 | 0.0007623  | 0.00076418 | 0.00076892 | 0.00077595 | 0.00078177 | 0.00078931 | 0.00079229 | 0.98446035 |
| 3.06 | 0.00073363 | 0.00073606 | 0.00073789 | 0.00074249 | 0.00074931 | 0.00075496 | 0.00076228 | 0.00076517 | 0.98445772 |
| 3.07 | 0.00070838 | 0.00071073 | 0.0007125  | 0.00071697 | 0.00072359 | 0.00072907 | 0.00073617 | 0.00073897 | 0.98445508 |
| 3.08 | 0.00068399 | 0.00068627 | 0.00068799 | 0.00069232 | 0.00069875 | 0.00070407 | 0.00071096 | 0.00071368 | 0.98445245 |
| 3.09 | 0.00066044 | 0.00066265 | 0.00066432 | 0.00066852 | 0.00067476 | 0.00067992 | 0.0006866  | 0.00068925 | 0.98444982 |
| 3.1  | 0.0006377  | 0.00063985 | 0.00064147 | 0.00064554 | 0.00065159 | 0.0006566  | 0.00066309 | 0.00066565 | 0.98444719 |
| 3.11 | 0.00061574 | 0.00061783 | 0.0006194  | 0.00062336 | 0.00062922 | 0.00063408 | 0.00064038 | 0.00064287 | 0.98444456 |
| 3.12 | 0.00059454 | 0.00059657 | 0.00059809 | 0.00060193 | 0.00060762 | 0.00061234 | 0.00061844 | 0.00062086 | 0.98444192 |
| 3.13 | 0.00057407 | 0.00057604 | 0.00057752 | 0.00058124 | 0.00058676 | 0.00059134 | 0.00059726 | 0.0005996  | 0.98443929 |
| 3.14 | 0.00055431 | 0.00055621 | 0.00055765 | 0.00056126 | 0.00056662 | 0.00057106 | 0.00057681 | 0.00057908 | 0.98443665 |
| 3.15 | 0.00053522 | 0.00053707 | 0.00053846 | 0.00054197 | 0.00054717 | 0.00055147 | 0.00055705 | 0.00055926 | 0.98443402 |
| 3.16 | 0.0005168  | 0.00051859 | 0.00051994 | 0.00052334 | 0.00052838 | 0.00053256 | 0.00053797 | 0.00054011 | 0.98443138 |
| 3.17 | 0.000499   | 0.00050074 | 0.00050205 | 0.00050535 | 0.00051024 | 0.0005143  | 0.00051955 | 0.00052162 | 0.98442874 |
| 3.18 | 0.00048182 | 0.00048351 | 0.00048478 | 0.00048798 | 0.00049272 | 0.00049666 | 0.00050175 | 0.00050377 | 0.98442611 |
| 3.19 | 0.00046523 | 0.00046687 | 0.0004681  | 0.0004712  | 0.00047581 | 0.00047962 | 0.00048457 | 0.00048652 | 0.98442347 |
| 3.2  | 0.00044922 | 0.0004508  | 0.000452   | 0.00045501 | 0.00045947 | 0.00046318 | 0.00046797 | 0.00046987 | 0.98442083 |
| 3.21 | 0.00043375 | 0.00043529 | 0.00043645 | 0.00043937 | 0.0004437  | 0.00044729 | 0.00045194 | 0.00045378 | 0.98441819 |
| 3.22 | 0.00041881 | 0.00042031 | 0.00042143 | 0.00042426 | 0.00042847 | 0.00043195 | 0.00043646 | 0.00043825 | 0.98441555 |
| 3.23 | 0.0004044  | 0.00040584 | 0.00040693 | 0.00040968 | 0.00041376 | 0.00041714 | 0.00042151 | 0.00042324 | 0.98441291 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 3.24 | 0.00039047 | 0.00039188 | 0.00039293 | 0.0003956  | 0.00039955 | 0.00040283 | 0.00040708 | 0.00040876 | 0.98441027 |
| 3.25 | 0.00037703 | 0.00037839 | 0.00037942 | 0.000382   | 0.00038584 | 0.00038902 | 0.00039313 | 0.00039476 | 0.98440763 |
| 3.26 | 0.00036405 | 0.00036537 | 0.00036636 | 0.00036887 | 0.00037259 | 0.00037567 | 0.00037967 | 0.00038125 | 0.98440499 |
| 3.27 | 0.00035151 | 0.00035279 | 0.00035376 | 0.00035619 | 0.0003598  | 0.00036279 | 0.00036667 | 0.0003682  | 0.98440235 |
| 3.28 | 0.00033941 | 0.00034065 | 0.00034159 | 0.00034395 | 0.00034745 | 0.00035035 | 0.00035411 | 0.00035559 | 0.9843997  |
| 3.29 | 0.00032772 | 0.00032893 | 0.00032984 | 0.00033212 | 0.00033552 | 0.00033833 | 0.00034198 | 0.00034342 | 0.98439706 |
| 3.3  | 0.00031644 | 0.00031761 | 0.00031849 | 0.00032071 | 0.000324   | 0.00032673 | 0.00033027 | 0.00033166 | 0.98439442 |
| 3.31 | 0.00030555 | 0.00030668 | 0.00030753 | 0.00030968 | 0.00031288 | 0.00031552 | 0.00031895 | 0.00032031 | 0.98439177 |
| 3.32 | 0.00029503 | 0.00029613 | 0.00029695 | 0.00029904 | 0.00030214 | 0.0003047  | 0.00030803 | 0.00030935 | 0.98438913 |
| 3.33 | 0.00028487 | 0.00028593 | 0.00028674 | 0.00028876 | 0.00029176 | 0.00029425 | 0.00029748 | 0.00029876 | 0.98438648 |
| 3.34 | 0.00027506 | 0.00027609 | 0.00027687 | 0.00027883 | 0.00028175 | 0.00028416 | 0.00028729 | 0.00028853 | 0.98438383 |
| 3.35 | 0.00026559 | 0.00026659 | 0.00026735 | 0.00026925 | 0.00027207 | 0.00027442 | 0.00027745 | 0.00027865 | 0.98438119 |
| 3.36 | 0.00025645 | 0.00025742 | 0.00025815 | 0.00025999 | 0.00026273 | 0.00026501 | 0.00026795 | 0.00026911 | 0.98437854 |
| 3.37 | 0.00024762 | 0.00024856 | 0.00024927 | 0.00025106 | 0.00025371 | 0.00025592 | 0.00025877 | 0.0002599  | 0.98437589 |
| 3.38 | 0.00023909 | 0.00024001 | 0.00024069 | 0.00024243 | 0.000245   | 0.00024714 | 0.00024991 | 0.000251   | 0.98437324 |
| 3.39 | 0.00023086 | 0.00023175 | 0.00023241 | 0.0002341  | 0.00023659 | 0.00023866 | 0.00024135 | 0.00024241 | 0.98437059 |
| 3.4  | 0.00022291 | 0.00022377 | 0.00022442 | 0.00022605 | 0.00022847 | 0.00023048 | 0.00023308 | 0.00023411 | 0.98436794 |
| 3.41 | 0.00021524 | 0.00021607 | 0.0002167  | 0.00021828 | 0.00022063 | 0.00022257 | 0.0002251  | 0.0002261  | 0.98436529 |
| 3.42 | 0.00020783 | 0.00020863 | 0.00020924 | 0.00021078 | 0.00021305 | 0.00021494 | 0.00021739 | 0.00021836 | 0.98436264 |
| 3.43 | 0.00020067 | 0.00020145 | 0.00020204 | 0.00020353 | 0.00020574 | 0.00020757 | 0.00020994 | 0.00021088 | 0.98435999 |
| 3.44 | 0.00019376 | 0.00019452 | 0.00019509 | 0.00019653 | 0.00019868 | 0.00020045 | 0.00020275 | 0.00020366 | 0.98435734 |
| 3.45 | 0.00018709 | 0.00018783 | 0.00018838 | 0.00018978 | 0.00019185 | 0.00019358 | 0.00019581 | 0.00019669 | 0.98435468 |
| 3.46 | 0.00018065 | 0.00018136 | 0.0001819  | 0.00018326 | 0.00018527 | 0.00018694 | 0.0001891  | 0.00018996 | 0.98435203 |
| 3.47 | 0.00017443 | 0.00017512 | 0.00017564 | 0.00017696 | 0.00017891 | 0.00018053 | 0.00018263 | 0.00018346 | 0.98434938 |
| 3.48 | 0.00016842 | 0.00016909 | 0.0001696  | 0.00017087 | 0.00017277 | 0.00017434 | 0.00017637 | 0.00017718 | 0.98434672 |
| 3.49 | 0.00016262 | 0.00016328 | 0.00016377 | 0.000165   | 0.00016683 | 0.00016836 | 0.00017033 | 0.00017111 | 0.98434407 |
| 3.5  | 0.00015703 | 0.00015766 | 0.00015813 | 0.00015933 | 0.00016111 | 0.00016258 | 0.0001645  | 0.00016525 | 0.98434141 |

Tabla 35 Multiorden para  $0 \geq n \geq 3.5$ ;  $n \neq 1$  a  $60^{\circ}$  C. Análisis completo.

| t (s)        | 0                         | 21600      | 86400      | 108000     | 172800     | 194400     | 259200     | 280800     | r |            |
|--------------|---------------------------|------------|------------|------------|------------|------------|------------|------------|---|------------|
| Experimental | 31.2704869                | 30.9138059 | 30.1951202 | 30.1019573 | 29.4165442 | 28.9108024 | 27.6198301 | 27.3137233 |   |            |
| n            | C <sup>Λ</sup> (1-n)(ppm) |            |            |            |            |            |            |            |   |            |
| 0            | 31.27                     | 30.91      | 30.20      | 30.10      | 29.42      | 28.91      | 27.62      | 27.31      |   | 0.98717408 |
| 0.01         | 30.21                     | 29.87      | 29.18      | 29.09      | 28.44      | 27.95      | 26.72      | 26.43      |   | 0.98714717 |
| 0.02         | 29.19                     | 28.86      | 28.21      | 28.12      | 27.49      | 27.03      | 25.85      | 25.57      |   | 0.98712022 |
| 0.03         | 28.2020452                | 27.8899606 | 27.260804  | 27.179214  | 26.5787102 | 26.1353513 | 25.002554  | 24.7337222 |   | 0.98709324 |
| 0.04         | 27.2476629                | 26.9492309 | 26.3474927 | 26.2694479 | 25.6949623 | 25.2707272 | 24.1864519 | 23.9290617 |   | 0.98706622 |
| 0.05         | 26.3255777                | 26.0402321 | 25.4647798 | 25.3901343 | 24.8405992 | 24.4347072 | 23.3969881 | 23.1505792 |   | 0.98703917 |
| 0.06         | 25.4346968                | 25.1618939 | 24.6116402 | 24.5402539 | 24.0146439 | 23.6263448 | 22.6332929 | 22.397423  |   | 0.98701208 |



|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.07 | 24.573964  | 24.313182  | 23.7870831 | 23.7188213 | 23.2161518 | 22.8447251 | 21.8945253 | 21.6687691 | 0.98698496 |
| 0.08 | 23.7423592 | 23.4930973 | 22.9901509 | 22.9248845 | 22.4442098 | 22.0889633 | 21.1798716 | 20.9638205 | 0.9869578  |
| 0.09 | 22.9388967 | 22.700674  | 22.2199181 | 22.157523  | 21.6979349 | 21.3582041 | 20.4885448 | 20.281806  | 0.9869306  |
| 0.1  | 22.162624  | 21.9349792 | 21.4754903 | 21.4158473 | 20.9764739 | 20.6516203 | 19.8197834 | 19.6219794 | 0.98690338 |
| 0.11 | 21.4126211 | 21.1951114 | 20.7560027 | 20.6989976 | 20.2790016 | 19.9684121 | 19.1728508 | 18.9836189 | 0.98687611 |
| 0.12 | 20.687999  | 20.4801993 | 20.06062   | 20.0061429 | 19.6047204 | 19.3078061 | 18.5470346 | 18.3660261 | 0.98684881 |
| 0.13 | 19.9878987 | 19.7894012 | 19.3885345 | 19.3364801 | 18.9528592 | 18.6690547 | 17.9416456 | 17.7685254 | 0.98682148 |
| 0.14 | 19.3114904 | 19.1219038 | 18.7389657 | 18.6892327 | 18.3226725 | 18.0514347 | 17.3560168 | 17.1904632 | 0.98679411 |
| 0.15 | 18.6579724 | 18.4769211 | 18.1111592 | 18.0636506 | 17.7134397 | 17.4542473 | 16.7895035 | 16.631207  | 0.98676671 |
| 0.16 | 18.02657   | 17.8536937 | 17.504386  | 17.4590086 | 17.124464  | 16.8768163 | 16.2414815 | 16.0901451 | 0.98673927 |
| 0.17 | 17.4165349 | 17.2514878 | 16.9179413 | 16.8746056 | 16.5550719 | 16.3184882 | 15.7113474 | 15.5666855 | 0.9867118  |
| 0.18 | 16.8271438 | 16.6695943 | 16.3511441 | 16.3097642 | 16.0046121 | 15.778631  | 15.1985173 | 15.0602556 | 0.98668429 |
| 0.19 | 16.2576983 | 16.1073281 | 15.8033362 | 15.7638297 | 15.4724553 | 15.2566337 | 14.7024264 | 14.5703013 | 0.98665675 |
| 0.2  | 15.7075234 | 15.5640272 | 15.2738813 | 15.2361692 | 14.9579928 | 14.7519053 | 14.2225282 | 14.0962867 | 0.98662917 |
| 0.21 | 15.1759668 | 15.0390518 | 14.7621646 | 14.7261711 | 14.4606363 | 14.2638747 | 13.7582942 | 13.6376932 | 0.98660155 |
| 0.22 | 14.6623986 | 14.5317839 | 14.2675918 | 14.233244  | 13.979817  | 13.7919894 | 13.3092132 | 13.194019  | 0.98657391 |
| 0.23 | 14.16621   | 14.0416261 | 13.7895885 | 13.7568166 | 13.5149851 | 13.3357152 | 12.8747906 | 12.7647789 | 0.98654622 |
| 0.24 | 13.6868128 | 13.5680014 | 13.3275997 | 13.2963365 | 13.0656089 | 12.8945358 | 12.4545478 | 12.3495032 | 0.98651851 |
| 0.25 | 13.2236389 | 13.1103521 | 12.8810888 | 12.8512701 | 12.6311746 | 12.4679517 | 12.048022  | 11.9477377 | 0.98649076 |
| 0.26 | 12.7761392 | 12.6681393 | 12.4495371 | 12.4211013 | 12.2111853 | 12.05548   | 11.6547656 | 11.5590428 | 0.98646297 |
| 0.27 | 12.3437833 | 12.2408424 | 12.0324437 | 12.0053315 | 11.8051607 | 11.656654  | 11.2743453 | 11.1829932 | 0.98643515 |
| 0.28 | 11.9260587 | 11.8279582 | 11.629324  | 11.6034787 | 11.4126366 | 11.2710222 | 10.9063423 | 10.8191777 | 0.98640729 |
| 0.29 | 11.5224703 | 11.4290006 | 11.2397099 | 11.2150771 | 11.033164  | 10.8981481 | 10.5503511 | 10.4671981 | 0.9863794  |
| 0.3  | 11.1325396 | 11.0434999 | 10.863149  | 10.8396763 | 10.6663089 | 10.5376095 | 10.2059798 | 10.1266694 | 0.98635147 |
| 0.31 | 10.7558046 | 10.6710022 | 10.4992038 | 10.4768413 | 10.3116518 | 10.1889986 | 9.87284895 | 9.7972192  | 0.98632351 |
| 0.32 | 10.3918186 | 10.3110688 | 10.1474518 | 10.1261515 | 9.96878714 | 9.85192052 | 9.55059178 | 9.47848694 | 0.98629552 |
| 0.33 | 10.0401502 | 9.96327594 | 9.80748452 | 9.78720021 | 9.63732281 | 9.52599387 | 9.23885332 | 9.17012397 | 0.98626749 |
| 0.34 | 9.70038261 | 9.62721418 | 9.47890703 | 9.45959461 | 9.31687974 | 9.21084972 | 8.93729025 | 8.87179295 | 0.98623943 |
| 0.35 | 9.37211304 | 9.30248779 | 9.16133779 | 9.14295491 | 9.00709147 | 8.90613133 | 8.64557041 | 8.58316752 | 0.98621133 |
| 0.36 | 9.0549524  | 8.98871445 | 8.85440797 | 8.83691404 | 8.70760373 | 8.6114938  | 8.36337253 | 8.30393191 | 0.98618319 |
| 0.37 | 8.74852476 | 8.68552469 | 8.55776115 | 8.54111724 | 8.41807402 | 8.32660364 | 8.0903858  | 8.03378066 | 0.98615502 |
| 0.38 | 8.4524669  | 8.39256154 | 8.2710528  | 8.2552216  | 8.13817123 | 8.05113837 | 7.82630956 | 7.77241823 | 0.98612682 |
| 0.39 | 8.1664279  | 8.10948005 | 7.99394997 | 7.97889571 | 7.86757528 | 7.78478619 | 7.57085297 | 7.51955867 | 0.98609858 |
| 0.4  | 7.89006872 | 7.83594691 | 7.72613083 | 7.71181924 | 7.6059767  | 7.52724562 | 7.32373467 | 7.27492539 | 0.98607031 |
| 0.41 | 7.62306178 | 7.57164006 | 7.46728437 | 7.45368258 | 7.35307633 | 7.27822515 | 7.0846825  | 7.03825074 | 0.98604201 |
| 0.42 | 7.36509059 | 7.31624829 | 7.21710997 | 7.20418649 | 7.10858495 | 7.03744291 | 6.85343317 | 6.8092758  | 0.98601367 |
| 0.43 | 7.11584937 | 7.0694709  | 6.97531709 | 6.96304175 | 6.87222296 | 6.80462636 | 6.62973199 | 6.5877501  | 0.98598529 |
| 0.44 | 6.8750427  | 6.83101731 | 6.74162494 | 6.72996881 | 6.64372006 | 6.57951198 | 6.41333258 | 6.37343128 | 0.98595688 |
| 0.45 | 6.64238514 | 6.60060678 | 6.51576211 | 6.5046975  | 6.42281493 | 6.36184495 | 6.20399661 | 6.16608487 | 0.98592844 |
| 0.46 | 6.41760092 | 6.37796801 | 6.2974663  | 6.28696666 | 6.20925494 | 6.1513789  | 6.00149352 | 5.96548405 | 0.98589996 |
| 0.47 | 6.2004236  | 6.16283885 | 6.086484   | 6.07652389 | 6.00279587 | 5.94787561 | 5.80560029 | 5.77140937 | 0.98587144 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.48 | 5.99059575 | 5.95496601 | 5.88257018 | 5.87312525 | 5.80320161 | 5.75110472 | 5.61610116 | 5.5836485  | 0.9858429  |
| 0.49 | 5.78786867 | 5.75410473 | 5.68548803 | 5.67653494 | 5.6102439  | 5.56084352 | 5.43278742 | 5.40199605 | 0.98581431 |
| 0.5  | 5.59200204 | 5.56001851 | 5.49500867 | 5.48652507 | 5.42370207 | 5.37687664 | 5.25545718 | 5.22625328 | 0.9857857  |
| 0.51 | 5.40276372 | 5.37247883 | 5.31091088 | 5.30287537 | 5.2433628  | 5.19899586 | 5.08391513 | 5.05622794 | 0.98575705 |
| 0.52 | 5.21992939 | 5.19126487 | 5.13298088 | 5.12537296 | 5.06901986 | 5.02699983 | 4.91797234 | 4.89173402 | 0.98572836 |
| 0.53 | 5.04328234 | 5.01616326 | 4.96101201 | 4.95381205 | 4.90047385 | 4.86069386 | 4.75744605 | 4.73259157 | 0.98569964 |
| 0.54 | 4.87261318 | 4.84696784 | 4.79480458 | 4.78799379 | 4.73753203 | 4.69988972 | 4.60215945 | 4.57862649 | 0.98567089 |
| 0.55 | 4.70771962 | 4.68347939 | 4.63416554 | 4.62772593 | 4.58000807 | 4.54440538 | 4.45194153 | 4.42967035 | 0.9856421  |
| 0.56 | 4.5484062  | 4.52550542 | 4.47890835 | 4.4728227  | 4.42772181 | 4.39406487 | 4.30662683 | 4.28556018 | 0.98561328 |
| 0.57 | 4.39448409 | 4.37285991 | 4.3288527  | 4.32310453 | 4.2804991  | 4.24869801 | 4.16605531 | 4.14613835 | 0.98558442 |
| 0.58 | 4.24577084 | 4.22536314 | 4.18382433 | 4.17839784 | 4.13817158 | 4.10814025 | 4.03007215 | 4.01125231 | 0.98555553 |
| 0.59 | 4.10209018 | 4.08284145 | 4.0436548  | 4.03853491 | 4.00057648 | 3.9722325  | 3.89852758 | 3.88075451 | 0.98552661 |
| 0.6  | 3.9632718  | 3.94512702 | 3.90818133 | 3.90335359 | 3.86755644 | 3.84082092 | 3.77127673 | 3.75450219 | 0.98549765 |
| 0.61 | 3.82915116 | 3.8120577  | 3.77724659 | 3.77269717 | 3.73895935 | 3.71375677 | 3.64817944 | 3.63235723 | 0.98546865 |
| 0.62 | 3.69956928 | 3.68347681 | 3.65069852 | 3.6464142  | 3.61463814 | 3.59089623 | 3.52910014 | 3.514186   | 0.98543963 |
| 0.63 | 3.57437256 | 3.55923297 | 3.52839016 | 3.52435828 | 3.49445064 | 3.47210023 | 3.41390767 | 3.39985923 | 0.98541056 |
| 0.64 | 3.45341262 | 3.43917988 | 3.41017946 | 3.40638793 | 3.3782594  | 3.35723431 | 3.30247517 | 3.28925184 | 0.98538147 |
| 0.65 | 3.33654606 | 3.32317618 | 3.29592915 | 3.29236637 | 3.26593155 | 3.24616844 | 3.19467991 | 3.18224283 | 0.98535234 |
| 0.66 | 3.22363438 | 3.21108529 | 3.18550653 | 3.18216145 | 3.15733862 | 3.13877691 | 3.09040317 | 3.07871514 | 0.98532317 |
| 0.67 | 3.11454372 | 3.10277524 | 3.07878337 | 3.0756454  | 3.05235642 | 3.03493817 | 2.9895301  | 2.97855551 | 0.98529397 |
| 0.68 | 3.0091448  | 2.99811848 | 2.97563573 | 2.97269474 | 2.95086491 | 2.93453468 | 2.89194961 | 2.88165437 | 0.98526474 |
| 0.69 | 2.90731266 | 2.89699181 | 2.87594381 | 2.87319014 | 2.85274801 | 2.8374528  | 2.79755421 | 2.78790571 | 0.98523548 |
| 0.7  | 2.80892661 | 2.79927614 | 2.77959185 | 2.77701625 | 2.75789353 | 2.74358262 | 2.70623995 | 2.69720696 | 0.98520618 |
| 0.71 | 2.71387004 | 2.70485643 | 2.68646794 | 2.68406157 | 2.66619297 | 2.65281792 | 2.61790626 | 2.60945891 | 0.98517684 |
| 0.72 | 2.62203026 | 2.61362149 | 2.59646393 | 2.59421834 | 2.57754148 | 2.56505594 | 2.53245584 | 2.52456556 | 0.98514747 |
| 0.73 | 2.53329843 | 2.52546392 | 2.5094753  | 2.50738243 | 2.49183766 | 2.48019735 | 2.44979459 | 2.44243404 | 0.98511807 |
| 0.74 | 2.44756936 | 2.4402799  | 2.42540103 | 2.42345317 | 2.40898352 | 2.3981461  | 2.36983146 | 2.3629745  | 0.98508863 |
| 0.75 | 2.36474143 | 2.35796915 | 2.34414348 | 2.34233325 | 2.3288843  | 2.31880932 | 2.29247839 | 2.28610001 | 0.98505916 |
| 0.76 | 2.28471648 | 2.27843474 | 2.26560828 | 2.26392866 | 2.25144839 | 2.24209719 | 2.21765018 | 2.21172648 | 0.98502966 |
| 0.77 | 2.20739964 | 2.20158303 | 2.18970422 | 2.18814848 | 2.17658724 | 2.1679229  | 2.14526442 | 2.13977253 | 0.98500012 |
| 0.78 | 2.13269928 | 2.12732353 | 2.11634316 | 2.11490489 | 2.10421525 | 2.09620249 | 2.07524139 | 2.07015946 | 0.98497055 |
| 0.79 | 2.06052684 | 2.05556881 | 2.04543989 | 2.04411297 | 2.03424963 | 2.02685477 | 2.00750396 | 2.0028111  | 0.98494094 |
| 0.8  | 1.99079678 | 1.98623438 | 1.97691207 | 1.97569066 | 1.96661039 | 1.95980124 | 1.94197753 | 1.93765379 | 0.9849113  |
| 0.81 | 1.92342644 | 1.9192386  | 1.91068012 | 1.90955864 | 1.90122017 | 1.89496602 | 1.87858993 | 1.87461623 | 0.98488163 |
| 0.82 | 1.85833598 | 1.8545026  | 1.84666712 | 1.84564025 | 1.83800419 | 1.83227572 | 1.81727135 | 1.81362947 | 0.98485192 |
| 0.83 | 1.79544824 | 1.79195014 | 1.78479874 | 1.78386139 | 1.77689015 | 1.77165937 | 1.75795426 | 1.75462678 | 0.98482218 |
| 0.84 | 1.73468867 | 1.73150758 | 1.72500311 | 1.72415044 | 1.71780817 | 1.71304836 | 1.70057332 | 1.69754363 | 0.9847924  |
| 0.85 | 1.67598527 | 1.67310374 | 1.6672108  | 1.66643819 | 1.66069068 | 1.65637635 | 1.64506533 | 1.64231756 | 0.98476259 |
| 0.86 | 1.61926843 | 1.61666988 | 1.61135469 | 1.61065774 | 1.60547235 | 1.6015792  | 1.59136917 | 1.58888815 | 0.98473275 |
| 0.87 | 1.56447095 | 1.56213953 | 1.55736991 | 1.55674441 | 1.55209005 | 1.54859488 | 1.53942569 | 1.53719696 | 0.98470287 |
| 0.88 | 1.51152786 | 1.50944849 | 1.50519377 | 1.50463572 | 1.50048272 | 1.49736341 | 1.48917769 | 1.48718744 | 0.98467296 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.89 | 1.46037642 | 1.45853472 | 1.45476567 | 1.45427126 | 1.45059134 | 1.44782682 | 1.44056981 | 1.43880487 | 0.98464302 |
| 0.9  | 1.41095598 | 1.40933828 | 1.40602705 | 1.40559264 | 1.40235887 | 1.39992901 | 1.39354854 | 1.39199633 | 0.98461304 |
| 0.91 | 1.36320797 | 1.36180123 | 1.35892131 | 1.35854343 | 1.35573013 | 1.35361579 | 1.34806207 | 1.34671061 | 0.98458303 |
| 0.92 | 1.3170758  | 1.31586761 | 1.31339374 | 1.31306909 | 1.31065181 | 1.30883473 | 1.30406032 | 1.30289817 | 0.98455298 |
| 0.93 | 1.27250479 | 1.27148334 | 1.26939146 | 1.26911691 | 1.26707235 | 1.26553514 | 1.26149482 | 1.26051107 | 0.9845229  |
| 0.94 | 1.22944209 | 1.22859615 | 1.22686339 | 1.22663594 | 1.22494192 | 1.22366802 | 1.22031868 | 1.21950295 | 0.98449279 |
| 0.95 | 1.18783668 | 1.18715554 | 1.18576012 | 1.18557692 | 1.18421234 | 1.18318596 | 1.18048657 | 1.17982894 | 0.98446264 |
| 0.96 | 1.14763923 | 1.14711273 | 1.14603392 | 1.14589227 | 1.14483702 | 1.14404315 | 1.1419546  | 1.14144565 | 0.98443246 |
| 0.97 | 1.1088021  | 1.10842056 | 1.10763865 | 1.10753598 | 1.10677095 | 1.10619529 | 1.10468035 | 1.10431107 | 0.98440225 |
| 0.98 | 1.07127925 | 1.07103349 | 1.07052974 | 1.07046358 | 1.06997057 | 1.06959953 | 1.06862276 | 1.0683846  | 0.984372   |
| 0.99 | 1.03502621 | 1.03490748 | 1.03466407 | 1.0346321  | 1.03439382 | 1.03421445 | 1.03374212 | 1.03362691 | 0.98434172 |
| 1.01 | 0.96615911 | 0.96626995 | 0.96649727 | 0.96652714 | 0.96674978 | 0.96691745 | 0.96735925 | 0.96746707 | 0.98428106 |
| 1.02 | 0.93346343 | 0.93367762 | 0.93411698 | 0.93417471 | 0.93460514 | 0.93492936 | 0.93578392 | 0.93599253 | 0.98425068 |
| 1.03 | 0.90187419 | 0.90218463 | 0.90282151 | 0.90290521 | 0.90352932 | 0.90399951 | 0.90523924 | 0.90554195 | 0.98422026 |
| 1.04 | 0.87135397 | 0.8717539  | 0.87257452 | 0.87268239 | 0.87348678 | 0.8740929  | 0.87569155 | 0.87608201 | 0.98418981 |
| 1.05 | 0.84186658 | 0.8423496  | 0.8433409  | 0.84347121 | 0.84444315 | 0.84517568 | 0.84710833 | 0.8475805  | 0.98415933 |
| 1.06 | 0.81337706 | 0.81393711 | 0.81508668 | 0.81523781 | 0.81636523 | 0.81721512 | 0.81945808 | 0.82000622 | 0.98412882 |
| 1.07 | 0.78585166 | 0.78648298 | 0.78777905 | 0.78794947 | 0.78922091 | 0.79017956 | 0.79271035 | 0.79332901 | 0.98409827 |
| 1.08 | 0.75925774 | 0.75995487 | 0.7613863  | 0.76157455 | 0.76297915 | 0.7640384  | 0.76683569 | 0.76751969 | 0.98406769 |
| 1.09 | 0.73356378 | 0.73432156 | 0.73587778 | 0.73608247 | 0.73760992 | 0.73876207 | 0.7418056  | 0.74255003 | 0.98403707 |
| 1.1  | 0.70873933 | 0.70955286 | 0.71122387 | 0.71144368 | 0.71308423 | 0.71432193 | 0.71759251 | 0.7183927  | 0.98400642 |
| 1.11 | 0.68475496 | 0.68561961 | 0.68739593 | 0.68762963 | 0.68937403 | 0.69069034 | 0.69416976 | 0.69502128 | 0.98397574 |
| 1.12 | 0.66158225 | 0.66249362 | 0.66436629 | 0.66461269 | 0.66645219 | 0.66784055 | 0.67151154 | 0.6724102  | 0.98394502 |
| 1.13 | 0.63919372 | 0.64014768 | 0.64210821 | 0.6423662  | 0.64429251 | 0.64574668 | 0.6495929  | 0.65053472 | 0.98391428 |
| 1.14 | 0.61756283 | 0.61855547 | 0.62059583 | 0.62086437 | 0.62286965 | 0.62438373 | 0.6283897  | 0.62937092 | 0.98388349 |
| 1.15 | 0.59666396 | 0.59769157 | 0.59980418 | 0.60008226 | 0.6021591  | 0.60372753 | 0.60787859 | 0.60889564 | 0.98385268 |
| 1.16 | 0.57647232 | 0.5775314  | 0.5797091  | 0.57999579 | 0.58213718 | 0.58375468 | 0.58803698 | 0.58908648 | 0.98382183 |
| 1.17 | 0.55696398 | 0.55805124 | 0.56028726 | 0.56058167 | 0.56278099 | 0.56444259 | 0.56884301 | 0.56992177 | 0.98379095 |
| 1.18 | 0.53811583 | 0.53922815 | 0.54151611 | 0.5418174  | 0.5440684  | 0.54576939 | 0.55027555 | 0.55138054 | 0.98376003 |
| 1.19 | 0.51990551 | 0.52103996 | 0.52337384 | 0.52368122 | 0.52597801 | 0.52771395 | 0.53231415 | 0.53344252 | 0.98372908 |
| 1.2  | 0.50231144 | 0.50346526 | 0.50583939 | 0.50615211 | 0.50848913 | 0.51025582 | 0.51493902 | 0.51608807 | 0.9836981  |
| 1.21 | 0.48531278 | 0.48648335 | 0.48889239 | 0.48920975 | 0.49158175 | 0.49337526 | 0.49813102 | 0.49929821 | 0.98366709 |
| 1.22 | 0.46888936 | 0.47007424 | 0.47251316 | 0.4728345  | 0.47523655 | 0.47705315 | 0.48187165 | 0.48305458 | 0.98363604 |
| 1.23 | 0.45302173 | 0.45421862 | 0.45668268 | 0.45700738 | 0.45943483 | 0.46127102 | 0.466143   | 0.46733939 | 0.98360496 |
| 1.24 | 0.43769107 | 0.4388978  | 0.44138257 | 0.44171003 | 0.44415853 | 0.44601099 | 0.45092775 | 0.45213547 | 0.98357385 |
| 1.25 | 0.42287921 | 0.42409376 | 0.42659505 | 0.42692473 | 0.42939016 | 0.43125581 | 0.43620913 | 0.43742618 | 0.9835427  |
| 1.26 | 0.40856861 | 0.40978906 | 0.41230295 | 0.41263434 | 0.41511284 | 0.41698877 | 0.42197094 | 0.42319543 | 0.98351152 |
| 1.27 | 0.39474228 | 0.39596685 | 0.39848968 | 0.39882229 | 0.40131025 | 0.40319372 | 0.40819749 | 0.40942764 | 0.9834803  |
| 1.28 | 0.38138385 | 0.38261087 | 0.38513918 | 0.38547257 | 0.3879666  | 0.38985505 | 0.39487362 | 0.39610776 | 0.98344906 |
| 1.29 | 0.36847748 | 0.36970539 | 0.37223597 | 0.3725697  | 0.37506663 | 0.37695765 | 0.38198465 | 0.38322121 | 0.98341778 |
| 1.3  | 0.35600788 | 0.35723521 | 0.35976505 | 0.36009872 | 0.36259558 | 0.36448693 | 0.36951638 | 0.3707539  | 0.98338647 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.31 | 0.34396025 | 0.34518565 | 0.34771194 | 0.34804519 | 0.3505392  | 0.35242877 | 0.35745509 | 0.35869219 | 0.98335512 |
| 1.32 | 0.33232033 | 0.33354252 | 0.33606264 | 0.33639512 | 0.33888369 | 0.34076953 | 0.34578749 | 0.34702288 | 0.98332374 |
| 1.33 | 0.32107432 | 0.32229212 | 0.32480363 | 0.32513501 | 0.32761574 | 0.329496   | 0.33450073 | 0.33573321 | 0.98329233 |
| 1.34 | 0.31020888 | 0.31142119 | 0.31392182 | 0.31425181 | 0.31672244 | 0.31859544 | 0.32358238 | 0.32481082 | 0.98326089 |
| 1.35 | 0.29971113 | 0.30091694 | 0.30340458 | 0.3037329  | 0.30619135 | 0.30805549 | 0.3130204  | 0.31424377 | 0.98322941 |
| 1.36 | 0.28956864 | 0.290767   | 0.2932397  | 0.29356609 | 0.29601042 | 0.29786423 | 0.30280318 | 0.3040205  | 0.9831979  |
| 1.37 | 0.27976938 | 0.28095941 | 0.28341537 | 0.2837396  | 0.28616801 | 0.28801012 | 0.29291946 | 0.29412983 | 0.98316636 |
| 1.38 | 0.27030174 | 0.27148264 | 0.27392018 | 0.27424202 | 0.27665287 | 0.27848201 | 0.28335835 | 0.28456092 | 0.98313478 |
| 1.39 | 0.26115449 | 0.26232552 | 0.26474311 | 0.26506236 | 0.2674541  | 0.26926912 | 0.27410932 | 0.27530332 | 0.98310317 |
| 1.4  | 0.25231679 | 0.25347726 | 0.25587349 | 0.25618996 | 0.25856119 | 0.26036101 | 0.26516219 | 0.26634689 | 0.98307153 |
| 1.41 | 0.24377816 | 0.24492746 | 0.24730103 | 0.24761455 | 0.24996398 | 0.2517476  | 0.2565071  | 0.25768185 | 0.98303986 |
| 1.42 | 0.23552849 | 0.23666605 | 0.23901577 | 0.23932618 | 0.24165262 | 0.24341915 | 0.24813452 | 0.2492987  | 0.98300815 |
| 1.43 | 0.227558   | 0.22868329 | 0.23100809 | 0.23131525 | 0.23361762 | 0.23536622 | 0.24003522 | 0.24118829 | 0.98297641 |
| 1.44 | 0.21985723 | 0.22096979 | 0.22326869 | 0.22357247 | 0.22584978 | 0.22757971 | 0.23220029 | 0.23334172 | 0.98294464 |
| 1.45 | 0.21241707 | 0.21351647 | 0.21578858 | 0.21608886 | 0.21834023 | 0.22005079 | 0.2246211  | 0.22575043 | 0.98291283 |
| 1.46 | 0.20522869 | 0.20631455 | 0.20855907 | 0.20885574 | 0.21108037 | 0.21277095 | 0.2172893  | 0.21840611 | 0.982881   |
| 1.47 | 0.19828356 | 0.19935555 | 0.20157178 | 0.20186474 | 0.2040619  | 0.20573194 | 0.21019681 | 0.21130072 | 0.98284912 |
| 1.48 | 0.19157347 | 0.19263128 | 0.19481857 | 0.19510775 | 0.1972768  | 0.19892581 | 0.20333583 | 0.20442649 | 0.98281722 |
| 1.49 | 0.18509046 | 0.18613382 | 0.18829162 | 0.18857694 | 0.1907173  | 0.19234483 | 0.1966988  | 0.19777589 | 0.98278529 |
| 1.5  | 0.17882683 | 0.17985552 | 0.18198333 | 0.18226473 | 0.18437591 | 0.18598158 | 0.1902784  | 0.19134166 | 0.98275332 |
| 1.51 | 0.17277517 | 0.17378898 | 0.1758864  | 0.17616381 | 0.17824537 | 0.17982883 | 0.18406757 | 0.18511676 | 0.98272132 |
| 1.52 | 0.16692831 | 0.16792707 | 0.16999372 | 0.1702671  | 0.17231867 | 0.17387964 | 0.17805947 | 0.17909437 | 0.98268928 |
| 1.53 | 0.1612793  | 0.16226288 | 0.16429847 | 0.16456777 | 0.16658904 | 0.16812726 | 0.17224748 | 0.1732679  | 0.98265722 |
| 1.54 | 0.15582147 | 0.15678975 | 0.15879402 | 0.15905922 | 0.16104992 | 0.16256518 | 0.16662519 | 0.16763099 | 0.98262512 |
| 1.55 | 0.15054833 | 0.15150122 | 0.15347399 | 0.15373505 | 0.15569497 | 0.15718711 | 0.16118642 | 0.16217746 | 0.98259298 |
| 1.56 | 0.14545364 | 0.14639108 | 0.14833219 | 0.1485891  | 0.15051808 | 0.15198696 | 0.15592517 | 0.15690135 | 0.98256082 |
| 1.57 | 0.14053136 | 0.1414533  | 0.14336266 | 0.1436154  | 0.14551332 | 0.14695884 | 0.15083566 | 0.15179689 | 0.98252862 |
| 1.58 | 0.13577566 | 0.13668208 | 0.13855962 | 0.13880818 | 0.14067497 | 0.14209707 | 0.14591227 | 0.1468585  | 0.98249639 |
| 1.59 | 0.13118089 | 0.13207178 | 0.13391749 | 0.13416187 | 0.1359975  | 0.13739613 | 0.14114959 | 0.14208076 | 0.98246413 |
| 1.6  | 0.12674161 | 0.127617   | 0.12943089 | 0.12967109 | 0.13147555 | 0.13285072 | 0.13654236 | 0.13745845 | 0.98243184 |
| 1.61 | 0.12245256 | 0.12331247 | 0.1250946  | 0.12533063 | 0.12710396 | 0.12845568 | 0.13208551 | 0.13298653 | 0.98239951 |
| 1.62 | 0.11830866 | 0.11915313 | 0.12090359 | 0.12113545 | 0.12287773 | 0.12420604 | 0.12777414 | 0.12866009 | 0.98236715 |
| 1.63 | 0.11430499 | 0.11513409 | 0.11685299 | 0.1170807  | 0.11879202 | 0.12009699 | 0.1236035  | 0.1244744  | 0.98233476 |
| 1.64 | 0.1104368  | 0.11125061 | 0.1129381  | 0.11316168 | 0.11484216 | 0.11612387 | 0.11956899 | 0.12042488 | 0.98230234 |
| 1.65 | 0.10669952 | 0.10749813 | 0.10915436 | 0.10937383 | 0.11102363 | 0.1122822  | 0.11566617 | 0.11650711 | 0.98226988 |
| 1.66 | 0.10308872 | 0.10387221 | 0.1054974  | 0.10571278 | 0.10733207 | 0.10856762 | 0.11189074 | 0.11271679 | 0.98223739 |
| 1.67 | 0.0996001  | 0.10036859 | 0.10196294 | 0.10217427 | 0.10376326 | 0.10497592 | 0.10823854 | 0.10904978 | 0.98220487 |
| 1.68 | 0.09622955 | 0.09698316 | 0.09854691 | 0.0987542  | 0.10031311 | 0.10150305 | 0.10470555 | 0.10550207 | 0.98217232 |
| 1.69 | 0.09297305 | 0.09371191 | 0.09524532 | 0.09544862 | 0.09697767 | 0.09814507 | 0.10128789 | 0.10206978 | 0.98213974 |
| 1.7  | 0.08982676 | 0.090551   | 0.09205434 | 0.09225368 | 0.09375314 | 0.09489818 | 0.09798177 | 0.09874915 | 0.98210712 |
| 1.71 | 0.08678695 | 0.08749671 | 0.08897027 | 0.08916568 | 0.09063583 | 0.09175871 | 0.09478358 | 0.09553655 | 0.98207447 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.72 | 0.08385    | 0.08454545 | 0.08598952 | 0.08618105 | 0.08762217 | 0.0887231  | 0.09168977 | 0.09242847 | 0.98204179 |
| 1.73 | 0.08101244 | 0.08169372 | 0.08310864 | 0.08329633 | 0.08470872 | 0.08578791 | 0.08869695 | 0.0894215  | 0.98200907 |
| 1.74 | 0.07827091 | 0.07893819 | 0.08032427 | 0.08050816 | 0.08189213 | 0.08294983 | 0.08580181 | 0.08651235 | 0.98197633 |
| 1.75 | 0.07562215 | 0.0762756  | 0.07763319 | 0.07781332 | 0.0791692  | 0.08020564 | 0.08300118 | 0.08369785 | 0.98194355 |
| 1.76 | 0.07306303 | 0.07370282 | 0.07503227 | 0.07520869 | 0.07653681 | 0.07755223 | 0.08029196 | 0.08097492 | 0.98191074 |
| 1.77 | 0.07059051 | 0.07121682 | 0.07251848 | 0.07269124 | 0.07399194 | 0.0749866  | 0.07767117 | 0.07834057 | 0.98187789 |
| 1.78 | 0.06820167 | 0.06881468 | 0.07008891 | 0.07025805 | 0.07153169 | 0.07250586 | 0.07513592 | 0.07579192 | 0.98184502 |
| 1.79 | 0.06589366 | 0.06649355 | 0.06774074 | 0.06790631 | 0.06915325 | 0.07010718 | 0.07268343 | 0.07332618 | 0.98181211 |
| 1.8  | 0.06366376 | 0.06425072 | 0.06547124 | 0.0656333  | 0.06685389 | 0.06778785 | 0.07031099 | 0.07094067 | 0.98177917 |
| 1.81 | 0.06150932 | 0.06208354 | 0.06327778 | 0.06343636 | 0.06463098 | 0.06554526 | 0.06801598 | 0.06863276 | 0.9817462  |
| 1.82 | 0.05942779 | 0.05998946 | 0.0611578  | 0.06131296 | 0.06248199 | 0.06337685 | 0.06579589 | 0.06639994 | 0.9817132  |
| 1.83 | 0.0574167  | 0.05796602 | 0.05910885 | 0.05926064 | 0.06040445 | 0.06128019 | 0.06364826 | 0.06423975 | 0.98168016 |
| 1.84 | 0.05547367 | 0.05601082 | 0.05712854 | 0.05727702 | 0.05839599 | 0.05925288 | 0.06157074 | 0.06214984 | 0.9816471  |
| 1.85 | 0.05359639 | 0.05412157 | 0.05521458 | 0.0553598  | 0.05645431 | 0.05729265 | 0.05956102 | 0.06012793 | 0.981614   |
| 1.86 | 0.05178264 | 0.05229605 | 0.05336474 | 0.05350674 | 0.05457719 | 0.05539726 | 0.05761691 | 0.05817179 | 0.98158087 |
| 1.87 | 0.05003027 | 0.0505321  | 0.05157687 | 0.05171572 | 0.05276249 | 0.05356458 | 0.05573625 | 0.05627929 | 0.9815477  |
| 1.88 | 0.0483372  | 0.04882765 | 0.04984891 | 0.04998465 | 0.05100812 | 0.05179252 | 0.05391697 | 0.05444836 | 0.98151451 |
| 1.89 | 0.04670143 | 0.04718069 | 0.04817883 | 0.04831152 | 0.04931209 | 0.05007909 | 0.05215708 | 0.052677   | 0.98148128 |
| 1.9  | 0.04512101 | 0.04558928 | 0.04656471 | 0.04669439 | 0.04767245 | 0.04842235 | 0.05045464 | 0.05096326 | 0.98144802 |
| 1.91 | 0.04359408 | 0.04405156 | 0.04500467 | 0.0451314  | 0.04608734 | 0.04682042 | 0.04880776 | 0.04930527 | 0.98141473 |
| 1.92 | 0.04211881 | 0.04256569 | 0.04349689 | 0.04362072 | 0.04455492 | 0.04527148 | 0.04721464 | 0.04770123 | 0.98138141 |
| 1.93 | 0.04069348 | 0.04112995 | 0.04203962 | 0.04216061 | 0.04307346 | 0.04377378 | 0.04567352 | 0.04614937 | 0.98134806 |
| 1.94 | 0.03931637 | 0.03974264 | 0.04063118 | 0.04074937 | 0.04164126 | 0.04232563 | 0.0441827  | 0.04464799 | 0.98131467 |
| 1.95 | 0.03798587 | 0.03840212 | 0.03926993 | 0.03938538 | 0.04025668 | 0.04092539 | 0.04274054 | 0.04319546 | 0.98128125 |
| 1.96 | 0.0367004  | 0.03710681 | 0.03795428 | 0.03806704 | 0.03891813 | 0.03957148 | 0.04134546 | 0.04179019 | 0.9812478  |
| 1.97 | 0.03545842 | 0.0358552  | 0.0366827  | 0.03679282 | 0.0376241  | 0.03826235 | 0.03999591 | 0.04043063 | 0.98121432 |
| 1.98 | 0.03425848 | 0.0346458  | 0.03545373 | 0.03556126 | 0.03637309 | 0.03699654 | 0.03869042 | 0.0391153  | 0.98118081 |
| 1.99 | 0.03309914 | 0.03347719 | 0.03426594 | 0.03437092 | 0.03516368 | 0.0357726  | 0.03742753 | 0.03784277 | 0.98114726 |
| 2    | 0.03197904 | 0.03234801 | 0.03311793 | 0.03322043 | 0.03399448 | 0.03458915 | 0.03620587 | 0.03661163 | 0.98111369 |
| 2.01 | 0.03089684 | 0.03125691 | 0.03200839 | 0.03210845 | 0.03286415 | 0.03344485 | 0.03502408 | 0.03542055 | 0.98108008 |
| 2.02 | 0.02985126 | 0.03020261 | 0.03093602 | 0.03103369 | 0.03177141 | 0.03233841 | 0.03388087 | 0.03426821 | 0.98104644 |
| 2.03 | 0.02884107 | 0.02918387 | 0.02989958 | 0.0299949  | 0.03071501 | 0.03126857 | 0.03277497 | 0.03315337 | 0.98101277 |
| 2.04 | 0.02786506 | 0.0281995  | 0.02889787 | 0.02899089 | 0.02969373 | 0.03023413 | 0.03170518 | 0.03207479 | 0.98097906 |
| 2.05 | 0.02692208 | 0.02724833 | 0.02792971 | 0.02802048 | 0.0287064  | 0.02923391 | 0.03067029 | 0.03103131 | 0.98094533 |
| 2.06 | 0.02601101 | 0.02632924 | 0.02699399 | 0.02708255 | 0.02775191 | 0.02826677 | 0.02966919 | 0.03002177 | 0.98091156 |
| 2.07 | 0.02513078 | 0.02544116 | 0.02608961 | 0.02617602 | 0.02682915 | 0.02733164 | 0.02870077 | 0.02904507 | 0.98087777 |
| 2.08 | 0.02428033 | 0.02458303 | 0.02521554 | 0.02529983 | 0.02593708 | 0.02642744 | 0.02776395 | 0.02810015 | 0.98084394 |
| 2.09 | 0.02345866 | 0.02375384 | 0.02437075 | 0.02445298 | 0.02507466 | 0.02555315 | 0.02685772 | 0.02718597 | 0.98081008 |
| 2.1  | 0.0226648  | 0.02295262 | 0.02355427 | 0.02363447 | 0.02424092 | 0.02470779 | 0.02598106 | 0.02630153 | 0.98077618 |
| 2.11 | 0.0218978  | 0.02217843 | 0.02276513 | 0.02284335 | 0.02343491 | 0.02389039 | 0.02513302 | 0.02544586 | 0.98074226 |
| 2.12 | 0.02115676 | 0.02143035 | 0.02200244 | 0.02207872 | 0.02265569 | 0.02310003 | 0.02431266 | 0.02461804 | 0.98070831 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.13 | 0.0204408  | 0.0207075  | 0.0212653  | 0.02133968 | 0.02190239 | 0.02233583 | 0.02351908 | 0.02381714 | 0.98067432 |
| 2.14 | 0.01974906 | 0.02000904 | 0.02055285 | 0.02062538 | 0.02117413 | 0.0215969  | 0.0227514  | 0.0230423  | 0.9806403  |
| 2.15 | 0.01908074 | 0.01933413 | 0.01986428 | 0.01993499 | 0.02047008 | 0.02088242 | 0.02200877 | 0.02229266 | 0.98060625 |
| 2.16 | 0.01843503 | 0.01868199 | 0.01919877 | 0.01926771 | 0.01978945 | 0.02019158 | 0.02129039 | 0.02156742 | 0.98057217 |
| 2.17 | 0.01781117 | 0.01805185 | 0.01855556 | 0.01862276 | 0.01913144 | 0.01952359 | 0.02059546 | 0.02086577 | 0.98053806 |
| 2.18 | 0.01720842 | 0.01744296 | 0.01793389 | 0.01799941 | 0.01849532 | 0.0188777  | 0.01992321 | 0.02018694 | 0.98050392 |
| 2.19 | 0.01662608 | 0.0168546  | 0.01733306 | 0.01739692 | 0.01788035 | 0.01825318 | 0.0192729  | 0.0195302  | 0.98046974 |
| 2.2  | 0.01606344 | 0.0162861  | 0.01675236 | 0.01681459 | 0.01728582 | 0.01764931 | 0.01864382 | 0.01889483 | 0.98043553 |
| 2.21 | 0.01551983 | 0.01573677 | 0.01619111 | 0.01625176 | 0.01671106 | 0.01706543 | 0.01803527 | 0.01828012 | 0.9804013  |
| 2.22 | 0.01499463 | 0.01520596 | 0.01564866 | 0.01570777 | 0.01615542 | 0.01650086 | 0.01744658 | 0.01768542 | 0.98036703 |
| 2.23 | 0.0144872  | 0.01469307 | 0.01512439 | 0.01518198 | 0.01561825 | 0.01595497 | 0.01687711 | 0.01711006 | 0.98033273 |
| 2.24 | 0.01399694 | 0.01419747 | 0.01461768 | 0.0146738  | 0.01509894 | 0.01542714 | 0.01632623 | 0.01655342 | 0.9802984  |
| 2.25 | 0.01352327 | 0.01371859 | 0.01412795 | 0.01418262 | 0.01459689 | 0.01491677 | 0.01579333 | 0.01601489 | 0.98026404 |
| 2.26 | 0.01306563 | 0.01325586 | 0.01365462 | 0.01370789 | 0.01411154 | 0.01442329 | 0.01527783 | 0.01549388 | 0.98022964 |
| 2.27 | 0.01262348 | 0.01280874 | 0.01319715 | 0.01324905 | 0.01364233 | 0.01394613 | 0.01477915 | 0.01498981 | 0.98019522 |
| 2.28 | 0.01219629 | 0.0123767  | 0.01275501 | 0.01280556 | 0.01318872 | 0.01348475 | 0.01429674 | 0.01450215 | 0.98016076 |
| 2.29 | 0.01178355 | 0.01195923 | 0.01232769 | 0.01237693 | 0.01275019 | 0.01303864 | 0.01383009 | 0.01403035 | 0.98012628 |
| 2.3  | 0.01138479 | 0.01155585 | 0.01191468 | 0.01196263 | 0.01232625 | 0.01260729 | 0.01337866 | 0.01357391 | 0.98009176 |
| 2.31 | 0.01099952 | 0.01116607 | 0.01151555 | 0.01156221 | 0.0119164  | 0.01219021 | 0.01294197 | 0.01313231 | 0.98005721 |
| 2.32 | 0.01062728 | 0.01078944 | 0.0111297  | 0.01117519 | 0.01152017 | 0.01178693 | 0.01251954 | 0.01270507 | 0.98002263 |
| 2.33 | 0.01026765 | 0.01042551 | 0.01075683 | 0.01080113 | 0.01113713 | 0.01139699 | 0.01211089 | 0.01229174 | 0.97998802 |
| 2.34 | 0.00992018 | 0.01007385 | 0.01039644 | 0.01043958 | 0.01076681 | 0.01101994 | 0.01171558 | 0.01189185 | 0.97995338 |
| 2.35 | 0.00958447 | 0.00973406 | 0.01004813 | 0.01009014 | 0.01040881 | 0.01065538 | 0.01133318 | 0.01150498 | 0.9799187  |
| 2.36 | 0.00926013 | 0.00940573 | 0.00971149 | 0.00975239 | 0.01006272 | 0.01030287 | 0.01096325 | 0.01113069 | 0.979884   |
| 2.37 | 0.00894675 | 0.00908848 | 0.00938613 | 0.00942595 | 0.00972813 | 0.00996202 | 0.0106054  | 0.01076857 | 0.97984927 |
| 2.38 | 0.00864399 | 0.00878192 | 0.00907167 | 0.00911044 | 0.00940467 | 0.00963246 | 0.01025924 | 0.01041824 | 0.9798145  |
| 2.39 | 0.00835147 | 0.00848571 | 0.00876774 | 0.00880549 | 0.00909196 | 0.00931379 | 0.00992437 | 0.0100793  | 0.9797797  |
| 2.4  | 0.00806885 | 0.00819948 | 0.008474   | 0.00851074 | 0.00878965 | 0.00900567 | 0.00960043 | 0.00975139 | 0.97974488 |
| 2.41 | 0.00779579 | 0.00792292 | 0.0081901  | 0.00822586 | 0.00849739 | 0.00870773 | 0.00928706 | 0.00943415 | 0.97971002 |
| 2.42 | 0.00753197 | 0.00765567 | 0.00791571 | 0.00795052 | 0.00821485 | 0.00841966 | 0.00898393 | 0.00912723 | 0.97967513 |
| 2.43 | 0.00727709 | 0.00739745 | 0.00765051 | 0.00768439 | 0.00794171 | 0.00814112 | 0.00869068 | 0.0088303  | 0.97964021 |
| 2.44 | 0.00703082 | 0.00714793 | 0.0073942  | 0.00742717 | 0.00767764 | 0.00787179 | 0.00840701 | 0.00854302 | 0.97960526 |
| 2.45 | 0.00679289 | 0.00690683 | 0.00714647 | 0.00717856 | 0.00742236 | 0.00761137 | 0.0081326  | 0.00826509 | 0.97957028 |
| 2.46 | 0.00656302 | 0.00667386 | 0.00690705 | 0.00693828 | 0.00717557 | 0.00735957 | 0.00786715 | 0.0079962  | 0.97953526 |
| 2.47 | 0.00634092 | 0.00644875 | 0.00667564 | 0.00670603 | 0.00693698 | 0.00711609 | 0.00761036 | 0.00773606 | 0.97950022 |
| 2.48 | 0.00612633 | 0.00623124 | 0.00645199 | 0.00648156 | 0.00670632 | 0.00688067 | 0.00736195 | 0.00748439 | 0.97946515 |
| 2.49 | 0.00591901 | 0.00602106 | 0.00623583 | 0.00626461 | 0.00648333 | 0.00665304 | 0.00712165 | 0.0072409  | 0.97943004 |
| 2.5  | 0.00571871 | 0.00581797 | 0.00602691 | 0.00605491 | 0.00626776 | 0.00643294 | 0.0068892  | 0.00700533 | 0.97939491 |
| 2.51 | 0.00552518 | 0.00562173 | 0.00582499 | 0.00585224 | 0.00605936 | 0.00622013 | 0.00666433 | 0.00677743 | 0.97935974 |
| 2.52 | 0.00533821 | 0.00543211 | 0.00562984 | 0.00565635 | 0.00585788 | 0.00601435 | 0.0064468  | 0.00655694 | 0.97932455 |
| 2.53 | 0.00515756 | 0.00524888 | 0.00544123 | 0.00546701 | 0.00566311 | 0.00581538 | 0.00623637 | 0.00634362 | 0.97928932 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.54 | 0.00498302 | 0.00507184 | 0.00525893 | 0.00528402 | 0.00547481 | 0.00562299 | 0.00603281 | 0.00613724 | 0.97925406 |
| 2.55 | 0.00481439 | 0.00490076 | 0.00508274 | 0.00510714 | 0.00529277 | 0.00543697 | 0.00583589 | 0.00593758 | 0.97921877 |
| 2.56 | 0.00465147 | 0.00473546 | 0.00491246 | 0.00493619 | 0.00511678 | 0.0052571  | 0.00564541 | 0.00574441 | 0.97918345 |
| 2.57 | 0.00449406 | 0.00457573 | 0.00474788 | 0.00477097 | 0.00494665 | 0.00508318 | 0.00546114 | 0.00555753 | 0.9791481  |
| 2.58 | 0.00434197 | 0.00442139 | 0.00458881 | 0.00461127 | 0.00478217 | 0.00491502 | 0.00528288 | 0.00537673 | 0.97911272 |
| 2.59 | 0.00419504 | 0.00427226 | 0.00443507 | 0.00445692 | 0.00462316 | 0.00475242 | 0.00511044 | 0.00520181 | 0.97907731 |
| 2.6  | 0.00405307 | 0.00412816 | 0.00428648 | 0.00430773 | 0.00446944 | 0.00459519 | 0.00494363 | 0.00503258 | 0.97904187 |
| 2.61 | 0.00391591 | 0.00398891 | 0.00414287 | 0.00416354 | 0.00432083 | 0.00444317 | 0.00478227 | 0.00486885 | 0.9790064  |
| 2.62 | 0.0037834  | 0.00385437 | 0.00400408 | 0.00402417 | 0.00417716 | 0.00429618 | 0.00462617 | 0.00471046 | 0.9789709  |
| 2.63 | 0.00365536 | 0.00372436 | 0.00386993 | 0.00388947 | 0.00403827 | 0.00415405 | 0.00447517 | 0.00455721 | 0.97893537 |
| 2.64 | 0.00353166 | 0.00359874 | 0.00374028 | 0.00375928 | 0.003904   | 0.00401663 | 0.0043291  | 0.00440895 | 0.97889981 |
| 2.65 | 0.00341215 | 0.00347735 | 0.00361497 | 0.00363345 | 0.00377419 | 0.00388375 | 0.00418779 | 0.00426552 | 0.97886421 |
| 2.66 | 0.00329668 | 0.00336006 | 0.00349386 | 0.00351182 | 0.0036487  | 0.00375526 | 0.0040511  | 0.00412675 | 0.97882859 |
| 2.67 | 0.00318512 | 0.00324672 | 0.0033768  | 0.00339427 | 0.00352738 | 0.00363103 | 0.00391887 | 0.00399249 | 0.97879294 |
| 2.68 | 0.00307733 | 0.00313721 | 0.00326367 | 0.00328066 | 0.00341009 | 0.0035109  | 0.00379096 | 0.0038626  | 0.97875725 |
| 2.69 | 0.00297319 | 0.00303139 | 0.00315433 | 0.00317084 | 0.00329671 | 0.00339475 | 0.00366722 | 0.00373694 | 0.97872154 |
| 2.7  | 0.00287257 | 0.00292914 | 0.00304865 | 0.00306471 | 0.00318709 | 0.00328245 | 0.00354752 | 0.00361537 | 0.97868579 |
| 2.71 | 0.00277536 | 0.00283034 | 0.00294651 | 0.00296212 | 0.00308112 | 0.00317386 | 0.00343172 | 0.00349775 | 0.97865002 |
| 2.72 | 0.00268144 | 0.00273488 | 0.00284478 | 0.00286297 | 0.00297867 | 0.00306886 | 0.00331971 | 0.00338396 | 0.97861422 |
| 2.73 | 0.0025907  | 0.00264263 | 0.00275239 | 0.00276714 | 0.00287963 | 0.00296733 | 0.00321135 | 0.00327387 | 0.97857838 |
| 2.74 | 0.00250303 | 0.00255349 | 0.00266017 | 0.00267452 | 0.00278388 | 0.00286916 | 0.00310653 | 0.00316736 | 0.97854252 |
| 2.75 | 0.00241832 | 0.00246736 | 0.00257105 | 0.00258499 | 0.00269132 | 0.00277424 | 0.00300513 | 0.00306432 | 0.97850662 |
| 2.76 | 0.00233649 | 0.00238414 | 0.00248491 | 0.00249846 | 0.00260183 | 0.00268247 | 0.00290704 | 0.00296462 | 0.97847069 |
| 2.77 | 0.00225742 | 0.00230372 | 0.00240166 | 0.00241483 | 0.00251532 | 0.00259372 | 0.00281215 | 0.00286818 | 0.97843474 |
| 2.78 | 0.00218102 | 0.00222602 | 0.0023212  | 0.002334   | 0.00243168 | 0.00250792 | 0.00272036 | 0.00277487 | 0.97839875 |
| 2.79 | 0.00210722 | 0.00215093 | 0.00224343 | 0.00225588 | 0.00235083 | 0.00242495 | 0.00263157 | 0.00268459 | 0.97836274 |
| 2.8  | 0.00203591 | 0.00207838 | 0.00216827 | 0.00218037 | 0.00227266 | 0.00234472 | 0.00254567 | 0.00259725 | 0.97832669 |
| 2.81 | 0.00196701 | 0.00200828 | 0.00209563 | 0.00210738 | 0.0021971  | 0.00226715 | 0.00246258 | 0.00251276 | 0.97829062 |
| 2.82 | 0.00190044 | 0.00194054 | 0.00202542 | 0.00203684 | 0.00212404 | 0.00219215 | 0.0023822  | 0.00243101 | 0.97825451 |
| 2.83 | 0.00183613 | 0.00187509 | 0.00195756 | 0.00196866 | 0.00205342 | 0.00211963 | 0.00230444 | 0.00235192 | 0.97821837 |
| 2.84 | 0.00177399 | 0.00181184 | 0.00189198 | 0.00190277 | 0.00198514 | 0.00204951 | 0.00222922 | 0.00227541 | 0.97818221 |
| 2.85 | 0.00171396 | 0.00175072 | 0.00182859 | 0.00183908 | 0.00191913 | 0.0019817  | 0.00215646 | 0.00220138 | 0.97814601 |
| 2.86 | 0.00165596 | 0.00169167 | 0.00176733 | 0.00177752 | 0.00185532 | 0.00191614 | 0.00208607 | 0.00212976 | 0.97810979 |
| 2.87 | 0.00159992 | 0.00163461 | 0.00170812 | 0.00171802 | 0.00179363 | 0.00185275 | 0.00201798 | 0.00206048 | 0.97807353 |
| 2.88 | 0.00154578 | 0.00157948 | 0.00165089 | 0.00166051 | 0.00173399 | 0.00179146 | 0.00195211 | 0.00199344 | 0.97803725 |
| 2.89 | 0.00149347 | 0.0015262  | 0.00159558 | 0.00160493 | 0.00167634 | 0.00173219 | 0.00188839 | 0.00192859 | 0.97800093 |
| 2.9  | 0.00144293 | 0.00147472 | 0.00154213 | 0.00155121 | 0.0016206  | 0.00167489 | 0.00182675 | 0.00186585 | 0.97796459 |
| 2.91 | 0.0013941  | 0.00142498 | 0.00149046 | 0.00149928 | 0.00156671 | 0.00161948 | 0.00176713 | 0.00180515 | 0.97792821 |
| 2.92 | 0.00134692 | 0.00137692 | 0.00144053 | 0.0014491  | 0.00151462 | 0.0015659  | 0.00170945 | 0.00174642 | 0.97789181 |
| 2.93 | 0.00130134 | 0.00133047 | 0.00139227 | 0.00140059 | 0.00146426 | 0.0015141  | 0.00165365 | 0.0016896  | 0.97785537 |
| 2.94 | 0.0012573  | 0.0012856  | 0.00134562 | 0.00135371 | 0.00141557 | 0.00146401 | 0.00159967 | 0.00163464 | 0.97781891 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.95 | 0.00121475 | 0.00124223 | 0.00130054 | 0.0013084  | 0.0013685  | 0.00141557 | 0.00154746 | 0.00158146 | 0.97778241 |
| 2.96 | 0.00117364 | 0.00120033 | 0.00125697 | 0.0012646  | 0.001323   | 0.00136874 | 0.00149695 | 0.00153001 | 0.97774589 |
| 2.97 | 0.00113393 | 0.00115984 | 0.00121486 | 0.00122227 | 0.00127901 | 0.00132346 | 0.00144809 | 0.00148023 | 0.97770934 |
| 2.98 | 0.00109555 | 0.00112072 | 0.00117415 | 0.00118136 | 0.00123648 | 0.00127968 | 0.00140082 | 0.00143208 | 0.97767275 |
| 2.99 | 0.00105848 | 0.00108292 | 0.00113482 | 0.00114182 | 0.00119537 | 0.00123734 | 0.0013551  | 0.00138549 | 0.97763614 |
| 3    | 0.00102266 | 0.00104639 | 0.0010968  | 0.0011036  | 0.00115562 | 0.00119641 | 0.00131087 | 0.00134041 | 0.9775995  |
| 3.01 | 0.00098805 | 0.0010111  | 0.00106005 | 0.00106666 | 0.0011172  | 0.00115683 | 0.00126808 | 0.0012968  | 0.97756283 |
| 3.02 | 0.00095461 | 0.00097699 | 0.00102454 | 0.00103095 | 0.00108005 | 0.00111856 | 0.00122669 | 0.00125462 | 0.97752613 |
| 3.03 | 0.00092231 | 0.00094404 | 0.00099021 | 0.00099644 | 0.00104414 | 0.00108155 | 0.00118665 | 0.0012138  | 0.97748939 |
| 3.04 | 0.0008911  | 0.0009122  | 0.00095704 | 0.00096309 | 0.00100942 | 0.00104577 | 0.00114791 | 0.00117431 | 0.97745263 |
| 3.05 | 0.00086094 | 0.00088143 | 0.00092497 | 0.00093085 | 0.00097586 | 0.00101118 | 0.00111044 | 0.00113611 | 0.97741584 |
| 3.06 | 0.00083181 | 0.0008517  | 0.00089399 | 0.00089969 | 0.00094341 | 0.00097772 | 0.0010742  | 0.00109915 | 0.97737902 |
| 3.07 | 0.00080366 | 0.00082297 | 0.00086403 | 0.00086958 | 0.00091204 | 0.00094538 | 0.00103914 | 0.00106339 | 0.97734217 |
| 3.08 | 0.00077646 | 0.00079521 | 0.00083509 | 0.00084047 | 0.00088172 | 0.0009141  | 0.00100522 | 0.00102879 | 0.9773053  |
| 3.09 | 0.00075019 | 0.00076839 | 0.00080711 | 0.00081234 | 0.0008524  | 0.00088386 | 0.00097241 | 0.00099532 | 0.97726839 |
| 3.1  | 0.0007248  | 0.00074247 | 0.00078007 | 0.00078515 | 0.00082406 | 0.00085462 | 0.00094067 | 0.00096294 | 0.97723145 |
| 3.11 | 0.00070027 | 0.00071743 | 0.00075393 | 0.00075887 | 0.00079666 | 0.00082635 | 0.00090996 | 0.00093161 | 0.97719448 |
| 3.12 | 0.00067657 | 0.00069323 | 0.00072868 | 0.00073346 | 0.00077017 | 0.00079901 | 0.00088026 | 0.00090131 | 0.97715749 |
| 3.13 | 0.00065368 | 0.00066985 | 0.00070426 | 0.00070891 | 0.00074456 | 0.00077258 | 0.00085153 | 0.00087198 | 0.97712046 |
| 3.14 | 0.00063156 | 0.00064725 | 0.00068067 | 0.00068518 | 0.0007198  | 0.00074702 | 0.00082373 | 0.00084362 | 0.97708341 |
| 3.15 | 0.00061018 | 0.00062542 | 0.00065786 | 0.00066225 | 0.00069587 | 0.00072231 | 0.00079685 | 0.00081617 | 0.97704632 |
| 3.16 | 0.00058953 | 0.00060433 | 0.00063582 | 0.00064008 | 0.00067273 | 0.00069841 | 0.00077084 | 0.00078962 | 0.97700921 |
| 3.17 | 0.00056958 | 0.00058394 | 0.00061452 | 0.00061866 | 0.00065036 | 0.0006753  | 0.00074568 | 0.00076393 | 0.97697207 |
| 3.18 | 0.00055031 | 0.00056424 | 0.00059393 | 0.00059795 | 0.00062874 | 0.00065296 | 0.00072134 | 0.00073908 | 0.9769349  |
| 3.19 | 0.00053169 | 0.00054521 | 0.00057404 | 0.00057793 | 0.00060783 | 0.00063136 | 0.00069779 | 0.00071503 | 0.9768977  |
| 3.2  | 0.00051369 | 0.00052682 | 0.00055548 | 0.00055859 | 0.00058762 | 0.00061047 | 0.00067502 | 0.00069177 | 0.97686046 |
| 3.21 | 0.00049631 | 0.00050905 | 0.00053622 | 0.00053989 | 0.00056808 | 0.00059028 | 0.00065298 | 0.00066927 | 0.97682321 |
| 3.22 | 0.00047951 | 0.00049188 | 0.00051825 | 0.00052182 | 0.00054919 | 0.00057075 | 0.00063167 | 0.00064749 | 0.97678592 |
| 3.23 | 0.00046329 | 0.00047529 | 0.00050089 | 0.00050435 | 0.00053093 | 0.00055187 | 0.00061105 | 0.00062643 | 0.9767486  |
| 3.24 | 0.00044761 | 0.00045926 | 0.00048411 | 0.00048747 | 0.00051328 | 0.00053361 | 0.00059111 | 0.00060605 | 0.97671125 |
| 3.25 | 0.00043246 | 0.00044377 | 0.00046789 | 0.00047115 | 0.00049621 | 0.00051596 | 0.00057181 | 0.00058633 | 0.97667388 |
| 3.26 | 0.00041783 | 0.0004288  | 0.00045221 | 0.00045538 | 0.00047971 | 0.00049889 | 0.00055315 | 0.00056726 | 0.97663647 |
| 3.27 | 0.00040369 | 0.00041434 | 0.00043706 | 0.00044014 | 0.00046376 | 0.00048238 | 0.00053509 | 0.0005488  | 0.97659904 |
| 3.28 | 0.00039003 | 0.00040036 | 0.00042242 | 0.00042541 | 0.00044834 | 0.00046643 | 0.00051763 | 0.00053095 | 0.97656157 |
| 3.29 | 0.00037683 | 0.00038686 | 0.00040827 | 0.00041117 | 0.00043344 | 0.000451   | 0.00050073 | 0.00051367 | 0.97652408 |
| 3.3  | 0.00036407 | 0.00037381 | 0.00039459 | 0.0003974  | 0.00041902 | 0.00043608 | 0.00048439 | 0.00049696 | 0.97648656 |
| 3.31 | 0.00035175 | 0.0003612  | 0.00038137 | 0.0003841  | 0.00040509 | 0.00042165 | 0.00046858 | 0.0004808  | 0.97644901 |
| 3.32 | 0.00033985 | 0.00034902 | 0.00036859 | 0.00037124 | 0.00039162 | 0.0004077  | 0.00045328 | 0.00046515 | 0.97641143 |
| 3.33 | 0.00032835 | 0.00033724 | 0.00035624 | 0.00035882 | 0.0003786  | 0.00039421 | 0.00043849 | 0.00045002 | 0.97637383 |
| 3.34 | 0.00031724 | 0.00032587 | 0.00034431 | 0.00034681 | 0.00036601 | 0.00038117 | 0.00042417 | 0.00043538 | 0.97633619 |
| 3.35 | 0.0003065  | 0.00031488 | 0.00033277 | 0.0003352  | 0.00035384 | 0.00036856 | 0.00041033 | 0.00042122 | 0.97629852 |



|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 3.36 | 0.00029613 | 0.00030426 | 0.00032162 | 0.00032398 | 0.00034208 | 0.00035637 | 0.00039693 | 0.00040751 | 0.97626083 |
| 3.37 | 0.00028611 | 0.00029399 | 0.00031085 | 0.00031313 | 0.0003307  | 0.00034458 | 0.00038398 | 0.00039426 | 0.97622311 |
| 3.38 | 0.00027643 | 0.00028408 | 0.00030043 | 0.00030265 | 0.00031971 | 0.00033318 | 0.00037144 | 0.00038143 | 0.97618535 |
| 3.39 | 0.00026707 | 0.0002745  | 0.00029037 | 0.00029252 | 0.00030908 | 0.00032216 | 0.00035932 | 0.00036902 | 0.97614757 |
| 3.4  | 0.00025803 | 0.00026524 | 0.00028064 | 0.00028273 | 0.0002988  | 0.0003115  | 0.00034759 | 0.00035701 | 0.97610976 |
| 3.41 | 0.0002493  | 0.00025629 | 0.00027124 | 0.00027327 | 0.00028886 | 0.00030119 | 0.00033625 | 0.0003454  | 0.97607193 |
| 3.42 | 0.00024087 | 0.00024765 | 0.00026215 | 0.00026412 | 0.00027926 | 0.00029123 | 0.00032527 | 0.00033416 | 0.97603406 |
| 3.43 | 0.00023271 | 0.00023929 | 0.00025337 | 0.00025528 | 0.00026997 | 0.00028159 | 0.00031465 | 0.00032329 | 0.97599616 |
| 3.44 | 0.00022484 | 0.00023122 | 0.00024488 | 0.00024673 | 0.000261   | 0.00027228 | 0.00030438 | 0.00031277 | 0.97595824 |
| 3.45 | 0.00021723 | 0.00022342 | 0.00023668 | 0.00023848 | 0.00025232 | 0.00026327 | 0.00029445 | 0.0003026  | 0.97592029 |
| 3.46 | 0.00020988 | 0.00021589 | 0.00022875 | 0.00023049 | 0.00024393 | 0.00025456 | 0.00028484 | 0.00029275 | 0.97588231 |
| 3.47 | 0.00020278 | 0.0002086  | 0.00022108 | 0.00022278 | 0.00023582 | 0.00024614 | 0.00027554 | 0.00028323 | 0.9758443  |
| 3.48 | 0.00019591 | 0.00020157 | 0.00021368 | 0.00021532 | 0.00022798 | 0.000238   | 0.00026655 | 0.00027402 | 0.97580626 |
| 3.49 | 0.00018928 | 0.00019477 | 0.00020652 | 0.00020811 | 0.0002204  | 0.00023012 | 0.00025785 | 0.0002651  | 0.97576819 |
| 3.5  | 0.0001829  | 0.0001882  | 0.0001996  | 0.0002011  | 0.0002131  | 0.0002225  | 0.0002494  | 0.0002565  | 0.97573009 |

Tabla 36 Multiorden para  $0 \geq n \geq 3.5$ ;  $n \neq 1$  a  $80^\circ$  C. Análisis completo.

| t (s)        | 0                         | 21600      | 86400      | 108000     | 172800     | 194400     | 259200     | 280800     | r          |
|--------------|---------------------------|------------|------------|------------|------------|------------|------------|------------|------------|
| Experimental | 31.5925645                | 30.714171  | 27.7928471 | 27.02758   | 25.6234812 | 24.8648686 | 22.7287753 | 21.6640559 |            |
| n            | C <sup>n</sup> (1-n)(ppm) |            |            |            |            |            |            |            |            |
| 0.79         | 2.06496562                | 2.05277404 | 2.0101383  | 1.99838658 | 1.97612316 | 1.96369076 | 1.92699668 | 1.90767923 | 0.99579601 |
| 0.78         | 2.13751255                | 2.12429357 | 2.07809438 | 2.06536863 | 2.0412697  | 2.02781792 | 1.98813892 | 1.96726447 | 0.99579596 |
| 0.8          | 1.99488092                | 1.98366239 | 1.94440446 | 1.93357683 | 1.91305575 | 1.90159153 | 1.86773478 | 1.84989873 | 0.99579571 |
| 0.77         | 2.21260823                | 2.19830488 | 2.14834784 | 2.13459578 | 2.10856392 | 2.09403926 | 2.05122116 | 2.02871082 | 0.99579555 |
| 0.81         | 1.92717489                | 1.91687755 | 1.88082019 | 1.87086892 | 1.85200112 | 1.84145611 | 1.8102954  | 1.7938683  | 0.99579504 |
| 0.76         | 2.29034218                | 2.27489477 | 2.22097632 | 2.2061433  | 2.17807661 | 2.16242314 | 2.11630495 | 2.09207642 | 0.99579478 |
| 0.82         | 1.86176679                | 1.85234119 | 1.81931519 | 1.8101947  | 1.79289503 | 1.7832224  | 1.75462247 | 1.73953495 | 0.99579402 |
| 0.75         | 2.37080711                | 2.35415308 | 2.29606014 | 2.28008895 | 2.24988092 | 2.2330402  | 2.18345381 | 2.1574212  | 0.99579366 |
| 0.83         | 1.79857863                | 1.7899776  | 1.75982149 | 1.75148821 | 1.7356753  | 1.72683025 | 1.70066168 | 1.68684726 | 0.99579265 |
| 0.74         | 2.45409895                | 2.43617279 | 2.37368229 | 2.35651312 | 2.32405239 | 2.30596337 | 2.25273325 | 2.22480699 | 0.99579218 |
| 0.84         | 1.73753508                | 1.72971363 | 1.70227329 | 1.69468563 | 1.68028171 | 1.67222144 | 1.64836037 | 1.6357554  | 0.99579091 |
| 0.73         | 2.54031702                | 2.52105009 | 2.45392859 | 2.43549888 | 2.40066906 | 2.38126794 | 2.32421088 | 2.29429753 | 0.99579034 |
| 0.85         | 1.67856333                | 1.6714786  | 1.64660699 | 1.63972521 | 1.626656   | 1.61933956 | 1.59766752 | 1.58621103 | 0.99578882 |
| 0.72         | 2.62956413                | 2.60888456 | 2.53688774 | 2.51713208 | 2.47981154 | 2.4590317  | 2.39795644 | 2.36595857 | 0.99578815 |
| 0.86         | 1.62159308                | 1.61520419 | 1.59276104 | 1.58654722 | 1.57474174 | 1.56813    | 1.54853364 | 1.53816728 | 0.99578637 |
| 0.71         | 2.72194669                | 2.69977923 | 2.62265147 | 2.60150148 | 2.5615631  | 2.53933494 | 2.4740419  | 2.4398579  | 0.9957856  |
| 0.87         | 1.5665564                 | 1.56082439 | 1.54067592 | 1.53509385 | 1.5244843  | 1.51853988 | 1.50091081 | 1.49157869 | 0.99578356 |
| 0.7          | 2.81757486                | 2.7938407  | 2.71131459 | 2.68869877 | 2.64600975 | 2.62226061 | 2.55254149 | 2.51606543 | 0.99578269 |
| 0.88         | 1.51338765                | 1.50827543 | 1.49029404 | 1.48530916 | 1.47583082 | 1.47051798 | 1.45475254 | 1.4464012  | 0.99578039 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.69 | 2.91656267 | 2.89117931 | 2.80297511 | 2.77881875 | 2.73324034 | 2.70789433 | 2.63353182 | 2.59465326 | 0.99577943 |
| 0.89 | 1.46202344 | 1.45749565 | 1.4415597  | 1.43713904 | 1.4287301  | 1.42401472 | 1.4100138  | 1.40259205 | 0.99577687 |
| 0.68 | 3.01902815 | 2.99190924 | 2.89773437 | 2.87195937 | 2.82334664 | 2.79632454 | 2.71709192 | 2.67569573 | 0.99577581 |
| 0.9  | 1.41240253 | 1.4084255  | 1.39441904 | 1.39053113 | 1.38313259 | 1.37898206 | 1.36665094 | 1.36010982 | 0.99577299 |
| 0.67 | 3.12509346 | 3.09614865 | 2.99569712 | 2.96822189 | 2.91642347 | 2.88764257 | 2.80330332 | 2.75926952 | 0.99577183 |
| 0.91 | 1.36446575 | 1.36100742 | 1.34881993 | 1.34543476 | 1.3389903  | 1.33537351 | 1.32462163 | 1.31891431 | 0.99576874 |
| 0.66 | 3.2348851  | 3.2040198  | 3.09697167 | 3.06771094 | 3.01256874 | 2.98194272 | 2.89225015 | 2.84545368 | 0.9957675  |
| 0.92 | 1.31815594 | 1.31518578 | 1.30471196 | 1.30180092 | 1.29625681 | 1.29314401 | 1.28388488 | 1.27896654 | 0.99576415 |
| 0.65 | 3.34853396 | 3.31564923 | 3.20166997 | 3.17053467 | 3.11188362 | 3.07932239 | 2.98401919 | 2.93432976 | 0.99576281 |
| 0.93 | 1.27341787 | 1.27090684 | 1.26204637 | 1.25958216 | 1.25488714 | 1.25224998 | 1.24440092 | 1.24022872 | 0.99575919 |
| 0.64 | 3.46617557 | 3.43116787 | 3.30990778 | 3.27680485 | 3.2144726  | 3.17988212 | 3.07870001 | 3.02598183 | 0.99575777 |
| 0.94 | 1.23019822 | 1.22811865 | 1.220776   | 1.2187326  | 1.21483778 | 1.21264916 | 1.20613123 | 1.20266421 | 0.99575387 |
| 0.63 | 3.58795019 | 3.55071124 | 3.42180474 | 3.38663701 | 3.32044361 | 3.28372578 | 3.17638497 | 3.1204966  | 0.99575237 |
| 0.95 | 1.18844543 | 1.18677104 | 1.18085521 | 1.17920784 | 1.17606657 | 1.17430067 | 1.16903847 | 1.16623746 | 0.9957482  |
| 0.62 | 3.71400304 | 3.67441955 | 3.53748457 | 3.50015052 | 3.42990815 | 3.3909606  | 3.27716942 | 3.21796348 | 0.99574661 |
| 0.96 | 1.14810972 | 1.14681549 | 1.14223989 | 1.14096491 | 1.13853274 | 1.1371649  | 1.13308644 | 1.13091403 | 0.99574217 |
| 0.61 | 3.8444844  | 3.80243791 | 3.65707515 | 3.61746879 | 3.5429814  | 3.50169734 | 3.38115168 | 3.31847469 | 0.9957405  |
| 0.97 | 1.10914301 | 1.10820515 | 1.10488732 | 1.10396223 | 1.1021968  | 1.10120351 | 1.09824006 | 1.09666048 | 0.99573578 |
| 0.6  | 3.97954988 | 3.93491648 | 3.78070869 | 3.73871934 | 3.65978231 | 3.61605034 | 3.48843322 | 3.4221253  | 0.99573403 |
| 0.98 | 1.07149882 | 1.07089472 | 1.06875623 | 1.06815959 | 1.0670205  | 1.06637934 | 1.06446533 | 1.06344442 | 0.99572903 |
| 0.59 | 4.11936051 | 4.07201067 | 3.90852186 | 3.86403397 | 3.78043377 | 3.7341377  | 3.59911874 | 3.52901338 | 0.99572721 |
| 0.99 | 1.03513227 | 1.03484043 | 1.03380667 | 1.03351806 | 1.03296684 | 1.03265645 | 1.03172929 | 1.03123441 | 0.99572192 |
| 0.58 | 4.264083   | 4.21388127 | 4.04065597 | 3.99354891 | 3.90506274 | 3.85608138 | 3.71331622 | 3.63924004 | 0.99572003 |
| 0.57 | 4.41388993 | 4.36069471 | 4.1772571  | 4.12740494 | 4.03380033 | 3.98200731 | 3.83113711 | 3.75290957 | 0.9957125  |
| 1.01 | 0.96606011 | 0.96633256 | 0.96729885 | 0.96756896 | 0.96808528 | 0.96837627 | 0.9692465  | 0.96971163 | 0.99570663 |
| 0.56 | 4.56895991 | 4.51262319 | 4.31847626 | 4.26574756 | 4.16678199 | 4.11204553 | 3.95269638 | 3.8701295  | 0.99570461 |
| 1.02 | 0.93327214 | 0.93379861 | 0.93566706 | 0.9361897  | 0.93718912 | 0.9377526  | 0.93943877 | 0.94034064 | 0.99569844 |
| 0.55 | 4.72947786 | 4.66984492 | 4.46446957 | 4.40872716 | 4.30414764 | 4.24633033 | 4.07811263 | 3.99101073 | 0.99569637 |
| 1.03 | 0.90159699 | 0.90236    | 0.90506966 | 0.90582809 | 0.90727899 | 0.90809736 | 0.91054774 | 0.91185925 | 0.9956899  |
| 0.54 | 4.89563516 | 4.83254433 | 4.61539842 | 4.55649915 | 4.4460418  | 4.38500041 | 4.20750825 | 4.11566761 | 0.99568777 |
| 1.04 | 0.87099689 | 0.87197985 | 0.87547284 | 0.87645115 | 0.87832344 | 0.87937994 | 0.8825452  | 0.88424051 | 0.995681   |
| 0.53 | 5.06762995 | 5.00091226 | 4.77142968 | 4.70922418 | 4.59261376 | 4.52819895 | 4.3410095  | 4.24421807 | 0.99567882 |
| 1.05 | 0.84143535 | 0.84262252 | 0.84684387 | 0.84802693 | 0.850292   | 0.85157066 | 0.85540385 | 0.85745831 | 0.99567174 |
| 0.52 | 5.2456673  | 5.17514619 | 4.93273583 | 4.86706826 | 4.74401773 | 4.67607385 | 4.47874666 | 4.37678374 | 0.99566952 |
| 1.06 | 0.81287713 | 0.81425357 | 0.8191511  | 0.82052453 | 0.82315517 | 0.82464082 | 0.82909718 | 0.83148729 | 0.99566212 |
| 0.51 | 5.42995951 | 5.35545051 | 5.09949521 | 5.03020297 | 4.90041302 | 4.82877782 | 4.62085411 | 4.51349001 | 0.99565986 |
| 1.07 | 0.78528818 | 0.78683974 | 0.79236391 | 0.79391407 | 0.79688441 | 0.7985626  | 0.80359954 | 0.80630289 | 0.99565215 |
| 0.5  | 5.62072633 | 5.54203672 | 5.27189217 | 5.19880563 | 5.06196417 | 4.98646855 | 4.76747053 | 4.65446623 | 0.99564985 |
| 1.08 | 0.75863558 | 0.76034885 | 0.7664527  | 0.76816661 | 0.77145207 | 0.77330907 | 0.77888603 | 0.78188129 | 0.99564181 |
| 0.49 | 5.81819522 | 5.73512366 | 5.4501173  | 5.37305953 | 5.22884114 | 5.14930891 | 4.91873899 | 4.79984575 | 0.99563948 |
| 1.09 | 0.73288758 | 0.73474985 | 0.74138881 | 0.74325417 | 0.7468314  | 0.74885416 | 0.75493256 | 0.75819937 | 0.99563112 |
| 0.48 | 6.02260164 | 5.93493784 | 5.63436762 | 5.55315408 | 5.40121953 | 5.31746706 | 5.07480709 | 4.94976612 | 0.99562876 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.1  | 0.70801346 | 0.71001271 | 0.71714454 | 0.71914967 | 0.72299649 | 0.72517259 | 0.73171574 | 0.73523475 | 0.99562006 |
| 0.47 | 6.23418932 | 6.14171363 | 5.82484683 | 5.73928505 | 5.57928068 | 5.49111665 | 5.23582712 | 5.10436917 | 0.99561768 |
| 1.11 | 0.68398356 | 0.68610839 | 0.69369309 | 0.6958269  | 0.69992226 | 0.70223993 | 0.70921292 | 0.71296568 | 0.99560865 |
| 0.46 | 6.45321056 | 6.35569358 | 6.02176551 | 5.93165477 | 5.76321195 | 5.67043702 | 5.40195621 | 5.26380115 | 0.99560626 |
| 1.12 | 0.66076924 | 0.66300888 | 0.67100852 | 0.67326051 | 0.67758444 | 0.68003249 | 0.68740213 | 0.69137111 | 0.99559688 |
| 0.45 | 6.67992651 | 6.57712868 | 6.22534136 | 6.13047236 | 5.95320686 | 5.85561336 | 5.57335645 | 5.42821289 | 0.99559448 |
| 1.13 | 0.6383428  | 0.64068707 | 0.64906577 | 0.65142597 | 0.65595952 | 0.65852732 | 0.66626211 | 0.6704306  | 0.99558475 |
| 0.44 | 6.9146075  | 6.80627867 | 6.43579943 | 6.33595392 | 6.14946529 | 6.0468369  | 5.75019509 | 5.59775994 | 0.99558234 |
| 1.14 | 0.61667752 | 0.61911677 | 0.62784057 | 0.63029955 | 0.63502476 | 0.63770223 | 0.64577221 | 0.65012435 | 0.99557226 |
| 0.43 | 7.15753338 | 7.04341235 | 6.65337239 | 6.54832283 | 6.35219375 | 6.24430512 | 5.93264471 | 5.77260269 | 0.99556985 |
| 1.15 | 0.59574755 | 0.59827269 | 0.60730946 | 0.60985828 | 0.61475813 | 0.61753571 | 0.62591246 | 0.63043314 | 0.99555941 |
| 0.42 | 7.40899379 | 7.28880787 | 6.87830076 | 6.76780993 | 6.56160552 | 6.44822196 | 6.12088331 | 5.95290655 | 0.99555701 |
| 1.16 | 0.57552795 | 0.57813038 | 0.58744974 | 0.59007994 | 0.5951383  | 0.59800692 | 0.60666346 | 0.61133835 | 0.99554621 |
| 0.41 | 7.66928858 | 7.54275307 | 7.11083321 | 6.99465382 | 6.77792094 | 6.65879799 | 6.3150946  | 6.1388421  | 0.99554382 |
| 1.17 | 0.5559946  | 0.55866621 | 0.56823945 | 0.57094304 | 0.57614463 | 0.57909571 | 0.58800643 | 0.5928219  | 0.99553264 |
| 0.4  | 7.93872811 | 7.80554584 | 7.35122681 | 7.22910107 | 7.00136759 | 6.87625069 | 6.51546807 | 6.33058523 | 0.99553028 |
| 1.18 | 0.5371242  | 0.53985735 | 0.54965737 | 0.55242676 | 0.55775714 | 0.56078255 | 0.56992317 | 0.57486629 | 0.99551872 |
| 0.39 | 8.21763367 | 8.07749441 | 7.59974732 | 7.47140654 | 7.23218057 | 7.10080462 | 6.72219926 | 6.52831735 | 0.99551638 |
| 1.19 | 0.51889427 | 0.52168173 | 0.53168294 | 0.53451099 | 0.53995648 | 0.54304851 | 0.55239604 | 0.55745452 | 0.99550443 |
| 0.38 | 8.50633782 | 8.3589178  | 7.85666948 | 7.72183362 | 7.47060273 | 7.33269169 | 6.93548987 | 6.73222552 | 0.99550213 |
| 1.2  | 0.50128305 | 0.50411804 | 0.51429629 | 0.51717624 | 0.52272392 | 0.52587529 | 0.53540792 | 0.54057013 | 0.99548979 |
| 0.37 | 8.80518479 | 8.65014609 | 8.12227732 | 7.98065453 | 7.71688492 | 7.57215136 | 7.15554805 | 6.94250264 | 0.99548753 |
| 1.21 | 0.48426956 | 0.48714568 | 0.49747821 | 0.50040368 | 0.50604133 | 0.50924515 | 0.51894225 | 0.52419714 | 0.99547479 |
| 0.36 | 9.11453094 | 8.95152091 | 8.39686448 | 8.24815062 | 7.97128625 | 7.81943094 | 7.38258851 | 7.15934764 | 0.99547258 |
| 1.22 | 0.46783351 | 0.47074473 | 0.4812101  | 0.48417507 | 0.48989117 | 0.49314092 | 0.50298296 | 0.50832006 | 0.99545943 |
| 0.35 | 9.43474513 | 9.26339575 | 8.68073452 | 8.52461266 | 8.23407439 | 8.07478579 | 7.61683281 | 7.38296566 | 0.99545727 |
| 1.23 | 0.45195529 | 0.45489596 | 0.46547397 | 0.46847277 | 0.47425643 | 0.47754597 | 0.48751447 | 0.49292387 | 0.99544371 |
| 0.34 | 9.76620916 | 9.58613645 | 8.97420125 | 8.81034117 | 8.50552583 | 8.33847962 | 7.85850951 | 7.61356827 | 0.99544162 |
| 1.24 | 0.43661598 | 0.43958077 | 0.45025244 | 0.45327971 | 0.45912067 | 0.46244418 | 0.47252169 | 0.47799401 | 0.99542764 |
| 0.33 | 10.1093183 | 9.92012157 | 9.27758912 | 9.10564675 | 8.78592616 | 8.61078476 | 8.10785445 | 7.85137361 | 0.99542561 |
| 1.25 | 0.42179728 | 0.42478121 | 0.43552866 | 0.43857938 | 0.44446797 | 0.44781997 | 0.45799    | 0.46351635 | 0.9954112  |
| 0.32 | 10.4644816 | 10.2657429 | 9.59123353 | 9.4108504  | 9.07557041 | 8.89198241 | 8.36511092 | 8.09660667 | 0.99540926 |
| 1.26 | 0.40748153 | 0.41047992 | 0.42128637 | 0.4243558  | 0.4302829  | 0.43365823 | 0.4439052  | 0.44947719 | 0.99539441 |
| 0.31 | 10.8321226 | 10.6234058 | 9.91548121 | 9.72628388 | 9.37476331 | 9.18236299 | 8.63052996 | 8.34949943 | 0.99539255 |
| 1.27 | 0.39365166 | 0.39666011 | 0.40750982 | 0.4105935  | 0.41655054 | 0.41994434 | 0.43025356 | 0.43586326 | 0.99537725 |
| 0.3  | 11.2126797 | 10.9935298 | 10.2506906 | 10.0522901 | 9.68381966 | 9.48222636 | 8.90437055 | 8.61029115 | 0.99537549 |
| 1.28 | 0.38029116 | 0.38330558 | 0.39418378 | 0.39727752 | 0.40325645 | 0.40666414 | 0.41702175 | 0.42266167 | 0.99535974 |
| 0.29 | 11.6066066 | 11.3765491 | 10.5972323 | 10.3892234 | 10.0030646 | 9.7918822  | 9.18689991 | 8.87922855 | 0.99535808 |
| 1.29 | 0.36738412 | 0.37040066 | 0.38129352 | 0.3843934  | 0.39038664 | 0.3938039  | 0.40419687 | 0.40985994 | 0.99534187 |
| 0.28 | 12.0143731 | 11.772913  | 10.9554895 | 10.73745   | 10.3328341 | 10.1116503 | 9.47839373 | 9.15656605 | 0.99534032 |
| 1.3  | 0.35491515 | 0.35793021 | 0.36882478 | 0.37192712 | 0.37792756 | 0.38135035 | 0.3917664  | 0.39744594 | 0.99532364 |
| 0.27 | 12.4364653 | 12.1830863 | 11.3258581 | 11.0973486 | 10.673475  | 10.4418609 | 9.77913644 | 9.44256602 | 0.99532221 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.31 | 0.34286937 | 0.34587962 | 0.35676378 | 0.35986514 | 0.36586611 | 0.36929063 | 0.37971821 | 0.38540795 | 0.99530505 |
| 0.26 | 12.8733866 | 12.6075503 | 11.7087477 | 11.4693102 | 11.0253458 | 10.782855  | 10.0894215 | 9.73749904 | 0.99530375 |
| 1.32 | 0.33123242 | 0.33423474 | 0.34509719 | 0.34819434 | 0.35418959 | 0.35761228 | 0.36804055 | 0.37373457 | 0.99528611 |
| 0.25 | 13.3256579 | 13.0468028 | 12.1045815 | 11.8537393 | 11.3888166 | 11.1349848 | 10.4095517 | 10.0416441 | 0.99528495 |
| 1.33 | 0.31999043 | 0.32298191 | 0.33381212 | 0.33690204 | 0.34288573 | 0.34630325 | 0.35672201 | 0.36241476 | 0.99526668 |
| 0.24 | 13.7938186 | 13.501359  | 12.5137971 | 12.2510537 | 11.7642699 | 11.4986138 | 10.7398394 | 10.355289  | 0.99526579 |
| 1.34 | 0.30912999 | 0.31210793 | 0.32289608 | 0.32597595 | 0.33194263 | 0.33535185 | 0.34575156 | 0.35143781 | 0.99524714 |
| 0.23 | 14.2784268 | 13.9717522 | 12.9368469 | 12.6616853 | 12.1521008 | 11.8741177 | 11.0806069 | 10.6787304 | 0.99524628 |
| 1.35 | 0.29863815 | 0.30160006 | 0.312337   | 0.31540422 | 0.32134878 | 0.32474677 | 0.33511849 | 0.34079333 | 0.99522712 |
| 0.22 | 14.7800603 | 14.458534  | 13.3741986 | 13.0860804 | 12.5527172 | 12.2618842 | 11.4321867 | 11.0122742 | 0.99522643 |
| 1.36 | 0.28850241 | 0.29144596 | 0.30212322 | 0.30517533 | 0.31109302 | 0.31447707 | 0.32481242 | 0.33047125 | 0.99520674 |
| 0.21 | 15.2993174 | 14.9622756 | 13.8263358 | 13.5247005 | 12.9665406 | 12.6623138 | 11.7949219 | 11.3562362 | 0.99520622 |
| 1.37 | 0.27871067 | 0.28163372 | 0.29224344 | 0.29527818 | 0.30116458 | 0.30453213 | 0.3148233  | 0.32046181 | 0.995186   |
| 0.2  | 15.8368172 | 15.4835677 | 14.2937582 | 13.9780223 | 13.3940065 | 13.0758201 | 12.1691664 | 11.7109416 | 0.99518567 |
| 1.38 | 0.26925126 | 0.27215183 | 0.28268675 | 0.285702   | 0.291553   | 0.29490169 | 0.30514138 | 0.31075555 | 0.9951649  |
| 0.19 | 16.3932006 | 16.0230219 | 14.7769825 | 14.4465385 | 13.8355646 | 13.5028299 | 12.5552854 | 12.076726  | 0.99516477 |
| 0.18 | 16.969131  | 16.5812709 | 15.2765431 | 14.9307585 | 14.2916795 | 13.9437844 | 12.9536557 | 12.4539354 | 0.99514352 |
| 1.39 | 0.2601129  | 0.26298917 | 0.27344256 | 0.27643639 | 0.28224817 | 0.28557579 | 0.29575721 | 0.30134327 | 0.99514345 |
| 0.17 | 17.5652951 | 17.1589695 | 15.7929922 | 15.4312087 | 14.7628311 | 14.3991389 | 13.364666  | 12.8429268 | 0.99512192 |
| 1.4  | 0.2512847  | 0.254135   | 0.26450068 | 0.26747127 | 0.2732403  | 0.27654482 | 0.28666164 | 0.29221607 | 0.99512163 |
| 0.16 | 18.1824039 | 17.7567954 | 16.3269007 | 15.9484329 | 15.249515  | 14.8693636 | 13.7887174 | 13.2440681 | 0.99509998 |
| 1.41 | 0.24275613 | 0.24557892 | 0.2558512  | 0.2587969  | 0.26451991 | 0.26779944 | 0.27784579 | 0.28336532 | 0.99509946 |
| 0.15 | 18.821193  | 18.3754498 | 16.8788589 | 16.4829935 | 15.7522434 | 15.3549442 | 14.2262236 | 13.6577388 | 0.99507769 |
| 1.42 | 0.23451701 | 0.23731091 | 0.24748457 | 0.25040384 | 0.25607783 | 0.25933063 | 0.26930106 | 0.27478264 | 0.99507693 |
| 0.14 | 19.4824243 | 19.0156583 | 17.4494769 | 17.0354715 | 16.2715451 | 15.8563822 | 14.6776116 | 14.0843302 | 0.99505505 |
| 1.43 | 0.22655753 | 0.22932126 | 0.23939154 | 0.24228299 | 0.24790518 | 0.25112962 | 0.26101911 | 0.26645992 | 0.99505404 |
| 0.13 | 20.1668861 | 19.6781721 | 18.0393856 | 17.6064675 | 16.8079666 | 16.3741953 | 15.1433218 | 14.524246  | 0.99503206 |
| 1.44 | 0.21886819 | 0.2216006  | 0.23156316 | 0.2344255  | 0.23999336 | 0.24318797 | 0.25299186 | 0.25838929 | 0.9950308  |
| 0.12 | 20.8753947 | 20.3637681 | 18.6492372 | 18.1966022 | 17.3620722 | 16.9089184 | 15.6238086 | 14.9779024 | 0.99500873 |
| 1.45 | 0.21143983 | 0.21413987 | 0.22399078 | 0.22682284 | 0.23233404 | 0.23549746 | 0.24521147 | 0.25056309 | 0.9950072  |
| 0.11 | 21.6087947 | 21.0732505 | 19.2797058 | 18.8065171 | 17.9344449 | 17.4611037 | 16.119541  | 15.4457284 | 0.99498505 |
| 1.46 | 0.20426359 | 0.20693033 | 0.21666602 | 0.21946674 | 0.22491916 | 0.22805015 | 0.23767036 | 0.24297395 | 0.99498324 |
| 0.1  | 22.3679608 | 21.8074516 | 19.9314885 | 19.4368751 | 18.5256869 | 18.0313213 | 16.6310026 | 15.9281666 | 0.99496103 |
| 1.47 | 0.1973309  | 0.19996352 | 0.20958079 | 0.2123492  | 0.21774093 | 0.22083835 | 0.23036116 | 0.23561466 | 0.99495892 |
| 0.09 | 23.1537981 | 22.5672326 | 20.6053058 | 20.0883616 | 19.1364203 | 18.6201602 | 17.1586925 | 16.4256736 | 0.99493665 |
| 1.48 | 0.19063352 | 0.19323126 | 0.20272726 | 0.2054625  | 0.21079179 | 0.21385462 | 0.22327675 | 0.22847828 | 0.99493424 |
| 0.08 | 23.9672436 | 23.3534847 | 21.3019026 | 20.7616845 | 19.7672877 | 19.2282286 | 17.7031257 | 16.9387199 | 0.99491194 |
| 1.49 | 0.18416344 | 0.18672565 | 0.19609784 | 0.19879914 | 0.20406443 | 0.20709174 | 0.21641021 | 0.22155804 | 0.99490921 |
| 0.07 | 24.8092673 | 24.1671302 | 22.022049  | 21.457576  | 20.4189527 | 19.8561542 | 18.2648333 | 17.4677909 | 0.99488688 |
| 1.5  | 0.17791295 | 0.18043908 | 0.18968522 | 0.19235187 | 0.19755177 | 0.20054273 | 0.20975484 | 0.21484741 | 0.99488382 |
| 0.06 | 25.6808733 | 25.0091234 | 22.7665412 | 22.1767924 | 21.0921011 | 20.5045857 | 18.8443635 | 18.0133871 | 0.99486147 |
| 1.51 | 0.1718746  | 0.17436416 | 0.18348229 | 0.1861137  | 0.19124697 | 0.19420082 | 0.20330414 | 0.20834003 | 0.99485807 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.05 | 26.5831007 | 25.880452  | 23.5362022 | 22.9201156 | 21.7874411 | 21.1741927 | 19.4422818 | 18.5760247 | 0.99483572 |
| 1.52 | 0.1660412  | 0.16849376 | 0.17748221 | 0.18007784 | 0.18514337 | 0.18805946 | 0.19705183 | 0.20202975 | 0.99483196 |
| 0.04 | 27.5170254 | 26.7821381 | 24.3318828 | 23.6883535 | 22.5057043 | 21.8656666 | 20.0591716 | 19.1562359 | 0.99480962 |
| 1.53 | 0.16040578 | 0.16282101 | 0.17167833 | 0.17423773 | 0.17923457 | 0.18211232 | 0.19099179 | 0.19591059 | 0.9948055  |
| 0.03 | 28.4837611 | 27.7152393 | 25.1544628 | 24.4823412 | 23.2476463 | 22.5797217 | 20.6956349 | 19.7545697 | 0.99478318 |
| 1.54 | 0.15496163 | 0.15733924 | 0.16606425 | 0.16858702 | 0.17351435 | 0.17635325 | 0.18511812 | 0.18997678 | 0.99477868 |
| 0.02 | 29.48      | 28.68      | 26.00      | 25.30      | 24.01      | 23.32      | 21.35      | 20.37      | 0.994756   |
| 1.55 | 0.14970225 | 0.15204203 | 0.16063376 | 0.16311957 | 0.16797669 | 0.1707763  | 0.17942509 | 0.18422269 | 0.9947515  |
| 0.01 | 30.52      | 29.68      | 26.88      | 26.15      | 24.81      | 24.08      | 22.03      | 21.01      | 0.994729   |
| 1.56 | 0.14462137 | 0.14692316 | 0.15538085 | 0.15782943 | 0.16261576 | 0.16537572 | 0.17390714 | 0.17864289 | 0.99472396 |
| 0    | 31.59      | 30.71      | 27.79      | 27.03      | 25.62      | 24.86      | 22.73      | 21.66      | 0.994702   |
| 1.57 | 0.13971294 | 0.14197664 | 0.15029972 | 0.15271086 | 0.15742593 | 0.16014592 | 0.16855889 | 0.17323209 | 0.99469607 |
| 1.58 | 0.13497109 | 0.13719665 | 0.14538474 | 0.14775829 | 0.15240173 | 0.15508151 | 0.16337511 | 0.16798517 | 0.99466783 |
| 1.59 | 0.13039019 | 0.13257759 | 0.1406305  | 0.14296633 | 0.14753787 | 0.15017725 | 0.15835076 | 0.16289717 | 0.99463922 |
| 1.6  | 0.12596476 | 0.12811404 | 0.13603172 | 0.13832979 | 0.14282924 | 0.14542809 | 0.15348091 | 0.15796328 | 0.99461026 |
| 1.61 | 0.12168953 | 0.12380077 | 0.13158332 | 0.13384361 | 0.13827088 | 0.14082911 | 0.14876084 | 0.15317883 | 0.99458094 |
| 1.62 | 0.1175594  | 0.11963271 | 0.1272804  | 0.12950292 | 0.13385801 | 0.13637557 | 0.14418592 | 0.14853929 | 0.99455127 |
| 1.63 | 0.11356945 | 0.11560498 | 0.12311818 | 0.12530301 | 0.12958597 | 0.13206286 | 0.1397517  | 0.14404028 | 0.99452124 |
| 1.64 | 0.10971492 | 0.11171286 | 0.11909207 | 0.1212393  | 0.12545027 | 0.12788654 | 0.13545385 | 0.13967753 | 0.99449085 |
| 1.65 | 0.1059912  | 0.10795177 | 0.11519763 | 0.11730738 | 0.12144656 | 0.12384229 | 0.13128816 | 0.13544693 | 0.99446011 |
| 1.66 | 0.10239387 | 0.10431731 | 0.11143053 | 0.11350298 | 0.11757063 | 0.11992594 | 0.12725059 | 0.13134446 | 0.99442901 |
| 1.67 | 0.09891864 | 0.10080522 | 0.10778662 | 0.10982196 | 0.11381839 | 0.11613343 | 0.12333719 | 0.12736625 | 0.99439756 |
| 1.68 | 0.09556135 | 0.09741136 | 0.10426188 | 0.10626032 | 0.11018591 | 0.11246086 | 0.11954414 | 0.12350853 | 0.99436575 |
| 1.69 | 0.09231801 | 0.09413177 | 0.10085239 | 0.10281419 | 0.10666936 | 0.10890443 | 0.11586774 | 0.11976766 | 0.99433358 |
| 1.7  | 0.08918475 | 0.0909626  | 0.0975544  | 0.09947982 | 0.10326504 | 0.10546046 | 0.1123044  | 0.11614009 | 0.99430106 |
| 1.71 | 0.08615783 | 0.08790012 | 0.09436426 | 0.09625359 | 0.09996936 | 0.10212541 | 0.10885065 | 0.1126224  | 0.99426818 |
| 1.72 | 0.08323364 | 0.08494075 | 0.09127844 | 0.09313198 | 0.09677887 | 0.09889583 | 0.10550311 | 0.10921125 | 0.99423495 |
| 1.73 | 0.0804087  | 0.08208101 | 0.08829353 | 0.09011161 | 0.0936902  | 0.09576837 | 0.10225852 | 0.10590342 | 0.99420137 |
| 1.74 | 0.07767964 | 0.07931755 | 0.08540623 | 0.0871892  | 0.0907001  | 0.09273982 | 0.09911371 | 0.10269577 | 0.99416743 |
| 1.75 | 0.0750432  | 0.07664713 | 0.08261335 | 0.08436157 | 0.08780544 | 0.08980704 | 0.09606562 | 0.09958529 | 0.99413313 |
| 1.76 | 0.07249624 | 0.07406662 | 0.0799118  | 0.08162563 | 0.08500315 | 0.086967   | 0.09311126 | 0.09656901 | 0.99409848 |
| 1.77 | 0.07003573 | 0.07157298 | 0.07729859 | 0.07897843 | 0.0822903  | 0.08421678 | 0.09024776 | 0.09364409 | 0.99406348 |
| 1.78 | 0.06765872 | 0.0691633  | 0.07477084 | 0.07641708 | 0.07966403 | 0.08155353 | 0.08747233 | 0.09080776 | 0.99402812 |
| 1.79 | 0.06536239 | 0.06683475 | 0.07232574 | 0.07393879 | 0.07712157 | 0.07897451 | 0.08478225 | 0.08805734 | 0.9939924  |
| 1.8  | 0.063144   | 0.0645846  | 0.06996061 | 0.07154088 | 0.07466026 | 0.07647704 | 0.0821749  | 0.08539023 | 0.99395634 |
| 1.81 | 0.0610009  | 0.0624102  | 0.06767281 | 0.06922073 | 0.0722775  | 0.07405855 | 0.07964773 | 0.0828039  | 0.99391992 |
| 1.82 | 0.05893054 | 0.06030901 | 0.06545984 | 0.06697583 | 0.06997078 | 0.07171654 | 0.07719828 | 0.0802959  | 0.99388314 |
| 1.83 | 0.05693044 | 0.05827856 | 0.06331922 | 0.06480374 | 0.06773768 | 0.0694486  | 0.07482417 | 0.07786387 | 0.99384601 |
| 1.84 | 0.05499823 | 0.05631647 | 0.06124861 | 0.06270209 | 0.06557586 | 0.06725237 | 0.07252306 | 0.0755055  | 0.99380853 |
| 1.85 | 0.05313159 | 0.05442044 | 0.05924571 | 0.06066859 | 0.06348302 | 0.0651256  | 0.07029272 | 0.07321856 | 0.9937707  |
| 1.86 | 0.05132831 | 0.05258824 | 0.05730831 | 0.05870105 | 0.06145698 | 0.06306609 | 0.06813098 | 0.07100089 | 0.99373251 |
| 1.87 | 0.04958624 | 0.05081773 | 0.05543426 | 0.05679731 | 0.0594956  | 0.0610717  | 0.06603571 | 0.06885039 | 0.99369397 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.88 | 0.04790329 | 0.04910683 | 0.0536215  | 0.05495531 | 0.05759681 | 0.05914039 | 0.06400488 | 0.06676502 | 0.99365508 |
| 1.89 | 0.04627745 | 0.04745352 | 0.05186801 | 0.05317306 | 0.05575863 | 0.05727015 | 0.06203651 | 0.06474282 | 0.99361583 |
| 1.9  | 0.0447068  | 0.04585589 | 0.05017187 | 0.0514486  | 0.05397911 | 0.05545905 | 0.06012867 | 0.06278186 | 0.99357623 |
| 1.91 | 0.04318946 | 0.04431203 | 0.04853119 | 0.04978007 | 0.05225638 | 0.05370523 | 0.0582795  | 0.0608803  | 0.99353628 |
| 1.92 | 0.04172361 | 0.04282016 | 0.04694416 | 0.04816565 | 0.05058863 | 0.05200687 | 0.0564872  | 0.05903634 | 0.99349598 |
| 1.93 | 0.04030752 | 0.04137852 | 0.04540904 | 0.04660359 | 0.04897411 | 0.05036222 | 0.05475002 | 0.05724822 | 0.99345532 |
| 1.94 | 0.03893949 | 0.03998541 | 0.04392411 | 0.04509218 | 0.04741111 | 0.04876958 | 0.05306627 | 0.05551427 | 0.99341432 |
| 1.95 | 0.03761788 | 0.0386392  | 0.04248774 | 0.0436298  | 0.045898   | 0.04722273 | 0.05143429 | 0.05383283 | 0.99337296 |
| 1.96 | 0.03634114 | 0.03733832 | 0.04109834 | 0.04221484 | 0.04443318 | 0.0457338  | 0.04985251 | 0.05220232 | 0.99333125 |
| 1.97 | 0.03510772 | 0.03608123 | 0.03975438 | 0.04084577 | 0.04301511 | 0.04428753 | 0.04831937 | 0.0506212  | 0.99328919 |
| 1.98 | 0.03391617 | 0.03486647 | 0.03845436 | 0.0395211  | 0.04164229 | 0.04288699 | 0.04683338 | 0.04908796 | 0.99324678 |
| 1.99 | 0.03276506 | 0.03369261 | 0.03719686 | 0.03823939 | 0.04031329 | 0.04153074 | 0.04539309 | 0.04760117 | 0.99320402 |
| 2    | 0.03165302 | 0.03255826 | 0.03598048 | 0.03699924 | 0.0390267  | 0.04021739 | 0.04399709 | 0.04615941 | 0.99316091 |
| 2.01 | 0.03057872 | 0.03146211 | 0.03480388 | 0.03579932 | 0.03778118 | 0.03894556 | 0.04264403 | 0.04476131 | 0.99311745 |
| 2.02 | 0.02954088 | 0.03040286 | 0.03366575 | 0.03463831 | 0.0365754  | 0.03771396 | 0.04133257 | 0.04340557 | 0.99307363 |
| 2.03 | 0.02853827 | 0.02937927 | 0.03256484 | 0.03351495 | 0.03540811 | 0.0365213  | 0.04006145 | 0.04209088 | 0.99302947 |
| 2.04 | 0.02756968 | 0.02839015 | 0.03149993 | 0.03242803 | 0.03427807 | 0.03536636 | 0.03882942 | 0.04081602 | 0.99298496 |
| 2.05 | 0.02663397 | 0.02743432 | 0.03046985 | 0.03137635 | 0.03318409 | 0.03424795 | 0.03763528 | 0.03957977 | 0.9929401  |
| 2.06 | 0.02573001 | 0.02651068 | 0.02947345 | 0.03035879 | 0.03212503 | 0.0331649  | 0.03647786 | 0.03838096 | 0.99289489 |
| 2.07 | 0.02485674 | 0.02561813 | 0.02850963 | 0.02937422 | 0.03109977 | 0.0321161  | 0.03535604 | 0.03721846 | 0.99284933 |
| 2.08 | 0.02401311 | 0.02475564 | 0.02757734 | 0.02842158 | 0.03010723 | 0.03110047 | 0.03426872 | 0.03609118 | 0.99280342 |
| 2.09 | 0.0231981  | 0.02392218 | 0.02667553 | 0.02749984 | 0.02914637 | 0.03011696 | 0.03321484 | 0.03499803 | 0.99275716 |
| 2.1  | 0.02241076 | 0.02311678 | 0.02580321 | 0.02660799 | 0.02821617 | 0.02916455 | 0.03219336 | 0.033938   | 0.99271055 |
| 2.11 | 0.02165014 | 0.0223385  | 0.02495941 | 0.02574507 | 0.02731566 | 0.02824225 | 0.03120331 | 0.03291007 | 0.9926636  |
| 2.12 | 0.02091534 | 0.02158642 | 0.02414321 | 0.02491013 | 0.02644389 | 0.02734913 | 0.03024369 | 0.03191328 | 0.9926163  |
| 2.13 | 0.02020548 | 0.02085966 | 0.0233537  | 0.02410227 | 0.02559994 | 0.02648425 | 0.02931359 | 0.03094668 | 0.99256865 |
| 2.14 | 0.0195197  | 0.02015737 | 0.02259001 | 0.02332061 | 0.02478292 | 0.02564672 | 0.0284121  | 0.03000936 | 0.99252065 |
| 2.15 | 0.01885721 | 0.01947872 | 0.02185129 | 0.02256429 | 0.02399198 | 0.02483567 | 0.02753833 | 0.02910042 | 0.9924723  |
| 2.16 | 0.0182172  | 0.01882292 | 0.02113672 | 0.02183251 | 0.02322629 | 0.02405027 | 0.02669143 | 0.02821902 | 0.99242361 |
| 2.17 | 0.01759891 | 0.0181892  | 0.02044553 | 0.02112446 | 0.02248503 | 0.02328972 | 0.02587057 | 0.02736431 | 0.99237457 |
| 2.18 | 0.0170016  | 0.01757682 | 0.01977694 | 0.02043937 | 0.02176742 | 0.02255321 | 0.02507496 | 0.02653549 | 0.99232519 |
| 2.19 | 0.01642457 | 0.01698505 | 0.01913021 | 0.0197765  | 0.02107272 | 0.02183999 | 0.02430382 | 0.02573177 | 0.99227546 |
| 2.2  | 0.01586712 | 0.01641321 | 0.01850463 | 0.01913513 | 0.02040019 | 0.02114933 | 0.02355639 | 0.0249524  | 0.99222538 |
| 2.21 | 0.01532859 | 0.01586062 | 0.01789951 | 0.01851456 | 0.01974913 | 0.02048051 | 0.02283195 | 0.02419663 | 0.99217495 |
| 2.22 | 0.01480834 | 0.01532663 | 0.01731417 | 0.01791411 | 0.01911884 | 0.01983284 | 0.02212979 | 0.02346375 | 0.99212418 |
| 2.23 | 0.01430575 | 0.01481062 | 0.01674798 | 0.01733314 | 0.01850867 | 0.01920565 | 0.02144922 | 0.02275307 | 0.99207307 |
| 2.24 | 0.01382021 | 0.01431199 | 0.0162003  | 0.01677101 | 0.01791797 | 0.0185983  | 0.02078958 | 0.02206392 | 0.99202161 |
| 2.25 | 0.01335116 | 0.01383014 | 0.01567053 | 0.01622711 | 0.01734612 | 0.01801015 | 0.02015023 | 0.02139564 | 0.9919698  |
| 2.26 | 0.01289802 | 0.01336451 | 0.01515809 | 0.01570084 | 0.01679252 | 0.0174406  | 0.01953054 | 0.0207476  | 0.99191765 |
| 2.27 | 0.01246026 | 0.01291456 | 0.0146624  | 0.01519165 | 0.01625659 | 0.01688906 | 0.01892991 | 0.02011919 | 0.99186516 |
| 2.28 | 0.01203736 | 0.01247976 | 0.01418292 | 0.01469897 | 0.01573777 | 0.01635497 | 0.01834774 | 0.01950981 | 0.99181232 |
| 2.29 | 0.01162882 | 0.0120596  | 0.01371912 | 0.01422226 | 0.0152355  | 0.01583776 | 0.01778349 | 0.01891889 | 0.99175914 |

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| 2.3  | 0.01123414 | 0.01165359 | 0.01327049 | 0.01376102 | 0.01474927 | 0.01533691 | 0.01723658 | 0.01834587 | 0.99170561 |
| 2.31 | 0.01085285 | 0.01126124 | 0.01283653 | 0.01331474 | 0.01427855 | 0.0148519  | 0.0167065  | 0.0177902  | 0.99165174 |
| 2.32 | 0.01048451 | 0.0108821  | 0.01241676 | 0.01288293 | 0.01382285 | 0.01438223 | 0.01619271 | 0.01725137 | 0.99159753 |
| 2.33 | 0.01012866 | 0.01051573 | 0.01201072 | 0.01246512 | 0.0133817  | 0.01392741 | 0.01569473 | 0.01672885 | 0.99154298 |
| 2.34 | 0.0097849  | 0.01016169 | 0.01161796 | 0.01206086 | 0.01295463 | 0.01348697 | 0.01521206 | 0.01622216 | 0.99148808 |
| 2.35 | 0.0094528  | 0.00981957 | 0.01123804 | 0.01166972 | 0.01254118 | 0.01306047 | 0.01474424 | 0.01573082 | 0.99143284 |
| 2.36 | 0.00913197 | 0.00948897 | 0.01087054 | 0.01129126 | 0.01214094 | 0.01264745 | 0.0142908  | 0.01525436 | 0.99137726 |
| 2.37 | 0.00882203 | 0.0091695  | 0.01051506 | 0.01092507 | 0.01175346 | 0.01224749 | 0.01385131 | 0.01479233 | 0.99132133 |
| 2.38 | 0.00852261 | 0.00886079 | 0.01017121 | 0.01057076 | 0.01137835 | 0.01186017 | 0.01342533 | 0.01434429 | 0.99126507 |
| 2.39 | 0.00823336 | 0.00856247 | 0.00983859 | 0.01022794 | 0.01101522 | 0.01148511 | 0.01301246 | 0.01390983 | 0.99120846 |
| 2.4  | 0.00795392 | 0.00827419 | 0.00951686 | 0.00989623 | 0.01066367 | 0.01112191 | 0.01261228 | 0.01348852 | 0.99115151 |
| 2.41 | 0.00768396 | 0.00799562 | 0.00920565 | 0.00957529 | 0.01032334 | 0.01077019 | 0.01222441 | 0.01307998 | 0.99109422 |
| 2.42 | 0.00742317 | 0.00772643 | 0.00890461 | 0.00926475 | 0.00999387 | 0.0104296  | 0.01184846 | 0.0126838  | 0.9910366  |
| 2.43 | 0.00717123 | 0.0074663  | 0.00861342 | 0.00896429 | 0.00967492 | 0.01009978 | 0.01148408 | 0.01229963 | 0.99097863 |
| 2.44 | 0.00692784 | 0.00721493 | 0.00833175 | 0.00867357 | 0.00936615 | 0.00978038 | 0.01113091 | 0.0119271  | 0.99092032 |
| 2.45 | 0.00669271 | 0.00697202 | 0.0080593  | 0.00839227 | 0.00906723 | 0.00947109 | 0.01078859 | 0.01156584 | 0.99086167 |
| 2.46 | 0.00646556 | 0.00673729 | 0.00779575 | 0.0081201  | 0.00877785 | 0.00917158 | 0.0104568  | 0.01121553 | 0.99080268 |
| 2.47 | 0.00624612 | 0.00651046 | 0.00754082 | 0.00785676 | 0.00849771 | 0.00888154 | 0.01013522 | 0.01087583 | 0.99074336 |
| 2.48 | 0.00603413 | 0.00629127 | 0.00729422 | 0.00760196 | 0.00822651 | 0.00860067 | 0.00982353 | 0.01054642 | 0.99068369 |
| 2.49 | 0.00582933 | 0.00607946 | 0.00705569 | 0.00735542 | 0.00796396 | 0.00832869 | 0.00952142 | 0.01022699 | 0.99062369 |
| 2.5  | 0.00563148 | 0.00587478 | 0.00682497 | 0.00711687 | 0.00770979 | 0.0080653  | 0.0092286  | 0.00991723 | 0.99056335 |
| 2.51 | 0.00544035 | 0.00567699 | 0.00660178 | 0.00688607 | 0.00746374 | 0.00781025 | 0.00894479 | 0.00961685 | 0.99050267 |
| 2.52 | 0.00525571 | 0.00548586 | 0.0063859  | 0.00666274 | 0.00722554 | 0.00756326 | 0.00866971 | 0.00932557 | 0.99044166 |
| 2.53 | 0.00507733 | 0.00530117 | 0.00617707 | 0.00644666 | 0.00699493 | 0.00732408 | 0.00840308 | 0.00904312 | 0.9903803  |
| 2.54 | 0.004905   | 0.00512269 | 0.00597507 | 0.00623759 | 0.00677169 | 0.00709247 | 0.00814466 | 0.00876922 | 0.99031861 |
| 2.55 | 0.00473853 | 0.00495022 | 0.00577968 | 0.0060353  | 0.00655558 | 0.00686818 | 0.00789418 | 0.00850361 | 0.99025659 |
| 2.56 | 0.0045777  | 0.00478356 | 0.00559068 | 0.00583957 | 0.00634636 | 0.00665098 | 0.00765141 | 0.00824605 | 0.99019423 |
| 2.57 | 0.00442234 | 0.00462251 | 0.00540786 | 0.00565019 | 0.00614382 | 0.00644065 | 0.0074161  | 0.00799629 | 0.99013153 |
| 2.58 | 0.00427224 | 0.00446688 | 0.00523101 | 0.00546694 | 0.00594774 | 0.00623697 | 0.00718803 | 0.0077541  | 0.9900685  |
| 2.59 | 0.00412724 | 0.0043165  | 0.00505995 | 0.00528965 | 0.00575792 | 0.00603974 | 0.00696697 | 0.00751924 | 0.99000513 |
| 2.6  | 0.00398716 | 0.00417117 | 0.00489449 | 0.0051181  | 0.00557415 | 0.00584874 | 0.00675271 | 0.00729149 | 0.98994142 |
| 2.61 | 0.00385184 | 0.00403074 | 0.00473443 | 0.00495211 | 0.00539626 | 0.00566378 | 0.00654504 | 0.00707064 | 0.98987739 |
| 2.62 | 0.00372111 | 0.00389503 | 0.00457961 | 0.00479151 | 0.00522404 | 0.00548467 | 0.00634376 | 0.00685649 | 0.98981301 |
| 2.63 | 0.00359482 | 0.0037639  | 0.00442985 | 0.00463612 | 0.00505731 | 0.00531122 | 0.00614867 | 0.00664881 | 0.98974831 |
| 2.64 | 0.00347281 | 0.00363718 | 0.00428499 | 0.00448576 | 0.00489591 | 0.00514326 | 0.00595958 | 0.00644743 | 0.98968327 |
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| 2.66 | 0.00324108 | 0.00339639 | 0.00400932 | 0.00419952 | 0.00458839 | 0.00482311 | 0.00559866 | 0.00606278 | 0.98955219 |
| 2.67 | 0.00313107 | 0.00328204 | 0.00387821 | 0.00406333 | 0.00444196 | 0.00467058 | 0.00542648 | 0.00587915 | 0.98948615 |
| 2.68 | 0.00302481 | 0.00317154 | 0.00375139 | 0.00393155 | 0.00430019 | 0.00452288 | 0.00525959 | 0.00570108 | 0.98941978 |
| 2.69 | 0.00292214 | 0.00306477 | 0.00362872 | 0.00380405 | 0.00416295 | 0.00437985 | 0.00509784 | 0.0055284  | 0.98935308 |
| 2.7  | 0.00282297 | 0.00296158 | 0.00351005 | 0.00368068 | 0.00403009 | 0.00424134 | 0.00494107 | 0.00536096 | 0.98928605 |
| 2.71 | 0.00272716 | 0.00286187 | 0.00339527 | 0.00356131 | 0.00390147 | 0.00410722 | 0.00478911 | 0.00519858 | 0.98921868 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.72 | 0.0026346  | 0.00276552 | 0.00328424 | 0.00344581 | 0.00377696 | 0.00397733 | 0.00464183 | 0.00504113 | 0.98915099 |
| 2.73 | 0.00254518 | 0.00267241 | 0.00317684 | 0.00333406 | 0.00365642 | 0.00385155 | 0.00449908 | 0.00488844 | 0.98908296 |
| 2.74 | 0.00245879 | 0.00258244 | 0.00307296 | 0.00322593 | 0.00353973 | 0.00372975 | 0.00436071 | 0.00474038 | 0.9890146  |
| 2.75 | 0.00237534 | 0.0024955  | 0.00297247 | 0.00312131 | 0.00342676 | 0.0036118  | 0.00422661 | 0.0045968  | 0.98894592 |
| 2.76 | 0.00229472 | 0.00241148 | 0.00287526 | 0.00302009 | 0.00331739 | 0.00349759 | 0.00409662 | 0.00445757 | 0.9888769  |
| 2.77 | 0.00221684 | 0.00233029 | 0.00278124 | 0.00292214 | 0.00321152 | 0.00338698 | 0.00397064 | 0.00432256 | 0.98880756 |
| 2.78 | 0.0021416  | 0.00225184 | 0.00269029 | 0.00282737 | 0.00310902 | 0.00327987 | 0.00384853 | 0.00419163 | 0.98873789 |
| 2.79 | 0.00206892 | 0.00217602 | 0.00260231 | 0.00273568 | 0.0030098  | 0.00317615 | 0.00373017 | 0.00406467 | 0.98866789 |
| 2.8  | 0.0019987  | 0.00210276 | 0.00251722 | 0.00264696 | 0.00291374 | 0.00307571 | 0.00361546 | 0.00394156 | 0.98859756 |
| 2.81 | 0.00193086 | 0.00203197 | 0.0024349  | 0.00256111 | 0.00282075 | 0.00297844 | 0.00350427 | 0.00382218 | 0.9885269  |
| 2.82 | 0.00186533 | 0.00196356 | 0.00235528 | 0.00247806 | 0.00273073 | 0.00288425 | 0.0033965  | 0.00370641 | 0.98845591 |
| 2.83 | 0.00180202 | 0.00189745 | 0.00227826 | 0.00239769 | 0.00264358 | 0.00279304 | 0.00329205 | 0.00359415 | 0.9883846  |
| 2.84 | 0.00174086 | 0.00183357 | 0.00220375 | 0.00231993 | 0.00255921 | 0.00270471 | 0.0031908  | 0.00348529 | 0.98831297 |
| 2.85 | 0.00168178 | 0.00177183 | 0.00213169 | 0.00224469 | 0.00247753 | 0.00261918 | 0.00309268 | 0.00337973 | 0.988241   |
| 2.86 | 0.0016247  | 0.00171218 | 0.00206198 | 0.00217189 | 0.00239846 | 0.00253635 | 0.00299756 | 0.00327736 | 0.98816871 |
| 2.87 | 0.00156955 | 0.00165454 | 0.00199455 | 0.00210146 | 0.00232192 | 0.00245614 | 0.00290538 | 0.00317809 | 0.9880961  |
| 2.88 | 0.00151628 | 0.00159883 | 0.00192933 | 0.00203331 | 0.00224781 | 0.00237847 | 0.00281603 | 0.00308183 | 0.98802316 |
| 2.89 | 0.00146482 | 0.001545   | 0.00186624 | 0.00196736 | 0.00217608 | 0.00230326 | 0.00272943 | 0.00298849 | 0.98794989 |
| 2.9  | 0.00141511 | 0.00149299 | 0.00180521 | 0.00190356 | 0.00210663 | 0.00223042 | 0.00264549 | 0.00289797 | 0.98787631 |
| 2.91 | 0.00136708 | 0.00144272 | 0.00174618 | 0.00184182 | 0.00203939 | 0.00215988 | 0.00256413 | 0.0028102  | 0.98780239 |
| 2.92 | 0.00132068 | 0.00139415 | 0.00168907 | 0.00178209 | 0.00197431 | 0.00209158 | 0.00248527 | 0.00272508 | 0.98772816 |
| 2.93 | 0.00127585 | 0.00134721 | 0.00163384 | 0.0017243  | 0.0019113  | 0.00202544 | 0.00240884 | 0.00264254 | 0.9876536  |
| 2.94 | 0.00123255 | 0.00130186 | 0.00158041 | 0.00166838 | 0.0018503  | 0.00196138 | 0.00233476 | 0.00256251 | 0.98757872 |
| 2.95 | 0.00119072 | 0.00125803 | 0.00152873 | 0.00161427 | 0.00179125 | 0.00189936 | 0.00226296 | 0.00248489 | 0.98750351 |
| 2.96 | 0.00115031 | 0.00121567 | 0.00147874 | 0.00156192 | 0.00173408 | 0.00183929 | 0.00219337 | 0.00240963 | 0.98742799 |
| 2.97 | 0.00111127 | 0.00117474 | 0.00143038 | 0.00151126 | 0.00167874 | 0.00178113 | 0.00212591 | 0.00233664 | 0.98735214 |
| 2.98 | 0.00107355 | 0.00113519 | 0.00138361 | 0.00146225 | 0.00162516 | 0.0017248  | 0.00206053 | 0.00226587 | 0.98727597 |
| 2.99 | 0.00103711 | 0.00109697 | 0.00133836 | 0.00141483 | 0.00157329 | 0.00167026 | 0.00199716 | 0.00219724 | 0.98719948 |
| 3    | 0.00100191 | 0.00106004 | 0.00129459 | 0.00136894 | 0.00152308 | 0.00161744 | 0.00193574 | 0.00213069 | 0.98712267 |
| 3.01 | 0.00096791 | 0.00102435 | 0.00125226 | 0.00132455 | 0.00147447 | 0.00156629 | 0.00187621 | 0.00206616 | 0.98704554 |
| 3.02 | 0.00093506 | 0.00098986 | 0.00121131 | 0.00128159 | 0.00142742 | 0.00151676 | 0.00181851 | 0.00200358 | 0.98696809 |
| 3.03 | 0.00090332 | 0.00095654 | 0.0011717  | 0.00124003 | 0.00138186 | 0.00146879 | 0.00176259 | 0.00194289 | 0.98689032 |
| 3.04 | 0.00087266 | 0.00092433 | 0.00113338 | 0.00119981 | 0.00133776 | 0.00142234 | 0.00170838 | 0.00188404 | 0.98681223 |
| 3.05 | 0.00084305 | 0.00089321 | 0.00109632 | 0.0011609  | 0.00129507 | 0.00137736 | 0.00165584 | 0.00182698 | 0.98673383 |
| 3.06 | 0.00081443 | 0.00086314 | 0.00106047 | 0.00112325 | 0.00125373 | 0.00133381 | 0.00160492 | 0.00177164 | 0.9866551  |
| 3.07 | 0.00078679 | 0.00083408 | 0.00102579 | 0.00108682 | 0.00121372 | 0.00129163 | 0.00155556 | 0.00171798 | 0.98657606 |
| 3.08 | 0.00076009 | 0.000806   | 0.00099225 | 0.00105158 | 0.00117499 | 0.00125078 | 0.00150772 | 0.00166595 | 0.9864967  |
| 3.09 | 0.00073429 | 0.00077886 | 0.0009598  | 0.00101747 | 0.00113749 | 0.00121123 | 0.00146136 | 0.00161549 | 0.98641703 |
| 3.1  | 0.00070937 | 0.00075264 | 0.00092841 | 0.00098448 | 0.00110118 | 0.00117292 | 0.00141641 | 0.00156656 | 0.98633704 |
| 3.11 | 0.00068529 | 0.0007273  | 0.00089805 | 0.00095255 | 0.00106604 | 0.00113583 | 0.00137285 | 0.00151911 | 0.98625673 |
| 3.12 | 0.00066203 | 0.00070282 | 0.00086868 | 0.00092166 | 0.00103202 | 0.00109991 | 0.00133063 | 0.0014731  | 0.98617611 |
| 3.13 | 0.00063956 | 0.00067915 | 0.00084028 | 0.00089177 | 0.00099908 | 0.00106513 | 0.00128971 | 0.00142848 | 0.98609517 |



|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 3.14 | 0.00061786 | 0.00065629 | 0.0008128  | 0.00086284 | 0.0009672  | 0.00103144 | 0.00125005 | 0.00138521 | 0.98601392 |
| 3.15 | 0.00059689 | 0.00063419 | 0.00078622 | 0.00083486 | 0.00093633 | 0.00099883 | 0.00121161 | 0.00134326 | 0.98593235 |
| 3.16 | 0.00057663 | 0.00061284 | 0.00076051 | 0.00080779 | 0.00090645 | 0.00096724 | 0.00117435 | 0.00130257 | 0.98585047 |
| 3.17 | 0.00055706 | 0.00059221 | 0.00073564 | 0.00078159 | 0.00087752 | 0.00093665 | 0.00113823 | 0.00126312 | 0.98576828 |
| 3.18 | 0.00053815 | 0.00057227 | 0.00071158 | 0.00075624 | 0.00084951 | 0.00090703 | 0.00110323 | 0.00122486 | 0.98568577 |
| 3.19 | 0.00051989 | 0.000553   | 0.00068831 | 0.00073172 | 0.0008224  | 0.00087835 | 0.0010693  | 0.00118776 | 0.98560295 |
| 3.2  | 0.00050224 | 0.00053439 | 0.00066581 | 0.00070799 | 0.00079615 | 0.00085057 | 0.00103641 | 0.00115179 | 0.98551982 |
| 3.21 | 0.0004852  | 0.00051639 | 0.00064403 | 0.00068502 | 0.00077074 | 0.00082367 | 0.00100454 | 0.0011169  | 0.98543638 |
| 3.22 | 0.00046873 | 0.00049901 | 0.00062297 | 0.00066281 | 0.00074615 | 0.00079762 | 0.00097365 | 0.00108307 | 0.98535262 |
| 3.23 | 0.00045282 | 0.00048221 | 0.0006026  | 0.00064131 | 0.00072233 | 0.0007724  | 0.0009437  | 0.00105027 | 0.98526856 |
| 3.24 | 0.00043745 | 0.00046597 | 0.00058289 | 0.00062051 | 0.00069928 | 0.00074797 | 0.00091468 | 0.00101846 | 0.98518418 |
| 3.25 | 0.0004226  | 0.00045029 | 0.00056383 | 0.00060039 | 0.00067696 | 0.00072432 | 0.00088655 | 0.00098761 | 0.9850995  |
| 3.26 | 0.00040826 | 0.00043513 | 0.0005454  | 0.00058092 | 0.00065536 | 0.00070142 | 0.00085929 | 0.0009577  | 0.9850145  |
| 3.27 | 0.0003944  | 0.00042048 | 0.00052756 | 0.00056208 | 0.00063444 | 0.00067923 | 0.00083286 | 0.00092869 | 0.9849292  |
| 3.28 | 0.00038102 | 0.00040632 | 0.00051031 | 0.00054385 | 0.00061419 | 0.00065775 | 0.00080725 | 0.00090056 | 0.98484359 |
| 3.29 | 0.00036809 | 0.00039264 | 0.00049362 | 0.00052621 | 0.00059459 | 0.00063695 | 0.00078242 | 0.00087328 | 0.98475767 |
| 3.3  | 0.00035559 | 0.00037942 | 0.00047748 | 0.00050915 | 0.00057562 | 0.00061681 | 0.00075836 | 0.00084683 | 0.98467144 |
| 3.31 | 0.00034353 | 0.00036665 | 0.00046186 | 0.00049264 | 0.00055724 | 0.0005973  | 0.00073504 | 0.00082119 | 0.98458491 |
| 3.32 | 0.00033187 | 0.0003543  | 0.00044676 | 0.00047666 | 0.00053946 | 0.00057842 | 0.00071243 | 0.00079631 | 0.98449807 |
| 3.33 | 0.0003206  | 0.00034237 | 0.00043215 | 0.0004612  | 0.00052224 | 0.00056012 | 0.00069052 | 0.00077219 | 0.98441092 |
| 3.34 | 0.00030972 | 0.00033085 | 0.00041802 | 0.00044624 | 0.00050558 | 0.00054241 | 0.00066929 | 0.00074881 | 0.98432346 |
| 3.35 | 0.00029921 | 0.00031971 | 0.00040435 | 0.00043177 | 0.00048944 | 0.00052526 | 0.0006487  | 0.00072613 | 0.98423571 |
| 3.36 | 0.00028905 | 0.00030894 | 0.00039113 | 0.00041777 | 0.00047382 | 0.00050865 | 0.00062875 | 0.00070413 | 0.98414764 |
| 3.37 | 0.00027924 | 0.00029854 | 0.00037834 | 0.00040422 | 0.0004587  | 0.00049256 | 0.00060942 | 0.00068281 | 0.98405927 |
| 3.38 | 0.00026977 | 0.00028849 | 0.00036596 | 0.00039111 | 0.00044406 | 0.00047699 | 0.00059068 | 0.00066212 | 0.9839706  |
| 3.39 | 0.00026061 | 0.00027878 | 0.000354   | 0.00037843 | 0.00042989 | 0.0004619  | 0.00057251 | 0.00064207 | 0.98388162 |
| 3.4  | 0.00025177 | 0.00026939 | 0.00034242 | 0.00036615 | 0.00041617 | 0.00044729 | 0.0005549  | 0.00062262 | 0.98379235 |
| 3.41 | 0.00024322 | 0.00026032 | 0.00033122 | 0.00035428 | 0.00040289 | 0.00043315 | 0.00053784 | 0.00060376 | 0.98370276 |
| 3.42 | 0.00023497 | 0.00025156 | 0.00032039 | 0.00034279 | 0.00039003 | 0.00041945 | 0.0005213  | 0.00058548 | 0.98361288 |
| 3.43 | 0.00022699 | 0.00024309 | 0.00030992 | 0.00033167 | 0.00037758 | 0.00040619 | 0.00050527 | 0.00056774 | 0.98352269 |
| 3.44 | 0.00021929 | 0.00023491 | 0.00029978 | 0.00032092 | 0.00036553 | 0.00039334 | 0.00048973 | 0.00055055 | 0.98343221 |
| 3.45 | 0.00021184 | 0.000227   | 0.00028998 | 0.00031051 | 0.00035386 | 0.0003809  | 0.00047467 | 0.00053387 | 0.98334142 |
| 3.46 | 0.00020465 | 0.00021935 | 0.00028049 | 0.00030044 | 0.00034257 | 0.00036886 | 0.00046007 | 0.0005177  | 0.98325033 |
| 3.47 | 0.00019771 | 0.00021197 | 0.00027132 | 0.00029069 | 0.00033164 | 0.00035719 | 0.00044592 | 0.00050202 | 0.98315894 |
| 3.48 | 0.000191   | 0.00020483 | 0.00026245 | 0.00028127 | 0.00032105 | 0.0003459  | 0.00043221 | 0.00048682 | 0.98306726 |
| 3.49 | 0.00018452 | 0.00019794 | 0.00025387 | 0.00027214 | 0.00031081 | 0.00033496 | 0.00041891 | 0.00047207 | 0.98297527 |
| 3.5  | 0.00017825 | 0.00019127 | 0.00024557 | 0.00026332 | 0.00030089 | 0.00032437 | 0.00040603 | 0.00045777 | 0.98288299 |

Tabla 37 Multiorden para  $0 \geq n \geq 3.5$ ;  $n \neq 1$  a  $90^\circ$  C. Análisis completo.

| t (s)        | 0                         | 21600      | 86400      | 108000     | 172800     | 194400     | 259200     | 280800     | r          |
|--------------|---------------------------|------------|------------|------------|------------|------------|------------|------------|------------|
| Experimental | 31.6304951                | 28.1056084 | 21.5642384 | 19.9006143 | 14.091239  | 12.3011795 | 10.0985412 | 9.31331058 |            |
| n            | C <sup>Λ</sup> (1-n)(ppm) |            |            |            |            |            |            |            |            |
| 1.19         | 0.51877598                | 0.53055368 | 0.55794388 | 0.56652016 | 0.60492238 | 0.62074055 | 0.64445242 | 0.65444058 | 0.99755632 |
| 1.2          | 0.50116277                | 0.51314654 | 0.54106965 | 0.54982781 | 0.58912868 | 0.60535572 | 0.62972114 | 0.63999883 | 0.99755582 |
| 1.18         | 0.53700821                | 0.54855132 | 0.57534436 | 0.58371927 | 0.6211395  | 0.63651638 | 0.65952831 | 0.66920822 | 0.99755444 |
| 1.21         | 0.48414755                | 0.49631051 | 0.52470576 | 0.5336273  | 0.57374732 | 0.59035219 | 0.61532659 | 0.62587577 | 0.99755296 |
| 1.17         | 0.55588119                | 0.56715947 | 0.5932875  | 0.60144054 | 0.63779137 | 0.65269315 | 0.67495688 | 0.68430908 | 0.9975502  |
| 1.22         | 0.46771003                | 0.48002686 | 0.50883678 | 0.51790413 | 0.55876755 | 0.57572053 | 0.60126109 | 0.61206437 | 0.99754774 |
| 1.16         | 0.57541747                | 0.58639887 | 0.61179023 | 0.61969981 | 0.65488966 | 0.66928104 | 0.69074638 | 0.69975071 | 0.99754358 |
| 1.23         | 0.45183058                | 0.46427747 | 0.49344773 | 0.50264424 | 0.54417889 | 0.5614515  | 0.5875171  | 0.59855775 | 0.99754016 |
| 1.15         | 0.59564034                | 0.6062909  | 0.63087001 | 0.63851342 | 0.67244632 | 0.6862905  | 0.70690525 | 0.71554078 | 0.99753459 |
| 1.24         | 0.43649027                | 0.44904481 | 0.47852409 | 0.48783398 | 0.52997111 | 0.54753613 | 0.57408728 | 0.58534919 | 0.99753022 |
| 1.14         | 0.61657393                | 0.62685772 | 0.65054482 | 0.65789819 | 0.69047366 | 0.70373225 | 0.72344212 | 0.73168715 | 0.99752322 |
| 1.25         | 0.42167078                | 0.43431192 | 0.46405181 | 0.47346009 | 0.51613428 | 0.53396564 | 0.56096445 | 0.5724321  | 0.99751793 |
| 1.13         | 0.63824324                | 0.64812222 | 0.67083322 | 0.67787147 | 0.70898428 | 0.72161728 | 0.74036585 | 0.74819787 | 0.99750946 |
| 1.26         | 0.40735443                | 0.42006241 | 0.45001721 | 0.45950973 | 0.50265871 | 0.52073149 | 0.54814159 | 0.55980006 | 0.9975033  |
| 1.12         | 0.6606741                 | 0.67010806 | 0.69175436 | 0.69845113 | 0.72799115 | 0.73995684 | 0.75768548 | 0.76508116 | 0.99749333 |
| 1.27         | 0.39352414                | 0.40628042 | 0.43640708 | 0.44597042 | 0.48953497 | 0.50782535 | 0.53561184 | 0.54744677 | 0.99748632 |
| 1.11         | 0.68389329                | 0.69283971 | 0.71332796 | 0.71965556 | 0.74750756 | 0.7587625  | 0.77541027 | 0.78234543 | 0.9974748  |
| 1.28         | 0.38016342                | 0.39295061 | 0.42320856 | 0.43283003 | 0.47675387 | 0.49523908 | 0.5233685  | 0.53536609 | 0.997467   |
| 1.1          | 0.70792851                | 0.71634247 | 0.73557437 | 0.74150375 | 0.76754718 | 0.77804609 | 0.79354971 | 0.79999927 | 0.99745389 |
| 1.29         | 0.36725631                | 0.38005813 | 0.41040922 | 0.42007682 | 0.46430647 | 0.48296476 | 0.51140503 | 0.52355199 | 0.99744534 |
| 1.09         | 0.73280844                | 0.7406425  | 0.75851457 | 0.76401523 | 0.78812404 | 0.79781977 | 0.81211349 | 0.81805148 | 0.99743058 |
| 1.3          | 0.35478741                | 0.36758866 | 0.39799697 | 0.40769938 | 0.45218406 | 0.47099465 | 0.49971503 | 0.5119986  | 0.99742135 |
| 1.08         | 0.75856276                | 0.76576685 | 0.78217021 | 0.78721014 | 0.80925253 | 0.81809598 | 0.83111153 | 0.83651103 | 0.99740488 |
| 1.31         | 0.34274186                | 0.3555283  | 0.38596011 | 0.39568664 | 0.44037814 | 0.45932122 | 0.48829224 | 0.50070016 | 0.99739503 |
| 1.07         | 0.78522222                | 0.79174347 | 0.80656359 | 0.81110924 | 0.83094745 | 0.83888751 | 0.85055401 | 0.85538713 | 0.99737679 |
| 1.32         | 0.33110526                | 0.34386363 | 0.37428729 | 0.38402785 | 0.42888046 | 0.4479371  | 0.47713056 | 0.48965105 | 0.99736639 |
| 1.06         | 0.81281861                | 0.81860128 | 0.83171772 | 0.83573388 | 0.85322397 | 0.86020744 | 0.87045131 | 0.87468918 | 0.9973463  |
| 1.33         | 0.31986375                | 0.33258167 | 0.3629675  | 0.37271259 | 0.41768297 | 0.43683514 | 0.46622402 | 0.47884577 | 0.99733543 |
| 1.05         | 0.84138487                | 0.84637017 | 0.85765632 | 0.86110612 | 0.8760977  | 0.88206921 | 0.89081407 | 0.89442678 | 0.99731341 |
| 1.34         | 0.3090039                 | 0.32166987 | 0.35199006 | 0.36173072 | 0.40677783 | 0.42600834 | 0.4555668  | 0.46827892 | 0.99730215 |
| 1.04         | 0.87095509                | 0.87508105 | 0.88440387 | 0.88724864 | 0.89958464 | 0.90448658 | 0.91165319 | 0.91460977 | 0.99727812 |
| 1.35         | 0.29851276                | 0.31111608 | 0.34134462 | 0.35107243 | 0.39615741 | 0.41544988 | 0.44515318 | 0.45794526 | 0.99726657 |
| 1.03         | 0.90156454                | 0.90476587 | 0.91198559 | 0.91418482 | 0.92370124 | 0.92747369 | 0.9329798  | 0.93524819 | 0.99724043 |
| 1.36         | 0.28837781                | 0.30090855 | 0.33102113 | 0.34072819 | 0.38581428 | 0.4051531  | 0.4349776  | 0.44783964 | 0.99722867 |
| 1.02         | 0.93324975                | 0.93545767 | 0.94042749 | 0.94193876 | 0.94846436 | 0.951045   | 0.95480531 | 0.95635233 | 0.99720034 |
| 1.37         | 0.27858696                | 0.29103592 | 0.32100986 | 0.33068874 | 0.37574119 | 0.39511153 | 0.42503462 | 0.43795702 | 0.99718847 |

|      |            |            |            |            |            |             |            |            |            |
|------|------------|------------|------------|------------|------------|-------------|------------|------------|------------|
| 1.01 | 0.96604852 | 0.96719061 | 0.96975641 | 0.9705353  | 0.97389135 | 0.97521536  | 0.9771414  | 0.97793268 | 0.99715785 |
| 1.38 | 0.26912852 | 0.28148721 | 0.31130137 | 0.32094509 | 0.36593109 | 0.38531883  | 0.41531892 | 0.42829248 | 0.99714598 |
| 1.39 | 0.25999121 | 0.27225178 | 0.3018865  | 0.31148854 | 0.35637712 | 0.37576884  | 0.40582531 | 0.41884121 | 0.99710119 |
| 0.99 | 1.03514469 | 1.03392237 | 1.03118679 | 1.03035923 | 1.02680859 | 1.02541453  | 1.02339334 | 1.02256528 | 0.99706563 |
| 1.4  | 0.25116412 | 0.26331937 | 0.29275637 | 0.30231062 | 0.3470726  | 0.36645555  | 0.39654871 | 0.40959851 | 0.99705412 |
| 0.98 | 1.07152454 | 1.06899546 | 1.0633462  | 1.06164014 | 1.05433587 | 1.05147496  | 1.04733393 | 1.04563974 | 0.99701592 |
| 1.41 | 0.24263673 | 0.25468002 | 0.28390236 | 0.29340313 | 0.338011   | 0.35737308  | 0.38748416 | 0.40055977 | 0.99700476 |
| 0.97 | 1.10918294 | 1.10525831 | 1.09650855 | 1.09387071 | 1.08260113 | 1.0781977   | 1.07183457 | 1.06923489 | 0.99696379 |
| 1.42 | 0.23439885 | 0.24632412 | 0.27531614 | 0.28475809 | 0.32918599 | 0.34851571  | 0.37862682 | 0.39172049 | 0.99695313 |
| 0.96 | 1.14816483 | 1.14275129 | 1.13070514 | 1.12707978 | 1.11162413 | 1.10559959  | 1.09690836 | 1.09336247 | 0.99690926 |
| 1.43 | 0.22644067 | 0.23824238 | 0.26698959 | 0.27636778 | 0.32059139 | 0.33987788  | 0.36997194 | 0.38307626 | 0.99689922 |
| 0.95 | 1.18851673 | 1.18151612 | 1.1659682  | 1.16129705 | 1.14142521 | 1.13369789  | 1.12256871 | 1.1180345  | 0.99685232 |
| 1.44 | 0.21875267 | 0.23042579 | 0.25891486 | 0.26822469 | 0.31222118 | 0.33145412  | 0.3615149  | 0.3746228  | 0.99684305 |
| 0.94 | 1.23028679 | 1.22159594 | 1.20233101 | 1.19655314 | 1.1720252  | 1.16251029  | 1.14882934 | 1.14326325 | 0.99679297 |
| 1.45 | 0.21132569 | 0.22286566 | 0.25108435 | 0.26032153 | 0.30406951 | 0.32323915  | 0.35325117 | 0.36635588 | 0.99678461 |
| 0.93 | 1.27352484 | 1.26303536 | 1.23982785 | 1.23287956 | 1.20344554 | 1.19205494  | 1.1757043  | 1.16906131 | 0.9967312  |
| 1.46 | 0.20415087 | 0.21555357 | 0.24349066 | 0.25265123 | 0.29613066 | 0.31522779  | 0.34517634 | 0.35827138 | 0.99672392 |
| 0.92 | 1.31828248 | 1.30588051 | 1.27849411 | 1.27030884 | 1.23570822 | 1.22235046  | 1.20320795 | 1.1954415  | 0.99666703 |
| 1.47 | 0.19721965 | 0.20848139 | 0.23612663 | 0.24520694 | 0.28839909 | 0.30741498  | 0.3372861  | 0.35036529 | 0.99666098 |
| 0.91 | 1.36461311 | 1.35017906 | 1.31836623 | 1.30887443 | 1.26883581 | 1.25341592  | 1.231355   | 1.22241696 | 0.99660044 |
| 1.48 | 0.19052375 | 0.20164124 | 0.22898531 | 0.23798199 | 0.28086938 | 0.29979581  | 0.32957621 | 0.34263367 | 0.9965958  |
| 0.9  | 1.41257202 | 1.39598033 | 1.35948185 | 1.34861085 | 1.3028515  | 1.2852709   | 1.2601605  | 1.25000114 | 0.99653145 |
| 1.49 | 0.18405519 | 0.19502552 | 0.22205997 | 0.23096992 | 0.27353626 | 0.29236548  | 0.32204256 | 0.33507266 | 0.99652837 |
| 0.89 | 1.46221643 | 1.44333529 | 1.40187972 | 1.38955363 | 1.33777911 | 1.31793546  | 1.28963987 | 1.27820776 | 0.99646004 |
| 1.5  | 0.17780624 | 0.18862685 | 0.21534408 | 0.22416446 | 0.2663946  | 0.2851193   | 0.31468111 | 0.32767851 | 0.99645871 |
| 1.51 | 0.17176946 | 0.18243811 | 0.2088313  | 0.21755952 | 0.25943939 | 0.27805272  | 0.30748794 | 0.32044752 | 0.99638683 |
| 0.88 | 1.51360558 | 1.49229663 | 1.44559985 | 1.43173941 | 1.37364308 | 1.35143017  | 1.31980885 | 1.30705087 | 0.99638622 |
| 1.52 | 0.16593763 | 0.17645243 | 0.20251549 | 0.21114919 | 0.25266578 | 0.271116129 | 0.3004592  | 0.3133761  | 0.99631272 |
| 0.87 | 1.56680078 | 1.54291886 | 1.49068347 | 1.47520591 | 1.41046851 | 1.38577614  | 1.35068359 | 1.33654483 | 0.99631    |
| 1.53 | 0.1603038  | 0.17066313 | 0.1963907  | 0.20492775 | 0.24606902 | 0.26444065  | 0.29359112 | 0.30646073 | 0.9962364  |
| 0.86 | 1.62186551 | 1.59525832 | 1.53717311 | 1.51999202 | 1.44828117 | 1.42099499  | 1.38228059 | 1.36670434 | 0.99623136 |
| 1.54 | 0.15486125 | 0.16506378 | 0.19045114 | 0.19888961 | 0.23964449 | 0.25788659  | 0.28688004 | 0.29969796 | 0.99615787 |
| 0.85 | 1.67886548 | 1.64937326 | 1.5851126  | 1.5661378  | 1.48710755 | 1.45710891  | 1.41461675 | 1.3975444  | 0.99615031 |
| 1.55 | 0.14960348 | 0.15964814 | 0.18469121 | 0.19302939 | 0.23338769 | 0.25149496  | 0.28032236 | 0.29308443 | 0.99607713 |
| 0.84 | 1.73786869 | 1.7053239  | 1.63454718 | 1.61368454 | 1.5269748  | 1.49414065  | 1.44770936 | 1.42908037 | 0.99606686 |
| 1.56 | 0.14452422 | 0.15441018 | 0.17910549 | 0.18734183 | 0.22729426 | 0.24526175  | 0.27391459 | 0.28661685 | 0.9959942  |
| 0.83 | 1.79894555 | 1.76317252 | 1.68552346 | 1.66267475 | 1.56791083 | 1.53211353  | 1.48157612 | 1.46132796 | 0.99598099 |
| 1.57 | 0.13961741 | 0.14934407 | 0.17368869 | 0.18182186 | 0.22135991 | 0.23918302  | 0.26765328 | 0.28029198 | 0.99590908 |
| 0.82 | 1.86216894 | 1.8229835  | 1.73808953 | 1.71315227 | 1.60994431 | 1.57105148  | 1.51623513 | 1.49430323 | 0.99589272 |
| 1.58 | 0.1348772  | 0.14444419 | 0.16843572 | 0.17646454 | 0.2155805  | 0.23325496  | 0.2615351  | 0.27410669 | 0.99582178 |
| 0.81 | 1.92761429 | 1.88482341 | 1.79229496 | 1.76516225 | 1.65310464 | 1.61097902  | 1.55170494 | 1.5280226  | 0.99580204 |
| 1.59 | 0.13029791 | 0.13970506 | 0.16334162 | 0.17126506 | 0.20995198 | 0.22747382  | 0.25555678 | 0.26805789 | 0.99573229 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.8  | 1.99535971 | 1.94876108 | 1.84819089 | 1.81875122 | 1.69742204 | 1.65192129 | 1.5880045  | 1.56250285 | 0.99570896 |
| 1.6  | 0.12587411 | 0.13512142 | 0.15840159 | 0.16621879 | 0.20447042 | 0.22183596 | 0.24971511 | 0.26214257 | 0.99564064 |
| 0.79 | 2.06548601 | 2.01486767 | 1.90583003 | 1.8739671  | 1.74292752 | 1.6939041  | 1.62515323 | 1.59776115 | 0.99561347 |
| 1.61 | 0.1216005  | 0.13068817 | 0.15361095 | 0.1613212  | 0.19913197 | 0.21633784 | 0.24400697 | 0.25635778 | 0.99554682 |
| 0.78 | 2.13807688 | 2.08321675 | 1.96526675 | 1.93085929 | 1.78965295 | 1.73695388 | 1.66317099 | 1.63381508 | 0.99551559 |
| 1.62 | 0.11747198 | 0.12640037 | 0.14896521 | 0.15656792 | 0.19393291 | 0.21097598 | 0.23842931 | 0.25070065 | 0.99545085 |
| 0.77 | 2.21321894 | 2.15388439 | 2.02655712 | 1.98947869 | 1.83763101 | 1.78109774 | 1.70207811 | 1.67068256 | 0.99541529 |
| 1.63 | 0.11348363 | 0.12225325 | 0.14445996 | 0.15195469 | 0.18886958 | 0.20574702 | 0.23297915 | 0.24516836 | 0.99535272 |
| 0.76 | 2.29100184 | 2.22694924 | 2.08975893 | 2.04987772 | 1.8868953  | 1.82636351 | 1.7418954  | 1.70838198 | 0.9953126  |
| 1.64 | 0.10963069 | 0.1182422  | 0.14009098 | 0.14747739 | 0.18393845 | 0.20064765 | 0.22765357 | 0.23975815 | 0.99525246 |
| 0.75 | 2.37151839 | 2.30249262 | 2.15493181 | 2.11211043 | 1.9374803  | 1.87277968 | 1.78264416 | 1.74693209 | 0.99520751 |
| 1.65 | 0.10590857 | 0.11436274 | 0.13585412 | 0.14313202 | 0.17913607 | 0.19567467 | 0.22244973 | 0.23446733 | 0.99515005 |
| 0.74 | 2.45486468 | 2.38059862 | 2.22213721 | 2.17623247 | 1.98942141 | 1.9203755  | 1.82434616 | 1.78635209 | 0.99510003 |
| 1.66 | 0.10231282 | 0.11061057 | 0.13174541 | 0.13891467 | 0.17445907 | 0.19082494 | 0.21736484 | 0.22929327 | 0.99504552 |
| 0.73 | 2.54114015 | 2.46135416 | 2.29143854 | 2.24230121 | 2.04275498 | 1.96918094 | 1.86702371 | 1.82666162 | 0.99499015 |
| 1.67 | 0.09883915 | 0.1069815  | 0.12776095 | 0.13482159 | 0.16990417 | 0.18609542 | 0.21239618 | 0.22423338 | 0.99493886 |
| 0.72 | 2.63044774 | 2.54484911 | 2.36290116 | 2.31037574 | 2.09751836 | 2.01922675 | 1.91069963 | 1.86788074 | 0.99487788 |
| 1.68 | 0.09548341 | 0.10347151 | 0.123897   | 0.13084912 | 0.16546821 | 0.18148311 | 0.20754111 | 0.21928515 | 0.99483009 |
| 0.71 | 2.72289401 | 2.63117641 | 2.43659246 | 2.38051696 | 2.15374986 | 2.07054445 | 1.95539727 | 1.91002998 | 0.99476321 |
| 1.69 | 0.09224161 | 0.10007667 | 0.12014991 | 0.12699369 | 0.16114805 | 0.17698511 | 0.20279701 | 0.21444611 | 0.99471921 |
| 0.7  | 2.81858929 | 2.72043214 | 2.51258196 | 2.45278762 | 2.21148885 | 2.12316637 | 2.00114055 | 1.95313034 | 0.99464616 |
| 1.7  | 0.08910987 | 0.09679321 | 0.11651615 | 0.12325185 | 0.1569407  | 0.1725986  | 0.19816135 | 0.20971386 | 0.99460623 |
| 0.69 | 2.91764774 | 2.81271563 | 2.59094133 | 2.52725235 | 2.27077574 | 2.17712565 | 2.04795391 | 1.99720326 | 0.99452672 |
| 1.71 | 0.08608446 | 0.09361749 | 0.11299228 | 0.11962028 | 0.15284319 | 0.16832081 | 0.19363166 | 0.20508604 | 0.99449116 |
| 0.68 | 3.02018758 | 2.9081296  | 2.67174448 | 2.60397778 | 2.33165203 | 2.23245627 | 2.09586239 | 2.0422707  | 0.9944049  |
| 1.72 | 0.08316176 | 0.09054595 | 0.10957499 | 0.1160957  | 0.14885266 | 0.16414904 | 0.18920551 | 0.20056034 | 0.994374   |
| 0.67 | 3.12633114 | 3.00678024 | 2.75506761 | 2.68303254 | 2.39416033 | 2.2891931  | 2.14489161 | 2.08835511 | 0.9942807  |
| 1.73 | 0.0803383  | 0.0875752  | 0.10626105 | 0.11267497 | 0.14496631 | 0.16008066 | 0.18488054 | 0.19613451 | 0.99425476 |
| 0.66 | 3.23620509 | 3.10877733 | 2.84098933 | 2.76448733 | 2.45834438 | 2.34737187 | 2.19506779 | 2.13547941 | 0.99415412 |
| 1.74 | 0.07761069 | 0.08470191 | 0.10304733 | 0.10935504 | 0.14118144 | 0.15611312 | 0.18065443 | 0.19180635 | 0.99413345 |
| 0.65 | 3.34994052 | 3.21423441 | 2.92959067 | 2.84841503 | 2.52424912 | 2.40702923 | 2.24641776 | 2.1836671  | 0.99402517 |
| 1.75 | 0.0749757  | 0.08192289 | 0.09993081 | 0.10613293 | 0.13749538 | 0.15224391 | 0.17652492 | 0.1875737  | 0.99401008 |
| 0.64 | 3.46767316 | 3.32326885 | 3.0209552  | 2.93489071 | 2.59192067 | 2.46820275 | 2.29896897 | 2.23294215 | 0.99389384 |
| 1.76 | 0.07243016 | 0.07923505 | 0.09690854 | 0.10300575 | 0.13390556 | 0.1484706  | 0.17248981 | 0.18343445 | 0.99388466 |
| 0.63 | 3.58954346 | 3.43600199 | 3.1151691  | 3.02399173 | 2.6614064  | 2.53093096 | 2.35274954 | 2.2833291  | 0.99376014 |
| 1.77 | 0.06997105 | 0.07663539 | 0.09397768 | 0.09997072 | 0.13040947 | 0.14479081 | 0.16854693 | 0.17938654 | 0.99375718 |
| 1.78 | 0.06759543 | 0.07412103 | 0.09113546 | 0.09702511 | 0.12700466 | 0.14120222 | 0.16469418 | 0.17542796 | 0.99362767 |
| 0.62 | 3.71569687 | 3.5525593  | 3.21232123 | 3.11579778 | 2.73275494 | 2.59525339 | 2.40778821 | 2.33485305 | 0.99362407 |
| 1.79 | 0.06530046 | 0.07168917 | 0.08837919 | 0.09416629 | 0.12368873 | 0.13770258 | 0.1609295  | 0.17155673 | 0.99349613 |
| 0.61 | 3.84628389 | 3.67307052 | 3.31250322 | 3.21039099 | 2.80601624 | 2.66121054 | 2.46411442 | 2.38753965 | 0.99348565 |
| 1.8  | 0.06308342 | 0.06933709 | 0.08570629 | 0.09139171 | 0.12045939 | 0.13428967 | 0.15725088 | 0.16777094 | 0.99336256 |
| 0.6  | 3.98146036 | 3.79766976 | 3.41580956 | 3.30785599 | 2.88124157 | 2.72884395 | 2.52175828 | 2.44141515 | 0.99334486 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 1.81 | 0.06094164 | 0.06706218 | 0.08311422 | 0.08869888 | 0.11731436 | 0.13096135 | 0.15365635 | 0.16406868 | 0.99322697 |
| 0.59 | 4.12138756 | 3.9264957  | 3.5223377  | 3.40827994 | 2.95848359 | 2.79819624 | 2.58075063 | 2.49650635 | 0.99320171 |
| 1.82 | 0.05887258 | 0.06486191 | 0.08060055 | 0.0860854  | 0.11425144 | 0.12771552 | 0.15014398 | 0.16044813 | 0.99308938 |
| 0.58 | 4.26623246 | 4.05969172 | 3.63218811 | 3.51175268 | 3.03779635 | 2.86931109 | 2.64112301 | 2.55284071 | 0.99305621 |
| 1.83 | 0.05687377 | 0.06273383 | 0.0781629  | 0.08354892 | 0.11126849 | 0.12455013 | 0.1467119  | 0.15690747 | 0.99294979 |
| 0.57 | 4.41616789 | 4.19740607 | 3.7454644  | 3.61836678 | 3.11923538 | 2.94223329 | 2.7029077  | 2.61044626 | 0.99290836 |
| 1.84 | 0.05494282 | 0.06067557 | 0.07579898 | 0.08108717 | 0.10836342 | 0.1214632  | 0.14335827 | 0.15344494 | 0.99280821 |
| 0.56 | 4.57137276 | 4.33979201 | 3.86227342 | 3.7282176  | 3.20285767 | 3.01700877 | 2.76613774 | 2.6693517  | 0.99275817 |
| 1.85 | 0.05307743 | 0.05868484 | 0.07350654 | 0.07869796 | 0.10553419 | 0.11845278 | 0.1400813  | 0.15005882 | 0.99266464 |
| 0.55 | 4.73203225 | 4.48700802 | 3.98272533 | 3.84140341 | 3.28872176 | 3.09368463 | 2.83084694 | 2.72958636 | 0.99260563 |
| 1.86 | 0.05127538 | 0.05675943 | 0.07128344 | 0.07637915 | 0.10277884 | 0.11551697 | 0.13687924 | 0.14674742 | 0.9925191  |
| 0.54 | 4.89833807 | 4.63921795 | 4.10693375 | 3.95802545 | 3.37688774 | 3.17230917 | 2.8970699  | 2.79118023 | 0.99245076 |
| 1.87 | 0.0495345  | 0.05489719 | 0.06912757 | 0.07412866 | 0.10009542 | 0.11265392 | 0.13375037 | 0.1435091  | 0.9923716  |
| 0.53 | 5.07048865 | 4.79659119 | 4.23501584 | 4.07818804 | 3.46741733 | 3.25293192 | 2.96484204 | 2.85416398 | 0.99229355 |
| 1.88 | 0.04785273 | 0.05309604 | 0.06703691 | 0.07194448 | 0.09748207 | 0.10986184 | 0.13069302 | 0.14034224 | 0.99222213 |
| 0.52 | 5.24868942 | 4.95930291 | 4.36709239 | 4.20199868 | 3.56037388 | 3.33560366 | 3.0341996  | 2.91856897 | 0.99213402 |
| 1.89 | 0.04622806 | 0.051354   | 0.06500947 | 0.06982466 | 0.09493694 | 0.10713895 | 0.12770556 | 0.13724526 | 0.99207072 |
| 0.51 | 5.433153   | 5.1275342  | 4.50328799 | 4.32956812 | 3.65582248 | 3.42037647 | 3.10517967 | 2.98442729 | 0.99197215 |
| 1.9  | 0.04465855 | 0.0496691  | 0.06304335 | 0.0677673  | 0.09245826 | 0.10448355 | 0.12478639 | 0.13421663 | 0.99191736 |
| 0.5  | 5.62409949 | 5.30147228 | 4.64373109 | 4.46101046 | 3.75382991 | 3.50730373 | 3.17782019 | 3.05177171 | 0.99180797 |
| 1.91 | 0.04314233 | 0.04803949 | 0.06113669 | 0.06577055 | 0.0900443  | 0.10189396 | 0.12193395 | 0.13125483 | 0.99176208 |
| 0.49 | 5.82175674 | 5.48131076 | 4.78855416 | 4.59644329 | 3.85446478 | 3.59644021 | 3.25216002 | 3.12063578 | 0.99164147 |
| 1.92 | 0.04167758 | 0.04646334 | 0.0592877  | 0.06383264 | 0.08769337 | 0.09936856 | 0.11914671 | 0.12835838 | 0.99160487 |
| 0.48 | 6.0263606  | 5.66724979 | 4.9378938  | 4.73598776 | 3.95779754 | 3.68784205 | 3.3282389  | 3.19105379 | 0.99147266 |
| 1.93 | 0.04026256 | 0.04493891 | 0.05749463 | 0.06195183 | 0.08540381 | 0.09690574 | 0.11642318 | 0.12552586 | 0.99144574 |
| 0.47 | 6.23815519 | 5.85949631 | 5.09189086 | 4.87976869 | 4.0639005  | 3.78156683 | 3.40609753 | 3.2630608  | 0.99130154 |
| 1.94 | 0.03889559 | 0.04346449 | 0.05575578 | 0.06012644 | 0.08317403 | 0.09450397 | 0.11376191 | 0.12275584 | 0.99128471 |
| 0.46 | 6.45739324 | 6.05826428 | 5.25069059 | 5.0279147  | 4.17284792 | 3.87767358 | 3.48577753 | 3.33669266 | 0.99112812 |
| 1.95 | 0.03757503 | 0.04203845 | 0.05406953 | 0.05835483 | 0.08100247 | 0.09216172 | 0.11116147 | 0.12004695 | 0.99112178 |
| 1.96 | 0.0362993  | 0.04065919 | 0.05243427 | 0.05663543 | 0.07888761 | 0.08987753 | 0.10862048 | 0.11739783 | 0.99095696 |
| 0.45 | 6.68433634 | 6.26377494 | 5.41444278 | 5.1805583  | 4.28471608 | 3.97622283 | 3.5673215  | 3.41198605 | 0.9909524  |
| 1.97 | 0.03506689 | 0.03932519 | 0.05084847 | 0.05496668 | 0.07682796 | 0.08764995 | 0.10613756 | 0.11480718 | 0.99079026 |
| 0.44 | 6.91925529 | 6.476257   | 5.58330188 | 5.33783605 | 4.39958326 | 4.07727667 | 3.65077307 | 3.48897846 | 0.99077439 |
| 1.98 | 0.03387631 | 0.03803495 | 0.04931063 | 0.0533471  | 0.07482208 | 0.08547757 | 0.10371141 | 0.11227369 | 0.99062169 |
| 0.43 | 7.16243039 | 6.69594696 | 5.75742715 | 5.49988863 | 4.51752987 | 4.18089875 | 3.73617685 | 3.56770822 | 0.99059409 |
| 1.99 | 0.03272616 | 0.03678705 | 0.0478193  | 0.05177525 | 0.07286858 | 0.08335904 | 0.10134071 | 0.10979611 | 0.99045125 |
| 0.42 | 7.41415181 | 6.92308932 | 5.93698282 | 5.666861   | 4.63863846 | 4.28715433 | 3.8235785  | 3.64821454 | 0.99041151 |
| 2    | 0.03161506 | 0.03558009 | 0.04637307 | 0.05024971 | 0.07096608 | 0.08129302 | 0.0990242  | 0.1073732  | 0.99027897 |
| 0.41 | 7.6747199  | 7.15793688 | 6.12213827 | 5.83890252 | 4.7629938  | 4.39611035 | 3.91302477 | 3.73053751 | 0.99022665 |
| 2.01 | 0.03054168 | 0.03441273 | 0.04497058 | 0.04876911 | 0.06911325 | 0.0792782  | 0.09676065 | 0.10500377 | 0.99010484 |
| 0.4  | 7.94444557 | 7.40075103 | 6.31306811 | 6.0161671  | 4.89068294 | 4.50783543 | 4.00456349 | 3.81471811 | 0.99003952 |
| 2.02 | 0.02950475 | 0.03328367 | 0.04361051 | 0.04733215 | 0.0673088  | 0.07731332 | 0.09454884 | 0.10268661 | 0.98992887 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.39 | 8.22365067 | 7.65180201 | 6.50995245 | 6.19881328 | 5.02179523 | 4.62239995 | 4.09824361 | 3.90079828 | 0.98985013 |
| 2.03 | 0.02850302 | 0.03219165 | 0.04229157 | 0.04593752 | 0.06555146 | 0.07539713 | 0.09238758 | 0.1004206  | 0.98975108 |
| 0.38 | 8.51266835 | 7.91136924 | 6.71297697 | 6.38700446 | 5.15642247 | 4.73987608 | 4.19411521 | 3.98882087 | 0.98965848 |
| 2.04 | 0.0275353  | 0.03113546 | 0.04101253 | 0.04458398 | 0.06384    | 0.07352844 | 0.09027573 | 0.09820458 | 0.98957147 |
| 0.37 | 8.81184347 | 8.17974159 | 6.92233318 | 6.58090899 | 5.29465887 | 4.86033781 | 4.29222958 | 4.07882971 | 0.98946457 |
| 2.05 | 0.02660043 | 0.03011392 | 0.03977216 | 0.04327033 | 0.06217322 | 0.07170607 | 0.08821215 | 0.09603747 | 0.98939005 |
| 0.36 | 9.121533   | 8.45721778 | 7.13821854 | 6.7807003  | 5.43660119 | 4.98386102 | 4.39263916 | 4.17086963 | 0.98926841 |
| 2.06 | 0.02569731 | 0.02912591 | 0.03856931 | 0.04199538 | 0.06054996 | 0.06992886 | 0.08619575 | 0.09391818 | 0.98920684 |
| 0.35 | 9.44210648 | 8.74410661 | 7.36083667 | 6.98655712 | 5.58234878 | 5.11052351 | 4.49539767 | 4.26498645 | 0.98907001 |
| 2.07 | 0.02482485 | 0.0281703  | 0.03740283 | 0.040758   | 0.05896908 | 0.0681957  | 0.08422543 | 0.09184566 | 0.98902183 |
| 0.34 | 9.77394641 | 9.04072739 | 7.59039755 | 7.1986636  | 5.73200366 | 5.24040507 | 4.60056003 | 4.36122705 | 0.98886938 |
| 2.08 | 0.02398201 | 0.02724605 | 0.03627164 | 0.03955708 | 0.05742948 | 0.06650549 | 0.08230016 | 0.08981887 | 0.98883505 |
| 0.33 | 10.1174488 | 9.34741024 | 7.82711769 | 7.41720947 | 5.88567058 | 5.3735875  | 4.7081825  | 4.45963934 | 0.98866651 |
| 2.09 | 0.02316778 | 0.02635212 | 0.03517465 | 0.03839154 | 0.05593007 | 0.06485718 | 0.08041889 | 0.08783681 | 0.98864649 |
| 0.32 | 10.4730234 | 9.66449651 | 8.07122037 | 7.64239021 | 6.04345709 | 5.51015471 | 4.81832261 | 4.56027233 | 0.98846143 |
| 2.1  | 0.0223812  | 0.02548753 | 0.03411084 | 0.03726034 | 0.05446982 | 0.06324971 | 0.07858063 | 0.08589849 | 0.98845617 |
| 2.11 | 0.02162133 | 0.0246513  | 0.03307921 | 0.03616248 | 0.05304768 | 0.06168209 | 0.07678438 | 0.08400294 | 0.98826411 |
| 0.31 | 10.8410946 | 9.99233909 | 8.32293583 | 7.87440728 | 6.20547363 | 5.65019271 | 4.93103927 | 4.66317613 | 0.98825412 |
| 2.12 | 0.02088725 | 0.0238425  | 0.03207878 | 0.03509696 | 0.05166268 | 0.06015332 | 0.0750292  | 0.08214922 | 0.98807029 |
| 0.3  | 11.2221015 | 10.3313029 | 8.58250149 | 8.1134682  | 6.37183361 | 5.79378971 | 5.04639275 | 4.76840199 | 0.9880446  |
| 2.13 | 0.0201781  | 0.02306025 | 0.0311086  | 0.03406284 | 0.05031384 | 0.05866245 | 0.07331414 | 0.0803364  | 0.98787475 |
| 0.29 | 11.6164988 | 10.6817651 | 8.85016217 | 8.35978683 | 6.54265346 | 5.94103616 | 5.16444473 | 4.87600229 | 0.98783288 |
| 2.14 | 0.01949302 | 0.02230365 | 0.03016776 | 0.03305919 | 0.04900021 | 0.05720852 | 0.07163828 | 0.07856359 | 0.98767748 |
| 0.28 | 12.0247571 | 11.0441158 | 9.12617033 | 8.6135835  | 6.71805276 | 6.09202481 | 5.28525834 | 4.98603063 | 0.98761896 |
| 2.15 | 0.01883121 | 0.02157188 | 0.02925538 | 0.03208511 | 0.04772088 | 0.05579063 | 0.07000073 | 0.07682991 | 0.98747849 |
| 0.27 | 12.4473635 | 11.4187584 | 9.41078629 | 8.87508524 | 6.89815426 | 6.24685076 | 5.40889819 | 5.09854178 | 0.98740285 |
| 2.16 | 0.01819186 | 0.02086412 | 0.02837059 | 0.03113973 | 0.04647495 | 0.05440788 | 0.06840061 | 0.07513448 | 0.9872778  |
| 0.26 | 12.8848223 | 11.8061097 | 9.70427852 | 9.14452597 | 7.08308402 | 6.40561154 | 5.53543039 | 5.21359178 | 0.98718455 |
| 2.17 | 0.01757422 | 0.02017958 | 0.02751256 | 0.03022221 | 0.04526155 | 0.0530594  | 0.06683707 | 0.07347646 | 0.98707542 |
| 0.25 | 13.3376554 | 12.2066008 | 10.0069238 | 9.42214672 | 7.2729715  | 6.56840716 | 5.66492259 | 5.33123792 | 0.98696408 |
| 2.18 | 0.01697755 | 0.0195175  | 0.02668049 | 0.02933172 | 0.04407984 | 0.05174434 | 0.06530927 | 0.07185503 | 0.98687135 |
| 0.24 | 13.8064032 | 12.6206776 | 10.3190077 | 9.70819581 | 7.46794958 | 6.73534015 | 5.79744405 | 5.45153877 | 0.98674143 |
| 2.19 | 0.01640113 | 0.01887715 | 0.02587357 | 0.02846747 | 0.04292897 | 0.05046187 | 0.06381639 | 0.07026938 | 0.9866656  |
| 0.23 | 14.291625  | 13.0488008 | 10.6408244 | 10.0029291 | 7.66815476 | 6.90651566 | 5.93306563 | 5.57455425 | 0.98651663 |
| 2.2  | 0.01584429 | 0.0182578  | 0.02509106 | 0.02762869 | 0.04180815 | 0.04921119 | 0.06235763 | 0.06871873 | 0.98645819 |
| 0.22 | 14.7938998 | 13.491447  | 10.9726776 | 10.3066103 | 7.87372715 | 7.08204152 | 6.07185985 | 5.7003456  | 0.98628966 |
| 2.21 | 0.01530635 | 0.01765877 | 0.02433222 | 0.02681461 | 0.0407166  | 0.04799151 | 0.06093223 | 0.06720229 | 0.98624912 |
| 0.21 | 15.3138268 | 13.9491088 | 11.3148802 | 10.6195111 | 8.08481064 | 7.26202828 | 6.21390094 | 5.82897547 | 0.98606055 |
| 2.22 | 0.01478668 | 0.0170794  | 0.02359632 | 0.02602453 | 0.03965354 | 0.04680206 | 0.0595394  | 0.06571931 | 0.9860384  |
| 0.2  | 15.8520266 | 14.4222956 | 11.667755  | 10.9419112 | 8.30155299 | 7.44658933 | 6.35926483 | 5.96050791 | 0.9858293  |
| 2.23 | 0.01428465 | 0.01651903 | 0.02288269 | 0.02525772 | 0.03861824 | 0.04564209 | 0.05817841 | 0.06426906 | 0.98582605 |
| 2.24 | 0.01379967 | 0.01597705 | 0.02219063 | 0.02451351 | 0.03760997 | 0.04451086 | 0.05684854 | 0.06285082 | 0.98561206 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 0.19 | 16.4091412 | 14.911534  | 12.0316348 | 11.2740992 | 8.52410589 | 7.6358409  | 6.50802928 | 6.09500842 | 0.98559591 |
| 2.25 | 0.01333115 | 0.01545286 | 0.02151951 | 0.02379123 | 0.03662803 | 0.04340768 | 0.05554906 | 0.06146387 | 0.98539646 |
| 0.18 | 16.9858354 | 15.4173685 | 12.4068629 | 11.6163721 | 8.75262513 | 7.82990222 | 6.66027382 | 6.23254396 | 0.98536039 |
| 2.26 | 0.01287853 | 0.01494586 | 0.02086868 | 0.02309023 | 0.03567172 | 0.04233183 | 0.05427928 | 0.06010753 | 0.98517925 |
| 0.17 | 17.5827974 | 15.9403621 | 12.7937931 | 11.9690362 | 8.98727064 | 8.02889551 | 6.81607987 | 6.37318304 | 0.98512276 |
| 2.27 | 0.01244129 | 0.01445549 | 0.02023754 | 0.02240988 | 0.03474038 | 0.04128266 | 0.05303854 | 0.05878111 | 0.98496044 |
| 0.16 | 18.2007394 | 16.4810969 | 13.1927905 | 12.3324069 | 9.22820666 | 8.23294613 | 6.97553075 | 6.51699567 | 0.98488302 |
| 2.28 | 0.01201889 | 0.01398122 | 0.01962548 | 0.02174958 | 0.03383335 | 0.04025948 | 0.05182615 | 0.05748397 | 0.98474005 |
| 0.15 | 18.8403988 | 17.0401747 | 13.6042313 | 12.7068093 | 9.47560184 | 8.44218259 | 7.13871171 | 6.66405347 | 0.98464117 |
| 2.29 | 0.01161083 | 0.0135225  | 0.01903194 | 0.02110874 | 0.03295001 | 0.03926166 | 0.05064148 | 0.05621545 | 0.98451807 |
| 0.14 | 19.5025388 | 17.6182177 | 14.0285036 | 13.0925782 | 9.72962933 | 8.65673671 | 7.30571002 | 6.81442968 | 0.98439723 |
| 2.3  | 0.01121663 | 0.01307884 | 0.01845634 | 0.02048677 | 0.03208973 | 0.03828858 | 0.04948388 | 0.05497493 | 0.98429453 |
| 0.13 | 20.1879496 | 18.2158693 | 14.4660076 | 13.4900587 | 9.99046694 | 8.87674361 | 7.47661498 | 6.96819916 | 0.98415119 |
| 2.31 | 0.0108358  | 0.01264973 | 0.01789816 | 0.01988314 | 0.03125191 | 0.03733961 | 0.04835275 | 0.05376178 | 0.98406942 |
| 0.12 | 20.8974489 | 18.8337947 | 14.917156  | 13.8996065 | 10.2582972 | 9.10234189 | 7.65151798 | 7.1254385  | 0.98390308 |
| 2.32 | 0.01046791 | 0.0122347  | 0.01735685 | 0.01929729 | 0.03043597 | 0.03641416 | 0.04724747 | 0.0525754  | 0.98384277 |
| 0.11 | 21.6318833 | 19.4726816 | 15.3823742 | 14.3215878 | 10.5333077 | 9.33367364 | 7.83051254 | 7.28622598 | 0.9836529  |
| 2.33 | 0.01011251 | 0.01183328 | 0.01683192 | 0.0187287  | 0.02964132 | 0.03551165 | 0.04616746 | 0.0514152  | 0.98361457 |
| 0.1  | 22.3921292 | 20.133241  | 15.8621011 | 14.7563802 | 10.8156908 | 9.57088458 | 8.01369438 | 7.45064168 | 0.98340066 |
| 2.34 | 0.00976918 | 0.01144504 | 0.01632286 | 0.01817686 | 0.02886743 | 0.0346315  | 0.04511214 | 0.05028061 | 0.98338485 |
| 2.35 | 0.0094375  | 0.01106954 | 0.0158292  | 0.01764129 | 0.02811374 | 0.03377317 | 0.04408094 | 0.04917105 | 0.9831536  |
| 0.09 | 23.1790937 | 20.8162081 | 16.3567891 | 15.2043725 | 11.1056442 | 9.81412413 | 8.20116146 | 7.61876746 | 0.98314636 |
| 2.36 | 0.00911708 | 0.01070635 | 0.01535047 | 0.01712149 | 0.02737973 | 0.03293612 | 0.04307331 | 0.04808598 | 0.98292085 |
| 0.08 | 23.9937158 | 21.5223431 | 16.8669049 | 15.6659655 | 11.4033708 | 10.0635455 | 8.39301402 | 7.79068705 | 0.98289001 |
| 2.37 | 0.00880754 | 0.01035508 | 0.01488621 | 0.01661701 | 0.02666488 | 0.03211981 | 0.04208871 | 0.04702485 | 0.98268659 |
| 0.07 | 24.8369676 | 22.2524319 | 17.3929295 | 16.1415721 | 11.709079  | 10.3193058 | 8.58935465 | 7.96648605 | 0.98263163 |
| 2.38 | 0.00850851 | 0.01001534 | 0.014436   | 0.0161274  | 0.0259687  | 0.03132373 | 0.04112663 | 0.04598714 | 0.98245085 |
| 0.06 | 25.7098552 | 23.0072871 | 17.9353591 | 16.6316177 | 12.0229829 | 10.5815661 | 8.79028834 | 8.146252   | 0.98237122 |
| 2.39 | 0.00821964 | 0.00968674 | 0.0139994  | 0.01565221 | 0.02529069 | 0.03054738 | 0.04018653 | 0.04497232 | 0.98221362 |
| 0.05 | 26.6134202 | 23.7877487 | 18.4947054 | 17.1365408 | 12.3453021 | 10.8504916 | 8.99592255 | 8.33007443 | 0.98210878 |
| 2.4  | 0.00794057 | 0.00936893 | 0.01357601 | 0.01519102 | 0.02463038 | 0.02979028 | 0.03926792 | 0.0439799  | 0.98197493 |
| 0.04 | 27.5487406 | 24.5946854 | 19.071496  | 17.6567929 | 12.6762622 | 11.1262518 | 9.20636722 | 8.51804485 | 0.98184434 |
| 2.41 | 0.00767097 | 0.00906154 | 0.01316543 | 0.01474342 | 0.02398732 | 0.02905194 | 0.03837031 | 0.04300939 | 0.98173477 |
| 0.03 | 28.5169327 | 25.4289953 | 19.6662747 | 18.1928395 | 13.0160949 | 11.4090203 | 9.4217349  | 8.71025688 | 0.98157789 |
| 2.42 | 0.00741053 | 0.00876423 | 0.01276726 | 0.01430901 | 0.02336104 | 0.02833189 | 0.03749322 | 0.04206028 | 0.98149316 |
| 0.02 | 29.5191515 | 26.2916069 | 20.2796027 | 18.7451601 | 13.365038  | 11.6989752 | 9.64214075 | 8.90680623 | 0.98130944 |
| 2.43 | 0.00715894 | 0.00847668 | 0.01238113 | 0.0138874  | 0.02275111 | 0.0276297  | 0.03663618 | 0.04113213 | 0.98125012 |
| 0.01 | 30.556593  | 27.1834804 | 20.9120584 | 19.3142487 | 13.7233358 | 11.9962991 | 9.86770263 | 9.10779077 | 0.98103901 |
| 2.44 | 0.00691588 | 0.00819857 | 0.01200668 | 0.01347821 | 0.02215711 | 0.02694491 | 0.03579872 | 0.04022445 | 0.98100564 |
| 0    | 31.6304951 | 28.1056084 | 21.5642384 | 19.9006143 | 14.091239  | 12.3011795 | 10.0985412 | 9.31331058 | 0.98076661 |
| 2.45 | 0.00668107 | 0.00792958 | 0.01164355 | 0.01308108 | 0.02157862 | 0.02627709 | 0.03498042 | 0.03933368 | 0.98075974 |
| 2.46 | 0.00645424 | 0.00766941 | 0.01129141 | 0.01269565 | 0.02101523 | 0.02562582 | 0.03418081 | 0.03846875 | 0.98051243 |

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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.47 | 0.00623511 | 0.00741779 | 0.01094992 | 0.01232158 | 0.02046655 | 0.02499069 | 0.03339949 | 0.03761984 | 0.98026372 |
| 2.48 | 0.00602342 | 0.00717441 | 0.01061875 | 0.01195852 | 0.0199322  | 0.02437131 | 0.03263602 | 0.03678968 | 0.98001362 |
| 2.49 | 0.00581892 | 0.00693902 | 0.0102976  | 0.01160617 | 0.0194118  | 0.02376727 | 0.03189001 | 0.03597783 | 0.97976213 |
| 2.5  | 0.00562136 | 0.00671136 | 0.00998617 | 0.0112642  | 0.01890498 | 0.02317821 | 0.03116105 | 0.03518389 | 0.97950928 |
| 2.51 | 0.0054305  | 0.00649116 | 0.00968415 | 0.0109323  | 0.0184114  | 0.02260375 | 0.03044875 | 0.03440748 | 0.97925507 |
| 2.52 | 0.00524613 | 0.00627819 | 0.00939127 | 0.01061018 | 0.0179307  | 0.02204352 | 0.02975273 | 0.0336482  | 0.9789995  |
| 2.53 | 0.00506801 | 0.00607221 | 0.00910724 | 0.01029756 | 0.01746255 | 0.02149718 | 0.02907263 | 0.03290567 | 0.9787426  |
| 2.54 | 0.00489595 | 0.00587298 | 0.0088318  | 0.00999414 | 0.01700663 | 0.02096438 | 0.02840807 | 0.03217953 | 0.97848436 |
| 2.55 | 0.00472972 | 0.00568029 | 0.0085647  | 0.00969967 | 0.01656261 | 0.02044478 | 0.0277587  | 0.03146941 | 0.9782248  |
| 2.56 | 0.00456914 | 0.00549393 | 0.00830567 | 0.00941387 | 0.01613018 | 0.01993807 | 0.02712417 | 0.03077497 | 0.97796393 |
| 2.57 | 0.00441401 | 0.00531368 | 0.00805448 | 0.0091365  | 0.01570905 | 0.01944391 | 0.02650415 | 0.03009585 | 0.97770176 |
| 2.58 | 0.00426415 | 0.00513934 | 0.00781088 | 0.00886729 | 0.0152989  | 0.018962   | 0.02589831 | 0.02943171 | 0.9774383  |
| 2.59 | 0.00411938 | 0.00497072 | 0.00757465 | 0.00860602 | 0.01489947 | 0.01849203 | 0.02530631 | 0.02878223 | 0.97717356 |
| 2.6  | 0.00397952 | 0.00480763 | 0.00734557 | 0.00835245 | 0.01451046 | 0.01803371 | 0.02472784 | 0.02814709 | 0.97690755 |
| 2.61 | 0.00384441 | 0.0046499  | 0.00712341 | 0.00810634 | 0.01413162 | 0.01758676 | 0.0241626  | 0.02752596 | 0.97664027 |
| 2.62 | 0.00371388 | 0.00449734 | 0.00690797 | 0.00786749 | 0.01376266 | 0.01715087 | 0.02361027 | 0.02691853 | 0.97637175 |
| 2.63 | 0.00358779 | 0.00434978 | 0.00669905 | 0.00763568 | 0.01340333 | 0.0167258  | 0.02307057 | 0.02632451 | 0.97610198 |
| 2.64 | 0.00346598 | 0.00420707 | 0.00649645 | 0.0074107  | 0.01305339 | 0.01631125 | 0.02254321 | 0.0257436  | 0.97583098 |
| 2.65 | 0.00334831 | 0.00406904 | 0.00629997 | 0.00719234 | 0.01271258 | 0.01590698 | 0.02202791 | 0.02517551 | 0.97555876 |
| 2.66 | 0.00323463 | 0.00393553 | 0.00610944 | 0.00698042 | 0.01238068 | 0.01551274 | 0.02152438 | 0.02461995 | 0.97528533 |
| 2.67 | 0.00312481 | 0.00380641 | 0.00592467 | 0.00677475 | 0.01205743 | 0.01512826 | 0.02103236 | 0.02407666 | 0.97501069 |
| 2.68 | 0.00301871 | 0.00368153 | 0.00574548 | 0.00657513 | 0.01174263 | 0.01475331 | 0.02055159 | 0.02354535 | 0.97473487 |
| 2.69 | 0.00291622 | 0.00356074 | 0.00557172 | 0.0063814  | 0.01143605 | 0.01438765 | 0.02008181 | 0.02302577 | 0.97445786 |
| 2.7  | 0.00281721 | 0.00344391 | 0.00540321 | 0.00619337 | 0.01113747 | 0.01403106 | 0.01962277 | 0.02251765 | 0.97417968 |
| 2.71 | 0.00272157 | 0.00333092 | 0.0052398  | 0.00601088 | 0.01084668 | 0.01368331 | 0.01917422 | 0.02202075 | 0.97390034 |
| 2.72 | 0.00262916 | 0.00322163 | 0.00508133 | 0.00583377 | 0.01056349 | 0.01334417 | 0.01873593 | 0.02153481 | 0.97361984 |
| 2.73 | 0.0025399  | 0.00311593 | 0.00492765 | 0.00566188 | 0.01028769 | 0.01301344 | 0.01830765 | 0.02105959 | 0.9733382  |
| 2.74 | 0.00245367 | 0.0030137  | 0.00477862 | 0.00549506 | 0.01001909 | 0.01269091 | 0.01788916 | 0.02059486 | 0.97305543 |
| 2.75 | 0.00237036 | 0.00291482 | 0.0046341  | 0.00533315 | 0.00975751 | 0.01237637 | 0.01748024 | 0.02014039 | 0.97277154 |
| 2.76 | 0.00228988 | 0.00281919 | 0.00449395 | 0.00517601 | 0.00950275 | 0.01206962 | 0.01708067 | 0.01969594 | 0.97248653 |
| 2.77 | 0.00221214 | 0.00272669 | 0.00435803 | 0.0050235  | 0.00925465 | 0.01177048 | 0.01669023 | 0.01926131 | 0.97220042 |
| 2.78 | 0.00213703 | 0.00263723 | 0.00422623 | 0.00487548 | 0.00901302 | 0.01147875 | 0.01630871 | 0.01883626 | 0.97191322 |
| 2.79 | 0.00206448 | 0.00255071 | 0.00409841 | 0.00473183 | 0.0087777  | 0.01119426 | 0.01593592 | 0.0184206  | 0.97162493 |
| 2.8  | 0.00199439 | 0.00246702 | 0.00397446 | 0.00459241 | 0.00854853 | 0.01091681 | 0.01557164 | 0.0180141  | 0.97133557 |
| 2.81 | 0.00192667 | 0.00238608 | 0.00385426 | 0.00445709 | 0.00832534 | 0.01064624 | 0.0152157  | 0.01761658 | 0.97104514 |
| 2.82 | 0.00186126 | 0.00230779 | 0.0037377  | 0.00432577 | 0.00810798 | 0.01038238 | 0.01486789 | 0.01722783 | 0.97075366 |
| 2.83 | 0.00179807 | 0.00223208 | 0.00362465 | 0.00419831 | 0.00789629 | 0.01012506 | 0.01452803 | 0.01684766 | 0.97046113 |
| 2.84 | 0.00173702 | 0.00215884 | 0.00351503 | 0.00407461 | 0.00769013 | 0.00987411 | 0.01419594 | 0.01647587 | 0.97016756 |
| 2.85 | 0.00167805 | 0.00208801 | 0.00340872 | 0.00395455 | 0.00748935 | 0.00962938 | 0.01387144 | 0.01611123 | 0.96987297 |
| 2.86 | 0.00162107 | 0.00201951 | 0.00330563 | 0.00383803 | 0.00729381 | 0.00939072 | 0.01355436 | 0.01575674 | 0.96957737 |
| 2.87 | 0.00156604 | 0.00195325 | 0.00320566 | 0.00372494 | 0.00710338 | 0.00915798 | 0.01324452 | 0.01540903 | 0.96928076 |
| 2.88 | 0.00151287 | 0.00188916 | 0.00310871 | 0.00361519 | 0.00691792 | 0.008931   | 0.01294177 | 0.015069   | 0.96898315 |



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|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 2.89 | 0.0014615  | 0.00182718 | 0.00301469 | 0.00350867 | 0.0067373  | 0.00870965 | 0.01264594 | 0.01473646 | 0.96868455 |
| 2.9  | 0.00141188 | 0.00176723 | 0.00292351 | 0.00340529 | 0.0065614  | 0.00849378 | 0.01235687 | 0.01441127 | 0.96838497 |
| 2.91 | 0.00136395 | 0.00170925 | 0.0028351  | 0.00330495 | 0.00639009 | 0.00828327 | 0.01207441 | 0.01409325 | 0.96808443 |
| 2.92 | 0.00131764 | 0.00165317 | 0.00274935 | 0.00320757 | 0.00622325 | 0.00807797 | 0.01179841 | 0.01378225 | 0.96778292 |
| 2.93 | 0.0012729  | 0.00159893 | 0.0026662  | 0.00311306 | 0.00606077 | 0.00787776 | 0.01152871 | 0.01347811 | 0.96748047 |
| 2.94 | 0.00122969 | 0.00154647 | 0.00258557 | 0.00302134 | 0.00590254 | 0.00768251 | 0.01126518 | 0.01318069 | 0.96717707 |
| 2.95 | 0.00118794 | 0.00149573 | 0.00250737 | 0.00293231 | 0.00574843 | 0.0074921  | 0.01100768 | 0.01288983 | 0.96687275 |
| 2.96 | 0.0011476  | 0.00144666 | 0.00243154 | 0.00284591 | 0.00559834 | 0.00730642 | 0.01075606 | 0.01260538 | 0.9665675  |
| 2.97 | 0.00110864 | 0.00139919 | 0.002358   | 0.00276206 | 0.00545218 | 0.00712533 | 0.01051019 | 0.01232721 | 0.96626134 |
| 2.98 | 0.001071   | 0.00135329 | 0.00228669 | 0.00268068 | 0.00530983 | 0.00694873 | 0.01026994 | 0.01205519 | 0.96595428 |
| 2.99 | 0.00103464 | 0.00130889 | 0.00221753 | 0.00260169 | 0.0051712  | 0.00677651 | 0.01003518 | 0.01178916 | 0.96564632 |
| 3    | 0.00099951 | 0.00126594 | 0.00215046 | 0.00252503 | 0.00503618 | 0.00660855 | 0.00980579 | 0.01152901 | 0.96533748 |
| 3.01 | 0.00096558 | 0.00122441 | 0.00208542 | 0.00245063 | 0.0049047  | 0.00644476 | 0.00958165 | 0.01127459 | 0.96502777 |
| 3.02 | 0.00093279 | 0.00118424 | 0.00202235 | 0.00237843 | 0.00477664 | 0.00628503 | 0.00936262 | 0.01102579 | 0.96471718 |
| 3.03 | 0.00090112 | 0.00114538 | 0.00196119 | 0.00230835 | 0.00465193 | 0.00612926 | 0.00914861 | 0.01078248 | 0.96440575 |
| 3.04 | 0.00087053 | 0.0011078  | 0.00190188 | 0.00224033 | 0.00453047 | 0.00597735 | 0.00893948 | 0.01054454 | 0.96409346 |
| 3.05 | 0.00084097 | 0.00107146 | 0.00184436 | 0.00217432 | 0.00441219 | 0.0058292  | 0.00873514 | 0.01031185 | 0.96378034 |
| 3.06 | 0.00081242 | 0.0010363  | 0.00178858 | 0.00211026 | 0.00429699 | 0.00568473 | 0.00853547 | 0.0100843  | 0.96346638 |
| 3.07 | 0.00078484 | 0.0010023  | 0.00173448 | 0.00204808 | 0.0041848  | 0.00554383 | 0.00834036 | 0.00986176 | 0.96315161 |
| 3.08 | 0.00075819 | 0.00096942 | 0.00168203 | 0.00198773 | 0.00407555 | 0.00540643 | 0.00814971 | 0.00964414 | 0.96283602 |
| 3.09 | 0.00073245 | 0.00093761 | 0.00163116 | 0.00192916 | 0.00396914 | 0.00527244 | 0.00796342 | 0.00943132 | 0.96251964 |
| 3.1  | 0.00070758 | 0.00090685 | 0.00158182 | 0.00187232 | 0.00386551 | 0.00514176 | 0.00778138 | 0.0092232  | 0.96220246 |
| 3.11 | 0.00068356 | 0.0008771  | 0.00153398 | 0.00181715 | 0.00376459 | 0.00501432 | 0.00760351 | 0.00901966 | 0.96188449 |
| 3.12 | 0.00066035 | 0.00084832 | 0.00148759 | 0.00176361 | 0.0036663  | 0.00489005 | 0.00742971 | 0.00882062 | 0.96156575 |
| 3.13 | 0.00063793 | 0.00082049 | 0.0014426  | 0.00171165 | 0.00357058 | 0.00476885 | 0.00725987 | 0.00862598 | 0.96124624 |
| 3.14 | 0.00061627 | 0.00079357 | 0.00139897 | 0.00166121 | 0.00347735 | 0.00465065 | 0.00709392 | 0.00843562 | 0.96092598 |
| 3.15 | 0.00059535 | 0.00076753 | 0.00135666 | 0.00161227 | 0.00338656 | 0.00453539 | 0.00693177 | 0.00824947 | 0.96060497 |
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| 3.17 | 0.00055561 | 0.00071799 | 0.00127584 | 0.00151866 | 0.00321204 | 0.00431336 | 0.00661849 | 0.0078894  | 0.95996073 |
| 3.18 | 0.00053675 | 0.00069443 | 0.00123726 | 0.00147391 | 0.00312817 | 0.00420645 | 0.0064672  | 0.0077153  | 0.95963753 |
| 3.19 | 0.00051852 | 0.00067165 | 0.00119984 | 0.00143048 | 0.0030465  | 0.0041022  | 0.00631937 | 0.00754505 | 0.95931361 |
| 3.2  | 0.00050092 | 0.00064961 | 0.00116355 | 0.00138833 | 0.00296696 | 0.00400053 | 0.00617492 | 0.00737855 | 0.95898899 |
| 3.21 | 0.00048391 | 0.0006283  | 0.00112836 | 0.00134743 | 0.0028895  | 0.00390137 | 0.00603377 | 0.00721572 | 0.95866367 |
| 3.22 | 0.00046748 | 0.00060769 | 0.00109423 | 0.00130772 | 0.00281406 | 0.00380468 | 0.00589584 | 0.00705649 | 0.95833766 |
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| 3.27 | 0.00039333 | 0.00051433 | 0.00093848 | 0.00112609 | 0.00246539 | 0.00335599 | 0.0052521  | 0.00631152 | 0.95669761 |
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| 3.3  | 0.00035461 | 0.00046535 | 0.00085588 | 0.00102945 | 0.00227728 | 0.00311259 | 0.0049001  | 0.00590283 | 0.95570587 |

|      |            |            |            |            |            |            |            |            |            |
|------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
| 3.31 | 0.00034257 | 0.00045008 | 0.00082999 | 0.00099912 | 0.00221783 | 0.00303545 | 0.00478809 | 0.00577257 | 0.95537406 |
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